

# From autonomous navigation to platooning in urban context

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**Abstract**—In this paper, the problem of autonomous navigation is addressed starting from the use of RTK-GPS until the use of vision as the main sensor. Using a decoupling strategy, it is possible to control separately lateral and longitudinal control in trajectory following tasks. Recent advances in vision, make possible to localize an urban vehicle in regard with a previously recorded trajectory.

The concept of sensory memory (GPS, Vision), which trades the learnt trajectory, is introduced and used to guide autonomously the vehicle. Then, an extension to vehicle platoon is described. Different kind of longitudinal control strategies are discussed : from a near to near approach, to a global strategy. Finally, in order to manage different kind of scenario which occur in a platoon context, a monitoring module is developed.

All theses aspects are currently addressed through the BODEGA (ROBEA-CNRS national interdisciplinary research program) and MOBIVIP (PREDIT3 national research program) projects.

## I. INTRODUCTION

In order to reduce and suppress nuisances, linked to the saturate traffic, new alternative "Urban Transportation Systems" are under development. Some of these projects, based on urban electric vehicles, have been already developed since the mid-90's, e.g. Praxitèle in France [12]-[4], CarLink in the USA [22], Crayon in Japan [7]. Such systems involve the capabilities of urban vehicles to be autonomously guided in a single or platoon configuration.

To move autonomously with the best efficiency, one of the most interesting functionality appears to be the platooning of vehicles composed of a leader followed by vehicles in a single file. Nevertheless, the automatic guided vehicles need to be localized the more accurate possible in their environment. Different approaches can be envisaged. Some applications, requiring equipped infrastructures, are in developing or developed: automatic vans in suspension over a guideway, thanks to Electro Magnetic forces, are described in [14], a fleet of urban shuttles detecting magnetic track integrated in the road pavement is described in [8]. The majority of Automated Highways Systems needs an equipped road with an adapted architecture as described in PATH project [10]. An alternative consists in relying on direct sensors (as cameras [5], radar [11],...), providing relative information with respect to the preceding vehicle without requiring an equipped infrastructure. Finally, mixed approaches are also investigated: in [21], the

authors combine a direct sensor (laser radar) with an inter-vehicles communication integrated in an equipped road infrastructure transmitting data from throttle and brake actuators. Unluckily, all these solutions have drawbacks: respectively the cost and the necessity to equip an area, and/or, a too small field of perception for the considered sensor. To overcome such problems, an interesting solution is the use of RTK GPS (Real Time Kinematic Global Positioning System) sensors, which can provide in realtime vehicle localization with a centimeter accuracy. These sensors, coupled with an inter-vehicles communication, permit to share absolute localization measurements. Some results of vehicles platoon control relying on this technology can be found in the literature: in [3], the authors develop particularly the GPS aspect, while in [17], the communication is studied.

This last approach was first developed in [2]: RTK-GPS sensors and inter-vehicles communication relying on WiFi technology are mounted on urban electric vehicles. Because of the problem of satellite visibility in urban context, more recently, we have started to investigate another perception system mainly based on vision data [19]. This novel approach [18] is currently under development and the first results in autonomous navigation are very promising.

One possible objective in platooning is to control vehicles velocity in order to keep either a constant cartesian distance or a constant time (see e.g. [9]) between the cars. Here, our aim is to keep a constant curvilinear distance between vehicles. The main advantage of curvilinear distance is that it agrees with the distance travelled (monotonous behavior) and is perfectly consistent when following reference paths with high curvature (which is not the case with cartesian distance).

Our platooning control design relies on nonlinear techniques, as in [6], instead of control approaches based on linear approximations (e.g. [15] [17]). These techniques can provide better tracking performances and allow to fully decouple longitudinal and lateral controls. Thanks to this decoupling feature, lateral guidance of each vehicle in the platoon can indeed be achieved independently, from its longitudinal control.

Usually, the standard approach to control a platoon is based on a local strategy, i.e. each vehicle is controlled from the unique data received from the single immediate front vehicle, see [2]. Such a local approach presents drawbacks,

like errors accumulation: the regulation errors, introduced by sensors noises, are growing from the first vehicle to the last one leading to unacceptable oscillations. To overcome these problems, inter-vehicles communication has to be considered: in [16], distance, velocity and acceleration with respect to the preceding vehicle are transmitted in order to compute the expected spacing error, and therefore to incorporate prediction in the controller. In [26], information from the immediate preceding and following vehicles are used in order to guarantee stability in tight platoon applications. We have developed a global control strategy in order to more widely capture the platoon behavior, information transmitted from the immediate front vehicle and the leader one are used to control each fleet element according to a global strategy.

The paper is organized as follows: first, modelling and theoretical concepts are addressed. Then, perception control and monitoring aspects of the work are presented. After, on one hand, full-scale experiments show the performances of a platoon composed of 2 vehicles, and, on the other hand, long platoon (10 cars) simulations are then reported.

## II. MODELLING AND THEORETICAL CONCEPTS

### A. Notations and Modelling

In our approach, we use a localization system (RTK-GPS or monocular vision) and inter-vehicles communication relying on WiFi technology. All the necessary equipments are mounted on urban electric vehicles called Cycabs (Fig. 1), which serve as development products in several French laboratories.



Fig. 1. Our experimental vehicles: Cycabs

The platoon architecture is presented on the Fig. 2. Each vehicle is equipped with an RTK-GPS (SAGITTA from Thales Navigation) and a monocular camera connected to a high level computer. A WIFI connection allows to receive the state of the platoon, and to send the state of the current vehicle. The low level control is based on a CAN architecture where two MPC555 micro-controllers pilot the heading and the longitudinal velocity of the vehicle.

1) *Notations*: Since Cycabs are devoted to move in urban environments, i.e. at low speed on asphalt, dynamic modelling can be unconsidered. Kinematic model can satisfactorily describe vehicle behavior, as corroborated by extensive tests done in various situations (different masses onboarded, on sloping grounds,...). In this paper, the celebrated tricycle

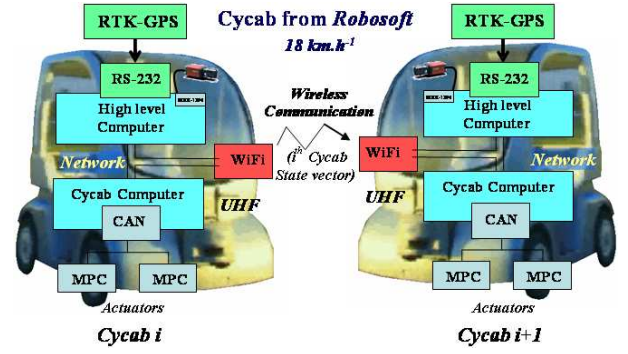


Fig. 2. Platoon architecture

model, validated by numerous laboratories [13] [20] [5] [23], is used to describe Cycab: the two actual front wheels are replaced by a unique virtual wheel located at the mid-distance between the actual wheels. The notations used are detailed and illustrated in Fig. 3:

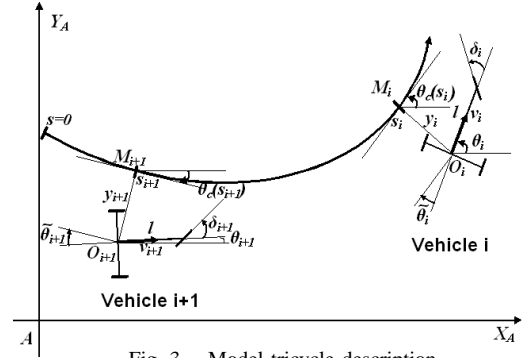


Fig. 3. Model tricycle description

- $C$  is the common reference path, defined in an absolute frame  $[A, X_A, Y_A]$ .
  - $O_i$  is the center of the  $i^{th}$  vehicle rear axle.
  - $M_i$  is the closest point on  $C$  to  $O_i$ .
  - $s_i$  is the curvilinear coordinate of point  $M_i$  along  $C$ , it corresponds to the distance covered along  $C$  by vehicle  $i$ .
  - $c(s_i)$  denotes the curvature of path  $C$  at  $M_i$ , and  $\theta_c(s_i)$  stands for the orientation of the tangent to  $C$  at  $M_i$ , with respect to frame  $[A, X_A, Y_A]$ .
  - $\theta_i$  is the heading of  $i^{th}$  Cycab at point  $O_i$ , with respect to frame  $[A, X_A, Y_A]$ .
  - $\hat{\theta}_i = \theta_i - \theta_c(s_i)$  denotes the angular deviation of the  $i^{th}$  vehicle with respect to  $C$ .
  - $y_i$  is the lateral deviation of the  $i^{th}$  vehicle with respect to  $C$ .
  - $\delta_i$  is the orientation of the  $i^{th}$  vehicle front wheel with respect to its centerline.
  - $L$  is Cycab wheelbase.
  - $v_i$  is the  $i^{th}$  vehicle linear velocity at point  $O_i$ .
  - $n$  is the number of vehicles in the platoon, so  $(i < n)$ .
- 2) *Modelling*: The vector  $(s_i, y_i, \hat{\theta}_i)$  describes the state of the  $i^{th}$  vehicle. It can be inferred online by comparing vehicle absolute localization (provided e.g. by a RTK-GPS sensor) to

the reference path. The celebrated tricycle model is (see [20], [5], [23]):

$$\begin{aligned}\dot{s}_i &= v_i \frac{\cos \tilde{\theta}_i}{1 - y_i c(s_i)} \\ \dot{y}_i &= v_i \sin \tilde{\theta}_i \\ \dot{\tilde{\theta}}_i &= v_i \left( \frac{\tan \delta_i}{L} - \frac{c(s_i) \cos \tilde{\theta}_i}{1 - y_i c(s_i)} \right)\end{aligned}\quad (1)$$

Lateral and longitudinal control objectives are to bring and maintain  $y_i$  and  $\tilde{\theta}_i$  to 0, by means of  $\delta_i$ , and the gap between cars to a fixed value  $d$ , by means of  $v_i$ . It is considered that:  $y_i \neq \frac{1}{c(s_i)}$  (i.e. vehicles are never on the reference path curvature center). In practical situation, if the  $n$  vehicles are well initialized, this singularity in model (1) is never met.

### B. Theoretical concepts

This section presents the conventional general navigation scheme and the adaptation we have done in order to take into account the imprecise map and the dynamic aspect of the environment.

1) *General scheme for navigation*: A general and well-known scheme for navigation is given by Fig. 4. The main concept uses the ability of the navigation system to present two levels :

- End user level : the user defines the mission, and the system elaborates an ordered set of reference trajectories. A specific module schedules the different reference trajectories during the execution.
- Execution level : The *obstacle avoidance module* permits to modify the reference trajectory in order to take into account the static and dynamic evolution of the scene. A *localization module* allows to extract the necessary information about the current vehicle (or the whole set of vehicle in case of platoon) in regard with the reference trajectory. The *control module* has in charge the execution of the trajectory following task. Finally, the *FDIR module* (*Failure Detection, Isolation and Recovery*) monitors the execution of the whole system in order to prevent from failures, and from different situations which can occur. In addition, on line reconfiguration of the whole system can be done using such module.

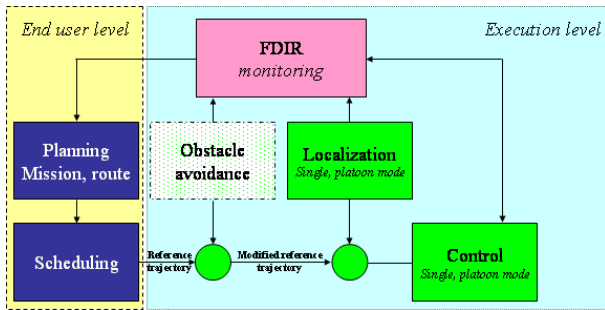


Fig. 4. General navigation scheme

This conventional system is efficient when the map of the environment is known with a centimeter accuracy for precise

navigation. Unfortunately, this hypothesis is difficult to guarantee : the map remains unprecise. So, instead of having a global view of the navigation system, we have preferred to use of a local view where each reference trajectory is defined in the sensor frame. This approach prevents from global errors of the map. As we have selected a local behaviour and a closed loop approach, the trajectory following task can be realized in good condition.

2) *Learning step : Concept of sensory memory*: In order to build a Topological representation of the environment, taking profit of the local perception of the reference trajectory, we have proposed to develop a learning step as represented in Fig. 5. During the learning step, the vehicle is driven by a human and acquires an ordered set of sensor information coming from proprioceptive and exteroceptive sensors. Theses information are stored (using the topological representation extracted from a GIS system) and represent the sensory memory of the reference trajectory. At the end, all the learnt trajectories are available in an Augmented GIS module.

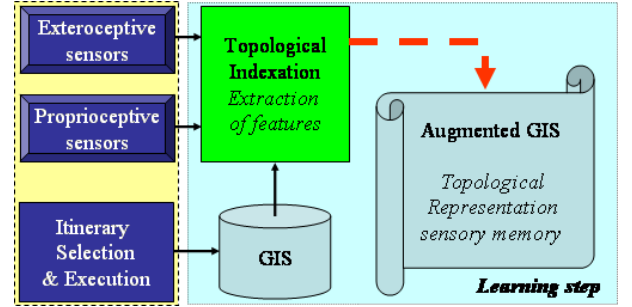


Fig. 5. Learning step : Sensory memory

3) *Localization step*: Completing the learning step, the system is ready to perform any autonomous displacements. After itinerary selection, a set of reference learnt trajectories are ready for execution. A localization module using the same sensors (used during the learning step), computes the necessary information in order to provide the control scheme. In the presented work, theses information are : the lateral deviation  $y_i$ , the angular deviation  $\tilde{\theta}_i$ , and the local datas of the reference trajectory (curvilinear abscissa  $s_i$ , local curvature  $c(s_i)$ )

## III. PERCEPTION, CONTROL AND MONITORING

In this section we will successively present the different aspects relating to perception, control and monitoring.

### A. Perception

For the perception aspect, we are currently addressing three main ways. The first one use an RTK-GPS (Real-Time Kinematic Global Positioning System) sensor in order to deliver an absolute localization of each vehicles. The second is a pure vision based approach and provide a relative localization of

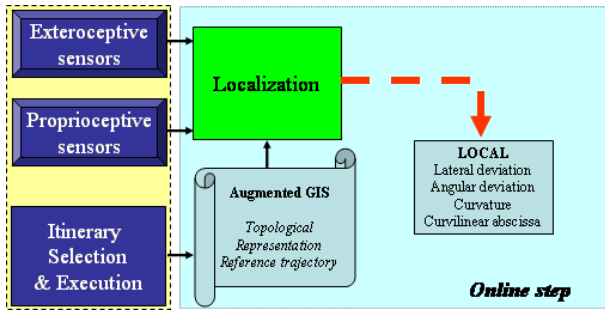


Fig. 6. Localization

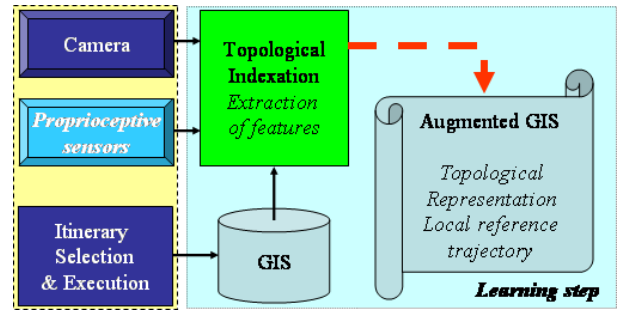


Fig. 8. Vision based memory

each vehicles, and the third one is supposed to take advantages of each approach by using data fusion techniques. We will present here only the two first ones (the last one is under development).

1) *Absolute Localization using RTK-GPS system:* The RTK GPS receiver is a Sagitta unit from Thales Navigation. It provides position measurements at a 10Hz sampling frequency, with a 2cm accuracy. The GPS reference station has been located on a 15m-height building. Each Cycab is equipped with a unique GPS sensor located on the roof of the vehicle straight up the mid-distance between the rear wheels. The radio receiver is in front of the vehicle. So, during the learning step (Fig. 7) the reference trajectory is extracted and stored in the GPS sensory memory. During the autonomous displacement, RTK-GPS sensor delivers the absolute localization, and the localization module is able to compute the relative position of the vehicle. To be available, GPS system needs at minimum the visibility of four satellites in any points of the reference trajectory, and at any time. Depending on the constellation, the quality and integrity of the signals are not always insured. Thanks to the news systems using the geostationary satellite EGNOS (for Europe) to improve theses points.

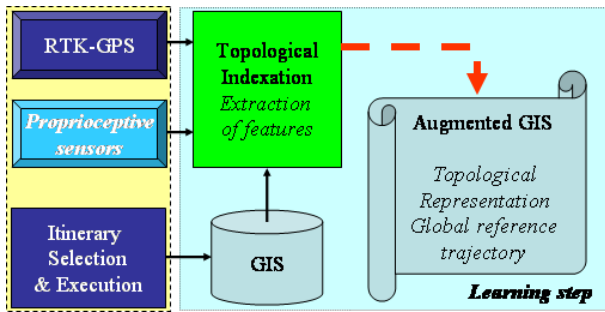


Fig. 7. GPS based memory

2) *Relative Localization using vision system:* Another solution is to design a system which can be embedded on the vehicle and offers the same kind functionalities as the GPS system does. Two years ago, we started to investigate a new approach based on a simple monocular camera [19].

During the learning step (Fig. 8), a camera acquires a

video sequence along a human driven trajectory. Then, a post processing algorithm extracts relevant information (here this is 3D points of the scene) from the video sequence in order to reconstruct the reference trajectory (using a bundle adjustment technique) and store it in an ordered way of key features. In on line step, the local extracted features are compared to the reference one in order to perform features matching, and then the localization procedure can be achieved. Fig. 9 represents an example of the visual memory (reference trajectory) learnt by vision in a real city center. The blue dots correspond to the 3D points of the environment, and small black squares represent the corresponding localization (obtained by 3D reconstruction) of the camera during the learning step.



Fig. 9. An example of Vision based memory of a reference trajectory

## B. Control

Our platooning control design relies on nonlinear techniques, as in [6]. These techniques can provide better tracking performances and allow to fully decouple longitudinal and lateral controls. Thanks to this decoupling feature, lateral guidance of each vehicle in the platoon can indeed be achieved independently, from its longitudinal control.

1) *Chained system*: As developed in [20], one way to build a nonlinear suitable control law for mobile robots is to turn their equations into chained form (as it has been done in [24]). In dimension 3 (as expected in our application), such a system is given by :

$$\begin{cases} \dot{a}_{1i} = m_{1i} \\ \dot{a}_{2i} = a_{3i} m_{1i} \\ \dot{a}_{3i} = m_{2i} \end{cases} \quad (2)$$

where  $A = (a_{1i}, a_{2i}, a_{3i})^T = \Theta(s_i, y_i, \tilde{\theta}_i)$  and  $M = (m_{1i}, m_{2i})^T = \Upsilon(v_i, \delta_i)$  are respectively the state and control vectors. One can check that such a system is almost linear: just replace time derivation by a derivation with respect to  $a_{1i}$ . It leads to system 3 (with notation  $(a_{ji})' = \frac{da_{ji}}{da_{1i}}$ ).

$$\begin{cases} a'_{1i} = 1 \\ a'_{2i} = a_{3i} \\ a'_{3i} = m_{3i} = \frac{m_{2i}}{m_{1i}} \end{cases} \quad (3)$$

The following state transformation

$$\begin{cases} a_{1i} = s_i \\ a_{2i} = y_i \\ a_{3i} = \tan \tilde{\theta}_i (1 - y_i c(s_i)) \end{cases}$$

is here proposed in association with control transformation given by :

$$\begin{cases} m_{1i} = v_i \frac{\cos \tilde{\theta}_i}{1 - y_i c(s_i)} \\ m_{2i} = \frac{d}{dt} \left( (1 - y_i c(s_i)) \tan \tilde{\theta}_i \right) \end{cases}$$

The new system 3 becomes in a linear form with longitudinal and lateral decoupling properties for trajectory following tasks.

2) *Lateral Control*: Path following can be now easily addressed : in view of the state transformation, the regulation of  $y_i$  and  $\tilde{\theta}_i$  is equivalent to regulation of  $a_{2i}$  and  $a_{3i}$ . So, the following auxiliary control law

$$m_{3i} = -k_d a_{3i} - k_p a_{2i} \quad (4)$$

provides the equation of a second order system :

$$a''_{2i} + k_d a'_{2i} + k_p a_{2i} = 0 \quad (5)$$

which can be tuned using the gains  $(k_p, k_d)$  to specify a settling distance (instead of a settling time). The following trajectory task is well achieved not depending on the value of the longitudinal velocity (as long as this value is not zero).

Such kind of lateral control techniques have been evaluated using both the GPS based memory in [23] and also the vision based memory in [18].

3) *Longitudinal Control*: The decoupling capabilities of the presented approach allows to be more flexible when considering a single vehicle or a platoon of vehicles. Indeed, it allows the user or a global system to impose a particular longitudinal velocity in single mode. In platoon mode the inter-distance between vehicle can be regulated through different control strategies.

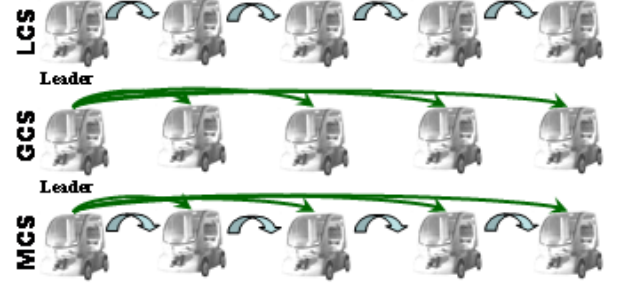


Fig. 10. Longitudinal control strategies

Fig. 10 illustrates the different control strategies which can be studied. The first one, called **LCS** is a local control strategy where the longitudinal control is based on a near to near approach. The second one, called **GCS**, is a global control strategy where the longitudinal control is based on the leader. Each of these solutions have drawbacks ([2] and [1]). This is the reason why, we have preferred to develop a third one, called **MCS**, which is a mixed strategy taking profit of advantages of both approaches depending on the context evolution.

So, we have proposed to regulate a new longitudinal error function (see Fig.11) defines by :

$$x_{i+1} = \sigma_{i+1} e_{i+1}^1 + (1 - \sigma_{i+1}) e_{i+1}^i \quad (6)$$

where

- $e_{i+1}^1$  represents the curvilinear distance between the current vehicle and the leader. In the GCS approach, this error is regulated to a desired distance  $i.d$ .
- $e_{i+1}^i$  represents the curvilinear distance between the current vehicle and the nearest front vehicle. In the LCS approach, this error is regulated to a desired distance  $d$ .
- $\sigma_{i+1}$  is a sigmoid function and gives more or less predominance at each error depending on the context.

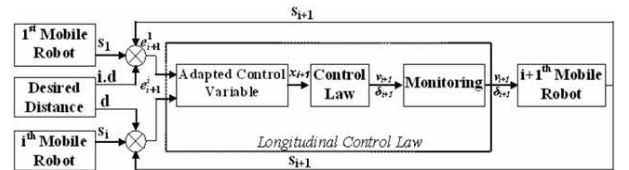


Fig. 11. Longitudinal control scheme



In order to design  $\sigma_{i+1}$ , security distance  $d_s$  is introduced as the minimal curvilinear distance that always must be observed between 2 vehicles. When distance between vehicles  $i$  and  $i+1$  is close to this limit, collision risk is important. Therefore, local approach must prevail over the absolute reference one.  $\sigma_{i+1}$  must then be close to 0 when  $e_{i+1}^i$  is close to  $-d + d_s$ . On the contrary, when inter-vehicles distance is close to  $d$ , absolute reference approach can be safely used.  $\sigma_{i+1}$  must then be close to 1 when  $e_{i+1}^i$  is close to 0. Such a commutation can be obtained via the sigmoid function (7):

$$\sigma_{i+1}(z_{i+1}) = 0.5 \left( \frac{1 - e^{-az_{i+1}}}{1 + e^{-az_{i+1}}} + 1 \right) \quad (7)$$

driven by variable  $z_{i+1}$  defined by:

$$z_{i+1} = e_{i+1}^i + \frac{d - d_s}{2}$$

Parameter  $a = 2.5$  is chosen to ensure the shape on Fig. 12.

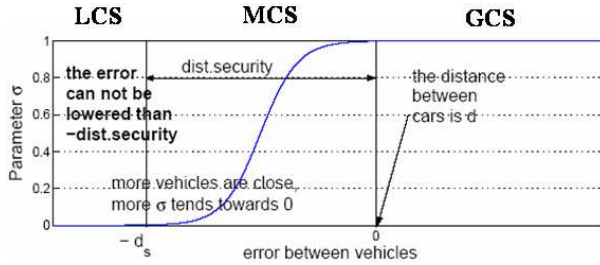


Fig. 12. Mode commutation using a sigmoid function

From the control point of view, we impose an exponential decrease of the new error function ( $\dot{x}_{i+1} = -kx_{i+1}$ ). Then, the longitudinal control law can be expressed by :

$$v_{i+1} = \frac{1 - y_{i+1} c(s_{i+1})}{\cos \bar{\theta}_{i+1} [1 + A(z_{i+1})(s_1 - s_i - id + d)]} \left( \sigma_{i+1} \frac{v_1 \cos \bar{\theta}_1}{1 - y_1 c(s_1)} + [1 - \sigma_{i+1} + A(z_{i+1})(s_1 - s_i + d - id)] \frac{v_i \cos \bar{\theta}_i}{1 - y_i c(s_i)} + kx_{i+1} \right) \quad (8)$$

where  $A(z_{i+1}) = \frac{a e^{(-a z_{i+1})}}{(1 + e^{(-a z_{i+1})})^2}$ .

### C. Monitoring

Control (8) presents one singularity, namely  $1 + (s_1 - s_i - (i - 1)d)A(z_{i+1}) = 0$ . However, it corresponds to a very special configuration of the first, the  $i^{th}$  and the  $(i + 1)^{th}$  vehicles, which is not expected to be met in practical situation. Moreover, if this configuration was met,  $v_{i+1}$  would increase to reach very large values that would then be corrected by monitoring.

Saturation problems can clearly appear: e.g. if the cars are too far, large accelerations, and so high velocities, can occur. In order to achieve passengers security and comfort, some constraints have to be satisfied. First, vehicles velocities have to be bounded:

$$0 \leq v_{i+1} \leq v_{max} \quad (9)$$

This ensures that vehicles never move back nor exceed a desired velocity. It can be done by using an adaptive gain in the longitudinal control law. Secondly, if vehicle  $i + 1$  is far behind vehicle  $i$ , or if vehicle  $i$  presents an odd behavior (e.g. if it stops abruptly), control law (8) may then lead to very large accelerations/decelerations, very unpleasant to passengers aboard. Therefore, the monitoring scheme shown on Fig. 13 has been introduced, with the aim to privilege passengers comfort, as far as their security can be guaranteed.

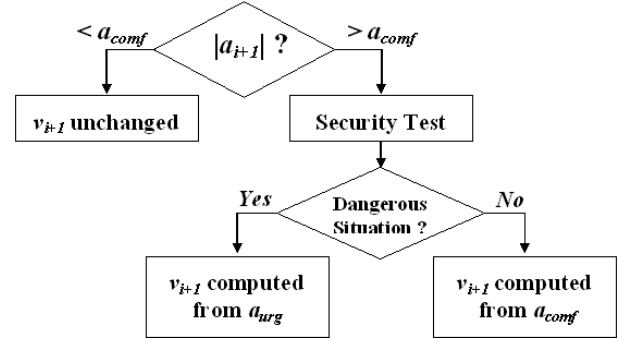


Fig. 13. Monitoring security and comfort

More precisely, the notation  $a_{comf}$  on Fig. 13 stands for the maximum acceleration/deceleration comfortable to a passenger aboard. Then, if the acceleration/deceleration of vehicle  $i + 1$ , denoted  $a_{i+1}$ , is superior to that value, a security test is performed:

- the case  $a_{i+1} > a_{comf} > 0$  occurs when vehicle  $i + 1$  is far behind vehicle  $i$ . In such a situation,  $a_{i+1}$  can be limited to  $a_{comf}$  without any collision risk.
- the case  $a_{i+1} < -a_{comf} < 0$  occurs if vehicle  $i$  stops abruptly. In such a situation, collision risks have to be investigated. To this aim, the distance covered by vehicle  $i + 1$ , if it was stopped with a deceleration  $-a_{comf}$ , is first computed, and its final inter-distance with vehicle  $i$  is derived (the worst case, i.e. vehicle  $i$  is stopped, is here assumed).

- if this inter-distance is superior to  $d_s$ , then  $a_{i+1}$  can safely be limited to  $-a_{comf}$ .
- in the other case, the deceleration (denoted  $-a_{urg}$ ) leading to a projected inter-distance equal to  $d_s$  is computed, and  $a_{i+1}$  is limited to that value. Passengers security is privileged with respect to their comfort.

When computing the final inter-distances with constant decelerations ( $-a_{urg}$  or  $-a_{comf}$ ), delays introduced by actuator features and transmission latencies are taken into account.

## IV. RESULTS

This section is divided into two parts: first, experimental results involving two vehicles validate control law (8) and

monitoring. Secondly, simulations with larger platoons compare capabilities of LCS and GCS.

#### A. Experimentation

Several experiments have been carried out at "Campus des Cézeaux", in Clermont-Ferrand area. These experiments involve only two vehicles, therefore  $\sigma_{i+1}$  has no influence as the immediate front car and the leader are the same. However, experiments with more vehicles are planned, since our lab will soon be equipped with additional vehicles. Only experimentations related to GPS base memory are reported here.

1) *Experimental Vehicle*: Experimental vehicles, named Cycab, are depicted on Fig. 1. Their small dimensions (length 1.90m, width 1.20m) are advantages for the urban traffic. These vehicles are entirely under control computer. The used kinematic configuration is the same as those of a car-like vehicle. Its maximum speed is  $v_{max} = 18km/h$ . In our experiments, a personal computer is added in each Cycab. This high-level computer collects information received from RTK GPS, mounted by serial link, and from front vehicles, via WiFi. The used RTK GPS receiver provides measurements at a 10HZ sampling frequency, with a 2cm accuracy. The steering values and the vehicle velocities computed by control laws are transmitted to the Cycab computer by an Ethernet network and reach the MPC555 micro-controllers by CAN. The used kinematic configuration is the same as the one of a car-like vehicle. Its maximum speed is 5m/s. The mounted RTK GPS receiver provides measurements at a 10Hz sampling frequency, with a 2cm accuracy. The communication between cars is ensured via WiFi.

2) *Experiment*: The gains of the lateral control law are tuned to impose that lateral deviation converges to 0 within 15m. Parameters of the longitudinal law are set to  $k = 0.6$ ,  $v_{max} = 4m/s$ ,  $a_{comf} = 1m/s^2$  (ensued from studies reported in [25]),  $d = 8m$  and  $d_s = 6.50m$ . In practical situation, we could imagine that the leader is pulling a trailer, and that collision occurs if the inter-distance is inferior to  $d_s$ .

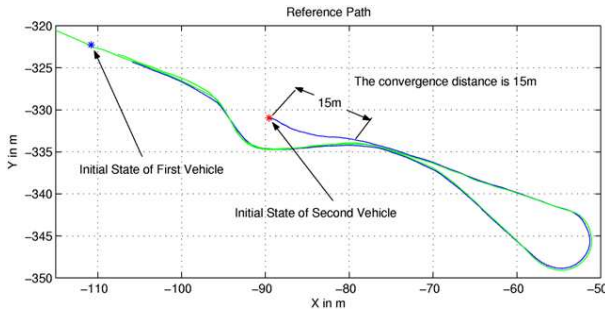


Fig. 14. Reference Trajectory : lateral control performances

Fig.14 illustrates the shape of the reference trajectory. For each vehicles, lateral deviation are less than 3cm in straight line and less than 10cm in bend.

The experiment reported on Fig 15 can be divided into three main parts. First, the hooking is tested: at initial time, the space between the cars is close to 20m. Thanks to the monitoring, the hooking appears smooth and comfortable (acceleration saturated at  $a_{comf}$  and  $v < v_{max}$ , see Fig. 16). In a second phase, the longitudinal standard law performances are scanned. Once the follower is hooked, the gap is equal to  $d$  with a satisfactory standard deviation of 4.7cm and a mean error inferior to 1cm (Fig. 17). Finally, the security of the law, in

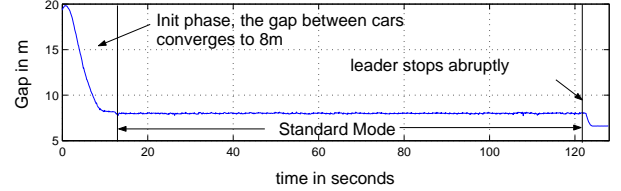


Fig. 15. Curvilinear distance between cars

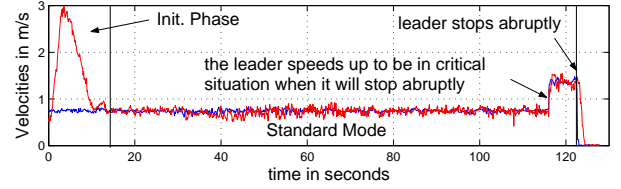


Fig. 16. Velocities measured by GPS

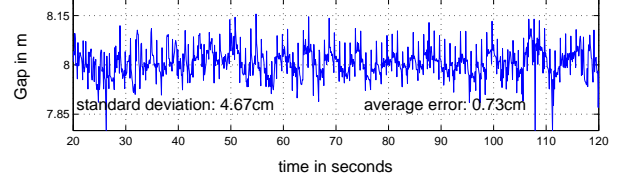


Fig. 17. Zoom on curvilinear distance in standard mode

critical situation is investigated. Preliminary, the leader reaches a higher velocity in order to position the platoon in a critical situation when it stops abruptly. As the security can not be achieved with a deceleration equal to  $-a_{comf}$ , an urgency deceleration equal to  $-1.2m/s^2$  is computed and applied, see Fig. 18 and Fig. 19. This experiment demonstrates satisfactory performances of the control law (8) and monitoring (comfort mode is tested at the beginning and security mode at the end).

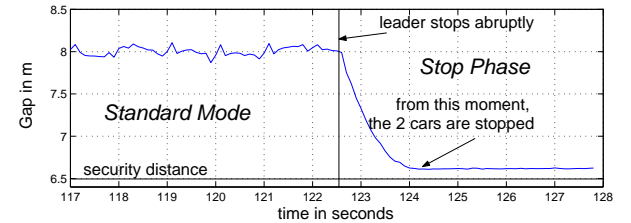


Fig. 18. Curvilinear Distance between cars in stop phase

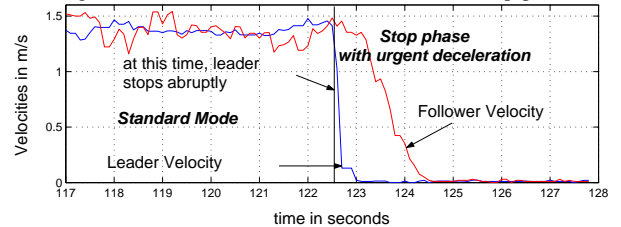


Fig. 19. Velocities evolution during stop phase

## B. Simulations

In this part, GCS is compared with a classical LCS. The common scenario is a path following to be achieved, by a 10 vehicles long platoon, at a constant velocity of  $2m/s$  (fixed by the leader). In order to simulate LCS, the parameter  $\sigma_{i+1}$  is simply set to 0 in control law (8). All parameters are identical in LCS and GCS simulations (they are the same as in the experiment). Finally GPS features are introduced via a white noise with a standard deviation of  $10cm$  added to position measurements. GPS sensors used in previous experiment have a  $2cm$  accuracy, but are quite expensive. When numerous vehicles have to be equipped, decimeter GPS appears more realistic. Moreover, less accurate sensors reveal more clearly the advantages of GCS over LCS.

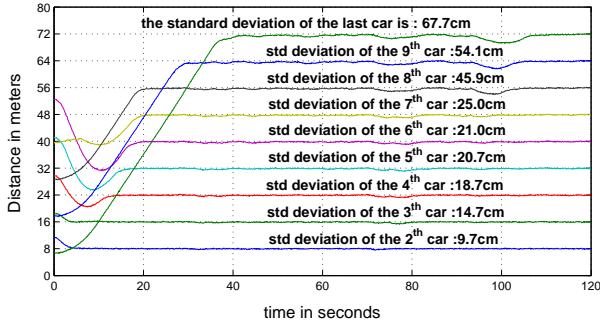


Fig. 20. Distance with the leader (LCS)

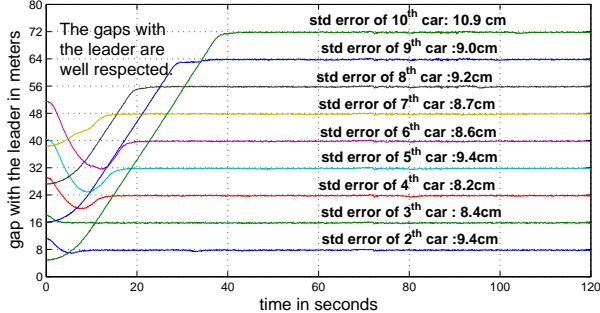


Fig. 21. Distance with the leader (GCS)

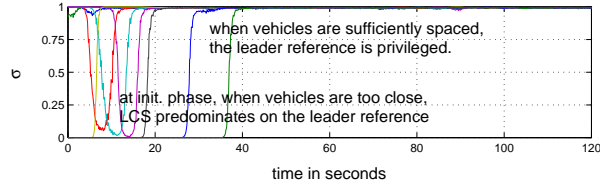


Fig. 22. Evolution of parameter  $\sigma_{i+1}$

The first simulation presents LCS. In order to highlight errors accumulation, the gap between each vehicle and a common reference point in the platoon, i.e. the platoon leader, is depicted on Fig. 20. The main drawbacks of LCS appear then clearly: the distance to the leader presents a standard deviation of  $9.7cm$  for the first follower, when it is  $67.7cm$  for the last one. The situation gets even worse in tight turns: when the last vehicle is in a bend, at  $t = 95s$  see Fig. 20, the maximum error recorded is  $2.80m$ .

In the second simulation, when GCS is used, these drawbacks disappear, see Fig. 21: each follower is subjected to

errors of the same order of magnitude. The standard longitudinal deviations of each vehicle are close to  $10cm$  ( $9.5cm$  for the first follower and  $10.9cm$  for the last one, i.e. the error is simply equal to the introduced GPS noise, see Fig. 23). Therefore, these simulations demonstrate that GCS surmounts the limitations of LCS. Moreover, when observing parameter  $\sigma_{i+1}$  in the Init. phase (Fig. 22), it can be seen that the platooning laws commute progressively from LCS (when inter-vehicles distance is small) to a control with respect to an absolute reference (when the gap is close to  $d$ ).

Vehicle	2	3	4	...	8	9	10
LCS	9.7	14.7	18.7	...	45.9	54.1	67.7
GCS	9.5	8.4	8.2	...	9.2	9.0	10.9

Fig. 23. Standard deviation (in cm) according the strategy

Platoon security is therefore ensured (by LCS) when cars are close to each other, and in standard mode, high regulation performances are obtained (by the absolute reference). The skill to adapt the longitudinal error at the met situation is clearly demonstrated.

## V. CONCLUSION

In this paper, we have presented some work done in the french national research context mainly in the ROBEA-CNRS BODEGA project, and in the PREDIT3 MOBIVIP project. The main goals of such projects are to demonstrate the ability of *Intelligent Transportation System* to supply autonomous services (*Car Sharing* in single or platoon mode) for the end user in city centers.

We have studied a complete system able to perform some autonomous following tasks in single and platoon mode using a navigation scheme which takes into account the imprecise part of the GIS map. Using a learning step to acquire a set of reference trajectories, we built an augmented GIS to order the trajectories using a topological description of the environment. Localization is performed in regard with the reference trajectories. We have designed nonlinear control laws whose main property is to decouple lateral and longitudinal behaviour. A monitoring module has been developed and takes in charge security, comfort, and system limitations aspects.

Validation have been realized both in real (up to 2 cars) and in simulation (up to 10 cars). In the real case, we have used RTK-GPS sensor in order to extract the local state of each vehicle involve in the platoon. From the perception point of view, as visibility of satellite becomes a difficult problem in city center, we have started to evaluate a novel solution using a simple monocular camera. The current results [18] show the validity of such approach (lateral error is less than  $10cm$  in straight line, and less than  $35cm$  in bend). Lateral control using this novel approach is ensured with a  $10cm$  accuracy.

The next research steps will concern control, multi-sensor perception, monitoring, and real validation with more cars.

In control, it remains two main critical points to study. The first one concerns the "point stabilization problem". As



vehicles are non holonomous robots, this point remains an open problem in control theory. The second one concerns the platoon modelling : it would be interesting to consider platoon as a multi-robot system under constraints.

We start to develop a multi-sensor approach using a low cost DGPS sensor, one monocular camera and some proprioceptive sensors. Data fusion techniques will be adapted to our particular application, knowing that we are not only interested to localize the current vehicle, but also to compute the localization of each cars involves in the platoon.

In the current version of our navigation system, we have not yet develop the obstacle avoidance module. It would be interesting to have one, and to extend the functionalities of the monitoring module in order to take into account an exhaustive set of states for the platoon.

Finally, we have already two cars equipped, and planed to buy three more. Real experiment (up to 5 or 6 cars) will be done in 2006 in order to validate our complete system.

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