# Distributed Optimization and Games

#### **Auctions**

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#### Outline

- □ Preliminaries
  - Auctions
  - Matching markets
- □ Possible approaches to ads pricing
- □ Google mechanism
- □ References
  - Easley, Kleinberg, "Networks, Crowds and Markets", ch.9,10,15

#### Google's GSP auction

- Generalized Second Price
- $\square$  Once all the bids are collected  $b_1 > b_2 > ... b_N$
- Company i pays b<sub>i+1</sub>
- □ In the case of a single good (position), GSP is equivalent to a 2<sup>nd</sup> price auction, and also to VCG
- But why Google wanted to implement something different???

### GSP properties

Truth-telling may not be an equilibrium

## GSP example

Ads positions

companies

1

 $r_1 = 10$ 

a

 $v_a = 7$ 

2

 $r_2=4$ 

(b)

 $v_b = 6$ 

3

 $r_3 = 0$ 

**c** 

 $v_c=1$ 

r<sub>i</sub>: click rate for an ad in position i (assumed to be independent from the ad and known a priori) v<sub>i</sub>: value that company i gives to a click

- □ If each player bids its true evaluation, a gets a payoff equal to 10
- □ If a bids 5, a gets a payoff equal to 24

### GSP properties

- Truth-telling may not be an equilibrium
- □ There is always at least 1 socially optimal NE

## GSP example

Ads positions

companies

1

$$r_1 = 10$$

a

$$v_a = 7$$

2

$$r_2=4$$

(b)

$$v_b = 6$$

 $r_3 = 0$ 

(c)

$$v_c=1$$

r<sub>i</sub>: click rate for an ad in position i (assumed to be independent from the ad and known a priori) v<sub>i</sub>: value that company i gives to a click

#### □ Multiple NE

- o a bids 5, b bids 4 and c bids 2
- o a bids 3, b bids 5 and c bids 1

### GSP properties

- Truth-telling may not be an equilibrium
- □ There is always at least 1 socially optimal NE
- □ Revenues can be higher or lower than VCG
  - Attention: the revenue equivalence principle does not hold for auctions with multiple goods!
  - Google was targeting higher revenues...
  - o ... not clear if they did the right choice.

### GSP example

Ads positions

companies

1

$$r_1 = 10$$

a

$$v_0 = 7$$

2

$$r_2=4$$

(b)

$$v_b = 6$$

3

$$r_3 = 0$$

(c)

$$v_c=1$$

#### □ Multiple NE

- o a bids 5, b bids 4, c bids 2  $\rightarrow$  google's revenue=48
- o a bids 3, b bids 5, c bids 1  $\rightarrow$  google's revenue=34
- □ With VCG, google's revenue=44

#### Other issues

- Click rates are unknown and depend on the ad!
  - Concrete risk: low-quality advertiser bidding high may reduce the search engine's revenue
  - Google's solution: introduce and ad-quality factor taking into account actual click rate, relevance of the page and its ranking
    - Google is very secretive about how to calculate it => the market is more opaque
- Complex queries, nobody paid for
  - Usually engines extrapolate from simpler bids