

# Maillage adaptatif pour des interfaces mobiles gaz-liquide-solide

### CFL Research Group (Computing and FLuids) MINES ParisTech, PSL Research University, CEMEF

mehdi.khalloufi@mines-paristech.fr

# Context: challenges in multiphase flows



### High fidelity multiphase framework: illustration Unsteady NS, Anisotropic mesh adaptation, regularisation, parallel computing....



### Anisotropic mesh adaptation

Y. Mesri Y., M. Khalloufi, E. Hachem, On optimal simplicial 3D meshes for minimizing the Hessian-based errors, App. Num. Math, 2016, 07

### We are concern to capture automatically: (i) boundary layers (ii) inner layers















### Anisotropic mesh adaptation

### We are concern to capture automatically: (i) boundary layers (ii) inner layers

# $= \begin{pmatrix} \frac{1}{0.01^2} \\ \frac{1}{1^2} \end{pmatrix} = \operatorname{improved}_{\text{remesher}} =$ Metric (directions, size)

### (iii) flow detachments



 $\rightarrow$  We refer to the use of an edge-based metric:

T. Coupez and E. Hachem, Solution of High-Reynolds Incompressible Flow with Stabilized Finite Element and Adaptive Anisotropic Meshing, Computer Methods in Applied Mechanics and Engineering, Vol. 267, pp. 65-85, 2013

$$\widetilde{\mathbb{M}^{i}} = \frac{\left|\Gamma(i)\right|}{d} \left(\widetilde{\mathbb{X}^{i}}\right)^{-1} \quad \text{With} \quad \widetilde{\mathbf{X}^{ij}} = s_{ij}\mathbf{X}^{ij} \quad \text{and} \quad s_{ij} = \left(\frac{e}{e(N)}\right)^{-\frac{1}{2}} = \left(\frac{\sum\limits_{i} n^{i}(1)}{N}\right)^{d} e_{ij}^{-1/2}$$

 $\rightarrow$  Extended to account accurately for sharp layers using the local wall shear stress:

$$au_{\mathrm{w}}\equiv au(y=0)=\murac{\partial u}{\partial y}\Big|_{y=0}$$

L. Billon, Y. Mesri, E. Hachem, Anisotropic boundary layer mesh generation for immersed complex geometries, accepted in Engineering with Computers, 2016 (online)

### Illustration 2: Dam breaking (water column with surface tension)



### Illustration 3: Filling and dome formation



### Fluid-Solid flows:

Moving solid Implicit representation by a levelset function Penalization by imposing zero rate of deformation Dynamic anisotropic meshing







Flapping wing
 Implicit representation by a levelset function
 Penalization by imposing zero rate of deformation
 Dynamic anisotropic meshing



# Quenching

Cooling of a hot part from austenization temperature to room temperature





# Industrial context

THOST Thermal Optimization System:

- Several companies
- Different parts
  - Geometries
  - Size (cm to m)
- Different quenchants (water, oil, air, polymer, gas,...)





Hollow cylinder - Areva



Seat flange - Faurecia

Accurate and robust simulation of the quenching processes

# Heat transfer



- Multiphase: solid/liquid/gas
- Agitation



### Quenching bath

Paradigm:

- Immersed volume methods
- Strong coupling solid/fluid/gas
- Natural heat transfer

# Heat transfer



# Outline: Looking for a robust multiphase framework...



### ...dedicated to industrial quenching and heat treatment

# Looking for a robust multiphase framework



# 1-Level set



Two possibilities:

Solving (1) and (2) separately

Fedkiw 2009, Osher 2000, Sussman 2005

Embedding (2) in (1) : auto reinitialisation Ville et.al. 2011, Bonito et al 2015

### A new Level Set method:

Conservative Level set method:

(1) Filtering

$$\phi(\alpha) = \frac{1}{2} \left( 1 + \tanh\left(\frac{\alpha}{2\varepsilon}\right) \right)$$



(2) Convection

$$\frac{\partial \phi}{\partial t} + u \cdot \nabla \phi = 0$$

2

Walker, Müller 2014

(3) Reinitialization

$$\frac{\partial \phi}{\partial \tau} + \nabla \cdot \left( \phi (1 - \phi) \mathbf{n} - \varepsilon ((\nabla \phi \cdot \mathbf{n}) \mathbf{n}) \right) = 0$$

E. Olsson, G. Kreiss, A conservative level set method for two phase flow, *Journal of Computational Physics*, Volume 210, Issue 1, 2005, Pages 225-246



# 2- Surface tension

### Surface tension

 $f_{\rm ST} = -\gamma \kappa \delta(\Gamma) \mathbf{n}$  $\mathbf{n} = \nabla \alpha / |\nabla \alpha| \qquad \kappa = -\nabla \cdot \mathbf{n}$ 

 $\gamma$  is the surface tension coefficient

Usually implemented as a source term in NS equations

$$\rho(\partial_t u + u \cdot \nabla u) - \nabla \cdot (2\mu\varepsilon(u)) + \nabla p = f + f_{ST}$$
  
$$\nabla \cdot u = 0$$

Numerical analysis shows that: time-step restriction

$$\Delta t < (\Delta x)^{\frac{3}{2}} \sqrt{\frac{\bar{\rho}}{2\pi\gamma}}$$

In 3D coupled problems, surface tension is the major bottleneck.



http://butane.chem.uiuc.edu/

### 2D and 3D validations



- Liquid Density: 10<sup>4</sup> kg/m<sup>3</sup> Viscosity: 1 kg/(m.s)
- Vapor
   Density: 10<sup>3</sup>kg/m<sup>3</sup>
   Viscosity: 1 kg/(m.s)

Surface tension 0,5 kg/s<sup>2</sup> Gravity g=-8x10<sup>-4</sup>m/s<sup>2</sup>

Mesh size h=1/80

# Surface tension

explicit



dt=0.1s

dt=1s

dt=4s

# Surface tension



### Case 1: High surface tension

Case 2: Low surface tension

M. Khalloufi, Y. Mesri, R. Valette, E. Hachem, High fidelity anisotropic adaptive variational multiscale method for multiphase flows with surface tension, **Computer Methods in Applied Mechanics and Engineering**, Vol. 307, pp.44-67, **2016** 

### Validation: Rising bubble with mesh adaptation





# Validation: 3D Rising bubble with mesh adaptation



Without surface tension

M. Khalloufi, Y. Mesri, R. Valette, E. Hachem, High fidelity anisotropic adaptive variational multiscale method for multiphase flows with surface tension, **Computer Methods in Applied Mechanics and Engineering**, Vol. 307, pp.44-67, **2016** 

### 3-Unified Compressible/Incompressible solver

Navier-Stokes equations

$$\rho(\partial_t u + u \cdot \nabla u) - \nabla \cdot \sigma = f \quad \text{in } \Omega \times [0, T]$$
$$\nabla \cdot u = 0 \quad \text{in } \Omega \times [0, T]$$

$$\frac{d\rho}{dt} = \left(\frac{\partial\rho}{\partial T}\right)_p \frac{dT}{dt} + \left(\frac{\partial\rho}{\partial p}\right)_T \frac{dp}{dt} \qquad \Longrightarrow \qquad \chi_p = \frac{1}{\rho} \left(\frac{\partial\rho}{\partial p}\right)_T \quad \text{and} \quad \chi_T = \frac{1}{\rho} \left(\frac{\partial\rho}{\partial T}\right)_p$$

 $\chi_T$  is the volume expansivity

 $\chi_P$  is the isothermal compressibility coefficient

**Conservation** equation

$$\nabla \cdot u + \chi_P \frac{\partial p}{\partial t} + \chi_P u \cdot \nabla p = \chi_T \frac{dT}{dt}$$

M. Billaud, G. Gallice, B. Nkonga, A simple stabilized finite element method for solving two phase compressible– incompressible interface flows, *Computer Methods in Applied Mechanics and Engineering*, Volume 200, Issues 9–12, 2011, pp.1272-1290

### 3-Unified Compressible/Incompressible solver

$$\rho \frac{\partial u}{\partial t} + \rho u \cdot \nabla u - \nabla \cdot (2\mu\varepsilon(u)) + \nabla p = f_v$$
$$\nabla \cdot u + \chi_P \frac{\partial p}{\partial t} + \chi_P u \cdot \nabla p = f_p$$

By splitting the velocity and the pressure into a coarse scale and a fine scale: Variaztional Multiscale Stabilized Finite Element Method

$$\begin{pmatrix} \underline{\rho\partial(u_{h}+\tilde{u})} \\ \partial t \end{pmatrix} + \left(\rho(u_{h}+\tilde{u})\cdot\nabla(u_{h}+\tilde{u}),v_{h}\right) - \left(p_{h}+\tilde{p},\nabla\cdot v_{h}\right) + \left(2\eta\varepsilon\left(u_{h}\right):\varepsilon\left(v_{h}\right)\right) = \left(f_{v},v_{h}\right) \quad \forall v_{h}\in\mathcal{V}_{h}$$

$$\left(\nabla\cdot(u_{h}+\tilde{u}),q_{h}\right) + \chi_{P}\left(\frac{\partial(p_{h}+\tilde{p})}{\partial t},q_{h}\right) + \chi_{P}\left((u_{h}+\tilde{u})\cdot\nabla(p_{h}+\tilde{p}),q_{h}\right) = \left(f_{p},q_{h}\right) \quad \forall q_{h}\in\mathcal{Q}_{h}$$

# 3-Unified Compressible/Incompressible solver

Compression of a bubble – Challenging case





E. Hachem, M. Khalloufi, J. Bruchon, R. Valette, Y. Mesri, Unified adaptive Variational MultiScale method for two phase compressible-incompressible flows, **Computer Methods in Applied Mechanics and Engineering**, Vol. 308, pp. 238-255, **2016** 





	<b>ρ</b> [kg/m <sup>3</sup> ]	$\mu$ [kg/(s·m)]	$c_p  [kJ/(kg \cdot K)]$	$k \left[ W/(m \cdot K) \right]$	L <sub>vap</sub> [kJ/kg]
Vapor $(100^{\circ}C)$	0.6	$1.2 \times 10^{-5}$	2.027	0.0248	
Water $(100^{\circ}C)$	960	$2.83\times10^{-4}$	4.215	0.682	2264.76

# Stefan problem



# Stefan problem





# Stefan problem

# For a given initial thickness of the film



$$\rho_l c_l \left( \frac{\partial T_l}{\partial t} + u \cdot \nabla T_l \right) - \nabla \cdot (k_l \nabla T_l) = 0 \quad \text{in } \Omega^l$$

$$\rho_g c_g \left( \frac{\partial T_g}{\partial t} + u \cdot \nabla T_g \right) - \nabla \cdot (k_g \nabla T_g) = 0 \quad \text{in } \Omega^g$$

### Mass rate transfer at the interface

$$\dot{m} = -\frac{q_l \cdot n - q_g \cdot n}{L} \qquad \qquad q = -k\nabla T$$

### **Navier-Stokes** equations

$$\rho\left(\frac{\partial u}{\partial t} + u \cdot \nabla u\right) - \nabla \cdot \mu(\nabla u + \nabla^T u) + \nabla p = f_{\rm ST} + \rho g$$

$$\nabla \cdot u = \dot{m} \left( \frac{1}{\rho_g} - \frac{1}{\rho_l} \right)$$



V. Mihalef et al. Physics based boiling simulation. *Proceedings of the 2006 ACM SIGGRAPH/Eurographics Symposium on Computer Animation*, SCA '06, pages 317-324

T. Kim et al. A simple boiling module. *Proceedings of the 2007 ACM SIGGRAPH/Eurographics Symposium on Computer Animation*, SCA '07, pages 27-34

V. Daru et al. Modélisation et simulation numérique du changement de phase liquide-vapeur en cavité. *Comptes Rendus Mécanique*, 334(1):25 - 33, 2006

Y. Sato et al. A sharp-interface phase change model for a mass-conservative interface tracking method. *Journal of Computational Physics*, 249(0):127 -- 161, 2013





Results in 3D, dt=0.01s, domain: 1m3 Cylinder: length 0,50m, diameter 0,10m



Perspective view

Front view

Results in 3D , dt=0.01s, domain: 1m3 Cylinder: length 0,50m , diameter 0,10m Position of the cylinder : z=0,50m



Perspective view

Front view

Results in 3D , dt=0.01s, domain: 1m3 Cylinder: length 0,50m , diameter 0,10m Position of the cylinder : z=0,25m



Perspective view

Front view

Results in 3D , dt=0.01s, domain: 1m3 Cylinder: length 0,50m , diameter 0,10m

### Industeel



T(metal, t=0s) = 880°C T(water, t=0s) = 25°C



### Density

### Temperature (log scale)



Perspective view

Front view



Evolution of the temperature at the core of the sample - With phase change model



Without phase change model

> With phase change model

O Problems with large boundary displacements

### **Thomas Toulorge**

### **Traditional approaches**

- Problems with limited boundary motion/deformation (e.g. aeroelasticity)
   → « Front tracking »: moving mesh + ALE
- Problems with large boundary motion/deformation (e.g. multi-phase flows)
   → « Front capturing »: level-set, phase-field, VoF…

### Many problems fall « in-between »

- High-Reynolds fluid dynamics applications with large boundary motion
- Resolving boundary layers: body-fitted meshes
- Objects with geometrical singularities subject to rigid-body motion: front capturing inappropriate
- Large boundary motion: pure moving meshes based on mechanical analogies often fail



O Ingredients for a robust « moving mesh » method

### **Optimization-based moving mesh techniques**

- Node movement driven by opt. procedure
- Mesh validity: objective function of element Jacobian
- Mesh quality: objective function of aspect ratio
- Use barrier functions to impose minimum mesh validity/quality



### **Topological modifications**

- Triggered if moving mesh does not yield the required validity/quality
- General operator in cavity around mesh edge<sup>1</sup> without node addition or deletion

O General « moving mesh » algorithm



### O First results



Test cases: F. Alauzet, A changing-topology moving mesh technique for large displacements, Engineering with Computers 30(2): 170-200.

**Quentin Schmid** 



### View factor





Construction of a "layer" of elements crossed by the zero isovalue of level set







Industrial part

Sectional view

### Validation



### Validation

















# **Conclusions & Perspectives**

□ 3D multiphase framework for quenching and boiling

□ Validation in 2D & 3D for several benchmarks

Industrial validations with experimental measurements

Influence of the geometries on the dynamic the vapor film

Coupling solid-fluid: computation of phase transformation

□ Towards moving and deformable geometries

Thank you for your attention