

### Verification Introduction to WComp Validation

#### **WComp Verification**



- WComp may be used to design critical applications
- Ensure a safe usage of WComp wrt component behavior
- Apply techniques used to develop critical software

#### Outline



- 1. Critical system validation
- 2. Model-checking Techniques
  - 1. Model specification as synchronous models
    - Introduction to synchronous modeling
    - Introduction to Lustre synchronous language
  - 2. Express and prove properties
- 3. Application to WComp

#### **Critical Software**



A critical software is a software whose failing has serious consequences:

- Nuclear technology
- Transportation
  - •Automotive
  - •Train

- - -

•Aircraft construction

# Exemple: The Patriot Missile Failure



 On February 25, 1991, during the Golf War, an american patriot missile battery in Dharam, Saudi Arabia, failed to track and intercept an incoming Iracq scud missile. The scud struck american army baracks, killing 28 soldiers and injuring around 100 others people.

# Exemple: The Patriot Missile Failure



 A report on the general accounting office, entitled Patriot Missile Defense: software problem led to system failure at Dharam reported on the cause of the failure. It turns out that the cause was an inaccurate calculation of the time since boot due to computer arithmetic errors.

### **Software Classification**





Depending of the level of risk of the system, different kinds of verification are required Example of the aeronautics norm DO178B:

Catastrophic (human life loss)

A

B

С

D

Ε

- Dangerous (serious injuries, loss of goods)
- Major (failure or loss of the system)
- Minor (without consequence on the system)
- Without effect

#### Software Classification



Minor		acceptable situation		e situation
Major				
Dangerous	Unacceptable situation			
catastrophic	10 <sup>-3</sup> / hour	10 <sup>-6 /</sup> hour	10 <sup>-9</sup> /hour	10 <sup>-12</sup> /hour
probabilities	probable	rare	very rare	very improbable

#### **Critical Software**



In addition, other consequences are relevant to determine the critical aspect of a software:

#### **Financial aspect**

Loosing of equipment, bug correction

Equipment callback (automotive)

#### Bad advertising

Intel famous bug

### How Develop critical software ?



Classical Development U Cycle



# How Develop Critical Software ?



- Cost of critical software development:
  - Specification : 10%
  - Design: 10%
  - Development: 25%
  - Integration tests: 5%
  - Validation: 50%
- Fact:
  - Earlier an error is detected, less expensive its correction is.

### How Develop Critical Software ?



- Goals of critical software specification:
  - Define application needs
    - $\Rightarrow$  specific domain engineers
  - Allowing application development
    - Coherency
    - Completeness
  - Allowing application functional validation
    - Express properties to be validated

#### $\Rightarrow$ Formal models usage







### Verification Critical Software Validation

# **Critical Software Validation**



- What is a correct software?
  - No execution errors, time constraints respected, compliance of results.
- Solutions:
  - At model level :
    - Simulation
    - Formal proofs
  - At implementation level:
    - Test
    - Abstract interpretation



- Testing
  - Run the program on set of inputs and check the results
- Static Analysis
  - Examine the source code to increase confidence that it works as intended
- Formal Verification
  - Argue formally that the application always works as intended

#### **Formal verification**



- What about functional validation ?
  - Does the program compute the expected outputs?
  - Respect of time constraints (temporal properties)
  - Intuitive partition of temporal properties:
    - Safety properties: something bad never happens
    - Liveness properties: something good eventually happens

# Safety and Liveness Properties



- Example: the beacon counter in a train:
  - Count the difference between beacons and seconds
  - Decide when the train is ontime, late, early

# Safety and Liveness Properties

- Some properties:
  - 1. It is impossible to be late and early;
  - 2. It is impossible to directly pass from late to early;

**Ubiguitous Network** 

Ultra-tiny computer are embedded into

- 3. It is impossible to remain late only one instant;
- 4. If the train stops, it will eventually get late
- Properties 1, 2, 3 : safety
- Property 4 : liveness

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- 4. If the train stops, it will eventually get late
- Properties 1, 2, 3 : safety
- Property 4 : liveness (refer to unbound future)

Safety and Liveness Properties Checking



- Use of model checking techniques
- Model checking goal: prove safety and liveness properties of a system in analyzing a model of the system.
- Model checking techniques require:
  - model of the system
  - express properties
  - algorithm to check properties on the model (⇒ decidability)

# Model Checking Techniques



- Model = automata which is the set of program behaviors
- Properties expression = temporal logic:
  - LTL : liveness properties
  - CTL: safety properties
- Algorithm =
  - LTL : algorithm exponential wrt the formula size and linear wrt automata size.
  - CTL: algorithm linear wrt formula size and wrt automata size



### Model Checking Model Specification

# **Model Checking Technique**



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#### **Component Models**



- WComp Components represent software specification
- To achieve component behavior verification we need to build its model well suited to software validation
- Component behavior specification with a Synchronous language
- Specification = model



#### **Determinism & Reactivity**

- Synchronous languages are deterministic and reactive
- Determinism:

The same input sequence always yields

The same output sequence

• Reactivity:

The program must react<sup>(1)</sup> to any stimulus Implies absence of deadlock

(1) Does not necessary generate outputs, the reaction may change internal state only.

### Synchronous Hypothesis



- Actually, a synchronous model works on a logical time.
- The time is
  - Discrete

Use N as time base

- Total ordering of instants.
- A reaction executes in one instant.
- Actions that compose the reaction may be partially ordered.

### Synchronous Hypothesis



- Communications between actors are also supposed to be instantaneous.
- All parts of a synchronous model receive exactly the same information (instantaneous broadcast).
- Outcome: Outputs are simultaneous with Inputs (they are said to be synchronous)
- Thanks to these strong hypotheses, program execution is fully deterministic.

#### Reactive ?



- Different ways to "react" to the environment:
  - Event driven system:
    - Receive events
    - Answer by sending events
  - Data flow system:
    - Receive data continuously
    - Answer by treating data continuously also

Some systems have components of both kinds

# Event Driven Reactive System



#### Langing gear management



### Data Flow Reactive System (Example)









LUSTRE is a data flow synchronous language:

- It is a very simple language (4 primitive operators to express reactions)
- Relies on models familiar to engineers
  - Equation systems
  - Data flow network
- Lends itself to formal verification (it is a kind of logical language)



- Very simple (mathematical) semantics
- LUSTRE programs can be interpreted as networks of operators.
- Data « flow » to operators where they are consumed. Then, the operators generate new data. (Data Flow description).

#### **Operator Networks**



- LUSTRE programs can be interpreted as networks of operators.
- Data « flow » to operators where they are consumed. Then, the operators generate new data. (Data Flow description).



#### Flows, Clocks



- A flow is a pair made of
  - A possibly infinite sequence of values of a given type
  - -A clock representing a sequence of instants

**X:T** 
$$(x_1, x_2, ..., x_n, ...)$$


#### Language (1)

```
Variable : (= flow) :
```

- typed

If not an input variable, defined by 1 and only 1 equation

Equation :  $\mathbf{x} = \mathbf{E}$  means  $\forall \mathbf{k}, \mathbf{x}_k = \mathbf{e}_k$ 

Assertion : Boolean expression that should be always true at each instant of its clock.





Substitution principle: if **x** = **E** then **E** can be substituted for **x** anywhere in the program and conversely

Definition principle:

A variable is fully defined by its declaration and the equation in which it appears as a left-hand side term



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#### « Combinational » Lustre



Data operators

Arithmetical: +, -, \*, /, div, mod Logical: and, or, not, xor, => Conditional: if ... then ... else ... Casts: int, real

« Point-wise » operators

$$X \text{ op } Y \Leftrightarrow \forall k, (X \text{ op } Y)_k = X_k \text{ op } Y_k$$



#### « Combinational » Example



if operator
 node Max (a,b : real) returns (m: real)
 let
 m = if (a >= b) then a else b.

$$m = ir (a >= b) then a else b tel$$

### functional «if then else »; it is not a statement

#### « Combinational » Example



if operator
 node Max (a,b : real) returns (m: real)
 let

m = if (a >= b) then a else b; tel



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#### Memorizing



Take the past into account! pre (previous):

$$X = (x_1, x_2, \dots, x_n, \dots) : pre(X) = (nil, x_1, \dots, x_{n-1}, \dots)$$

Undefined value denoting uninitialized memory: nil

-> (initialize): sometimes call "followed by"  

$$X = (x_1, x_2, \dots, x_n, \dots)$$
,  $Y = (y_1, y_2, \dots, y_n, \dots)$ :  
 $(X -> Y) = (x_1, y_2, \dots, y_n, \dots)$ 

#### « Sequential » Examples





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#### Sequential » Examples



node MinMax (X:int) returns (min,max:int);
let

min = X -> if (X max = X -> if (X > pre max) then X else pre max; tel

#### « Review » Example



node CT (init:int) returns (c:int); let c = init -> pre c + 2; tel

#### node DoubleCall (even:bool) returns (n:int); let

## n = if even then CT(0) else CT(1);

tel

#### Doublecall(ff ff tt tt ff ff tt tt ff) = ?

#### **Recursive definitions**



Temporal recursion

Usual. Use **pre** and -> e.g.: nat = 1 -> **pre** nat + 1

Instantaneous recursion

$$e.g.: X = 1.0 / (2.0 - X)$$

Forbidden in Lustre, even if a solution exists! Be carefull with cross-recursion.



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#### **Bistable**



- Node Switch (on,off:bool) returns (s:bool); such that:
  - S raises (false to true) if on, and falls (true to false) if off
  - must work even off and on are the same

#### node Switch (on,off:bool) returns (s:bool) let $s = if (false \rightarrow pre s)$ then not off else on; tel

# Ubiquitous Network

- A node Count (reset, x: bool) returns (c:int) such that:
  - c is reset to 0 if reset, otherwise it is incremented if x

node Count (reset, x: bool) returns (c:int) let

tel

Count

#### Osc and Osc2



```
node osc (reset: bool) returns (b:int)
let
```

```
b = true -> not pre(b);
tel
```

```
node osc2 (reset: bool) returns (b:int)
let
```

#### A Stopwatch



- 1 integer output : time
- 3 input buttons: on\_off, reset, freeze
  - on\_off starts and stops the watch
  - reset resets the stopwatch (if not running)
  - freeze freezes the displayed time (if running)
- Local variables
  - running, freezed : bool (Switch instances)
  - cpt : int (Count instance)

#### A stopwatch



node Stopwatch (on\_off, reset, freeze: bool) returns (time:int)

var running, freezed: bool; cpt:int

#### let





#### **Ubiguitous Network** Modulo Counter with Clock Ultra-tiny computer are embedded into a node MCounterClock (incr:bool; modulo : int) returns (cpt:int; modulo clock: bool); var count : int; let $count = 0 \rightarrow if incr pre(cpt) + 1$ else pre (cpt); cpt = count mod modulo;modulo clock = count <> cpt; tel

#### Timer



(second, minute\_clock) = MCounterClock(true, 60);
(minute, hour\_clock) =

MCounterClock(minute\_clock,60);
(hour, dummy\_clock) =

MCounterClock(hour\_clock, 24);

#### tel

#### **Numerical Examples**



- Integrator node:
  - -f : real function and Y its integrated value using the trapezoid method:
  - F, STEP : 2 real such that:

$$F_n = f(x_n)$$
 and  $x_{n+1} = x_n + STEP_{n+1}$   
 $Y_{n+1} = Y_n + (F_n + F_{n+1}) * STEP_{n+1}/2$ 

#### **Numerical Examples**



#### node integrator (F, STEP, init : real) returns (Y : real);

#### let

# Y = init -> pre(Y) + ((F + pre(F))\*STEP)/2.0tel

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#### **Lustre Program Compilation**



- Static verifications are performed:
  - local and output variables have one equation definition;
  - non recursive node call;
  - absence of uninitialized expression;
  - no cyclic definition (each cyclic definition ⇒ pre operator usage);



#### Lustre Program Compilation



- automaton like code
  - choose state variables among:
    - boolean expressions resulting from pre operator;
    - variables (like \_init) associated with some clock whose value is true at first instant

#### **Lustre Program Compilation**



#### For WD, we consider 2 state variables: \_init (true, false, false, ....) and pre\_is\_set

3 states: **S0**: \_init = true and pre\_is\_set = nil **S1**: \_init = false and pre\_is\_set = false **S2**: \_init = false and pre\_is\_set = true

#### Lustre Program Compilation





#### Lustre Program Compilation





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#### Lustre Program **Ubiguitous Network** Compilation Ultra-tiny computer are embedded into 4 S0: alarm := false; initial alarm = is\_set and deadline; is\_set = false -> if set then true else if reset then false else pre(is\_set); S2: if set then S1: if set then alarm := deadline; alarm:= deadline; set go to S2; go to S2; else else if reset then alarm := false; alarm := false; go to S1; go to S1; reset else alarm := deadline; qo to S2; −set ¬reset

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#### Lustre Program = Model





reset

¬ reset



#### **Model Checking Technique**

#### **Model Checking Technique**



- Model = automata which is the set of program behaviors
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#### **Properties Checking**



- Liveness Property  $\Phi$  :
  - $\Phi \Rightarrow$  automata B( $\Phi$ )
  - $L(B(\Phi)) = \emptyset$  décidable
  - $\Phi \mid = \mathcal{M} : \mathbb{L}(\mathcal{M} \otimes B(^{\sim}\Phi)) = \emptyset$
#### **Safety Properties**



- CTL formula characterization:
  - Atomic formulas
  - Usual logic operators: not, and, or ( $\Rightarrow$ )
  - Specific temporal operators:
    - EX  $\varnothing$ , EF  $\varnothing$ , EG  $\varnothing$
    - AX  $\varnothing$ , AF  $\varnothing$ , AG  $\varnothing$
    - $EU(\emptyset_1, \emptyset_2), AU(\emptyset_1, \emptyset_2)$

## **Safety Properties Verification**

- Ubiquitous Network
- We call Sat( $\emptyset$ ) the set of states where  $\emptyset$  is true.
- $\mathcal{M} \models \emptyset$  iff  $s_{init} \in Sat(\emptyset)$ .
- Algorithm:
  - Sat(Φ) = { s | Φ |= s}
  - Sat(not  $\Phi$ ) = S\Sat( $\Phi$ )
  - Sat( $\Phi$ 1 or  $\Phi$ 2) = Sat( $\Phi$ 1) U Sat( $\Phi$ 2)
  - Sat (EX  $\Phi$ ) = {s |  $\exists t \in Sat(\Phi)$ , s  $\rightarrow$  t} (Pre Sat( $\Phi$ ))
  - Sat (EG  $\Phi$ ) = gfp ( $\Gamma(x)$  = Sat( $\Phi$ )  $\cap$  Pre(x))
  - Sat  $(E(\Phi 1 \cup \Phi 2)) = Ifp (\Gamma(x) = Sat(\Phi 2) \cup (Sat(\Phi 1) \cap Pre(x)))$





# Model Checking with Observers



- Express safety properties as observers.
- An observer is a program which observes the program and outputs ok when the property holds and failure when its fails





Ubiquitous Network

**Observers in Scade** 

P: aircraft autopilot and security system



#### **Edge Satefy Property**



node Edge (b: bool) returns (f : bool); let

```
f = b and not pre (b);
```

```
tel
```

node Edge\_verif (b: bool) returns (prop: bool);
var res : bool;

let

```
res = Edge(b);
```

```
prop = true -> res and not pre(res);
```

tel

### **Train Safety Properties**



- Example: the beacon counter in a train:
  - Count the difference between beacons and seconds

- Decide when the train is ontime, late, early

```
node train (sec, bea : bool) returns (ontime, early, late: bool)
let
    diff = (0 ->pre diff) + (if bea then 1 else 0) + (if sec then -1 else 0);
    early = (true -> pre ontime) and (diff > 3) or
        (false -> pre early) and (diff > 1);
late = (true -> pre ontime) and (diff < -3) or
        (false -> pre late) and (diff < -1);
ontime = not (early or late);
tel</pre>
```

### **Train Safety Properties**



- It is impossible to be late and early;
  - ok = not (late and early)
- It is impossible to directly pass from late to early;
  - ok = true -> (not early and pre late);
- It is impossible to remain late only one instant;
  - Plate = false -> pre late;
     PPlate = false -> pre Plate;
     ok = not (not late and Plate and not PPlate);

#### **Properties Validation**



- Taking into account the environment
  - without any assumption on the environment, proving properties is difficult
  - but the environment is indeterminist
    - Human presence no predictable
    - Fault occurrence
    - ..
  - Solution: use assertion to make hypothesis on the environment and make it determinist





- Express safety properties as observers.
- Express constraints about the environment as assertions.





remains true (or failure false).



#### **Train Assumptions**



- property = assumption + observer: " if the train keeps the right speed, it remains on time"
- observer = ok = ontime
- assumption:

- naïve: assume = (bea = sec);

#### **Train Assumptions**



- property = assumption + observer: " if the train keeps the right speed, it remains on time"
- observer = ok = ontime
- assumption:
  - more precise : bea and sec alternate:
    - SF = Switch (sec and not bea, bea and not sec);
    - BF = Switch (bea and not sec, sec and not bea); assume = (SF => not sec) and (BF => not bea);



#### WComp Component Validation

#### **Component Validation**





#### WComp critical component usage validation





# Example: monitoring eldery people at home



Ubiguitous Network







#### Example: camera and fridge



```
node camera (in_kitchen, close_fridge: bool)
    returns (warning1: bool);
let
    warning1= in_kitchen and close_fridge
tel
    node fridge (fridge_opened, one_minute: bool)
    returns (warning2, weak_alarm2: bool);
let
```

```
warning2= fridge_opened and not one_minute;
weak_alarm2= fridge_opened and one_minute;
tel
```

#### Example: WComp Assembly





Need for synchronous monitor composition:

- 1. Parallel composition is obvious in Lustre (||)
- 2. Combination function (ζ) to specify how outputs are combined.

# Example: Monitor Composition

camera || fridge || posture Ubiguitous Network

Ultra-tiny computer are embedded into

warning = warning1 and warning2 and warning3 and not weak\_alarm2 and not weak\_alarm3; weak\_alarm = weak\_alarm2 xor weak\_alarm3; strong\_alarm = weak\_alarm2 and weak\_alarm3;

tel

# Example: Composition Verification



```
node verif (close_fridge, fridge_opened, one_minute,
          standing, sitting, lying, in kitchen : bool)
     returns (prop: bool)
 var warning, weak_alarm, strong_alarm : bool;
let
                                       Assertion on environment
 (warning, weak_alarm, strong_alarm) =
     comp(close fridge, fridge opened, one minute, standing,
  sitting, lying, in kitchen);
 assert (not ((standing and lying) or (standing and sitting) or
  (lying and sitting))
 prop = if (fridge_opened and one_minute and lying)
        then strong_alarm else true;
tel
                 Property verified with Lesar (prop always true)
```



