

Bigraphs and Bigraphical Reactive Systems

Michael Westergaard

`mw@daimi.au.dk`

Department of Computer Science
University of Aarhus

Grand Challenges for Computing Research

1. In Vivo ↔ In Silico
2. Science for Global Ubiquitous Computing
3. Memories for Life
4. Scalable Ubiquitous Computing Systems
5. The Architecture of Brain and Mind
6. Dependable Systems Evolution
7. Journeys in Non-Classical Computation

Source: http://www.nesc.ac.uk/esi/events/Grand_Challenges/

Scenario (1/2)

- Room
 - ◆ Person
 - Wireless head-set
 - Mobile phone
 - ◆ Laptop computer
 - ◆ Telephone



Scenario (2/2)



- The laptop computer and the mobile phone is connected to the internet
- The wireless head-set is connected to the telephone
- The telephone and the mobile phone is connected to the phone network

Calculi for Mobile Systems

- Ambient-calculus: Focus on location (with local linkage only)
- π -calculus: Focus on linkage
- (Object-)Petri-nets: Focus on location and linkage to near environment

Calculi for Mobile Systems

- Ambient-calculus: Focus on location (with local linkage only)
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... using either of these, it is not easy to describe our scenario...

Remote Linking

- Until now, mobile calculi regard linking as local
- This is not always desirable
- E.g. telephone conversation, internet connections
- We will try to address this

Contents

- Bigraphs
- Bigraphical Reactive Systems (BRS)
- Expressiveness
- Further topics

Bigraphs – Place Graphs (1/2)

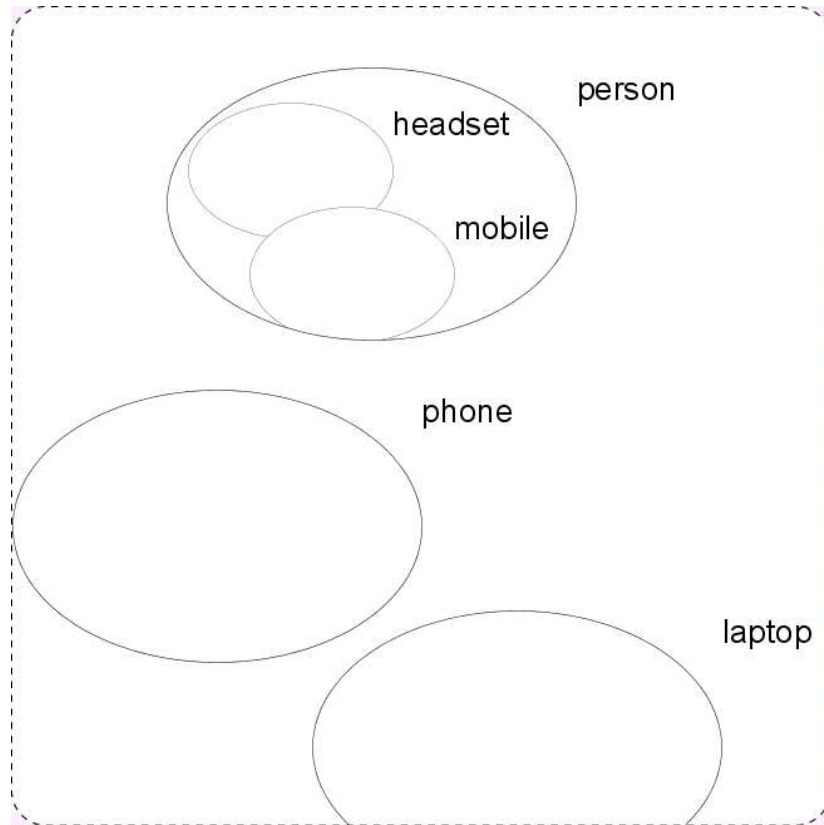
- Mobile ambients nicely describe location
- Let us try to describe our scenario...

Bigraphs – Place Graphs (1/2)

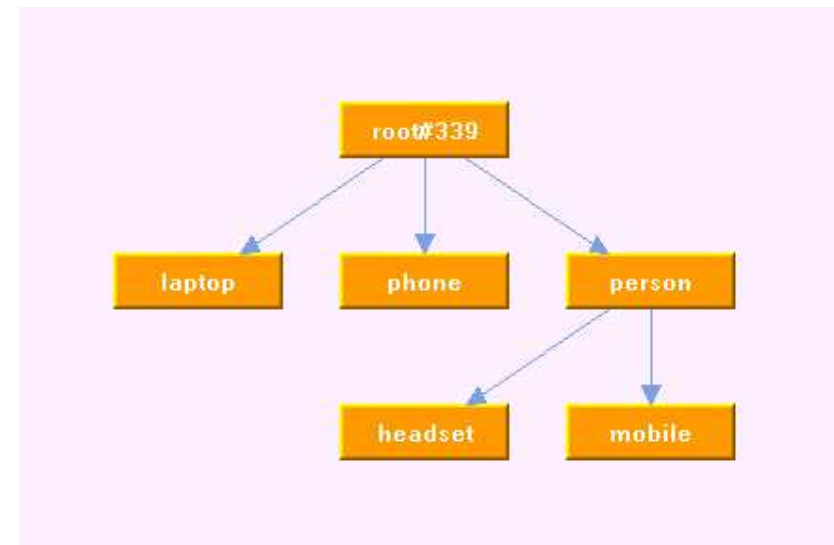
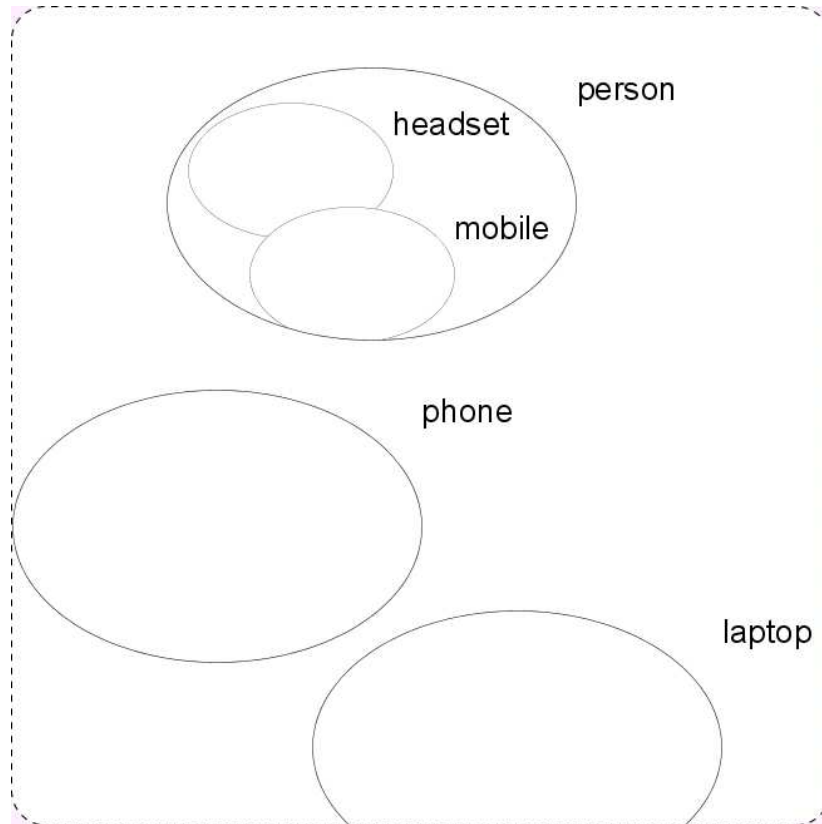
- Mobile ambients nicely describe location
- Let us try to describe our scenario...

```
person[ headset[] | mobile[] ] |  
      phone[] | laptop[]
```

Bigraphs – Place Graphs (2/2)

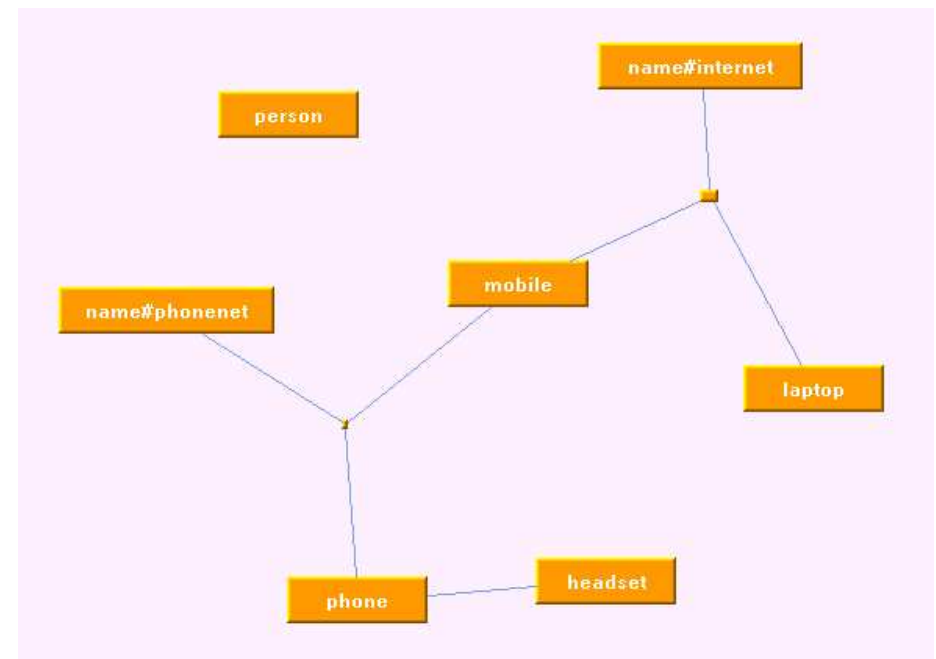


Bigraphs – Place Graphs (2/2)



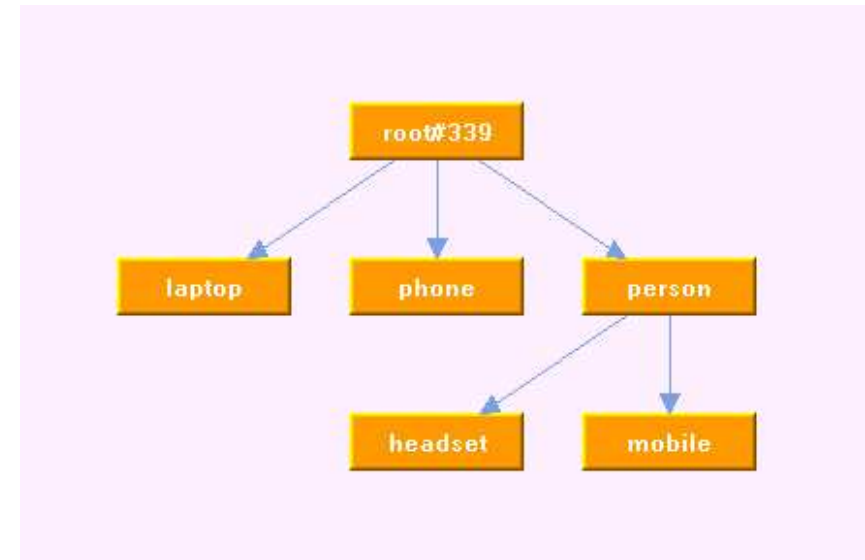
Bigraphs – Link Graphs

- We can describe linkage by drawing a graph with each entity as a node and each link as an edge
- Compare e.g. to network topology drawings



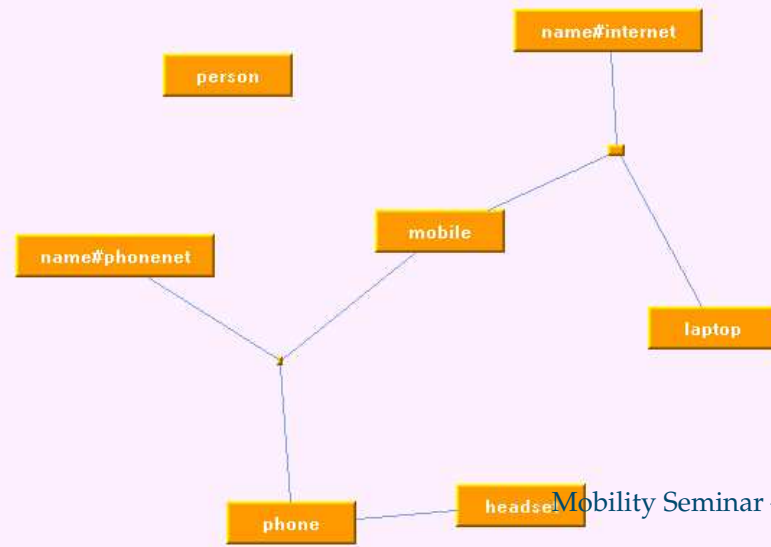
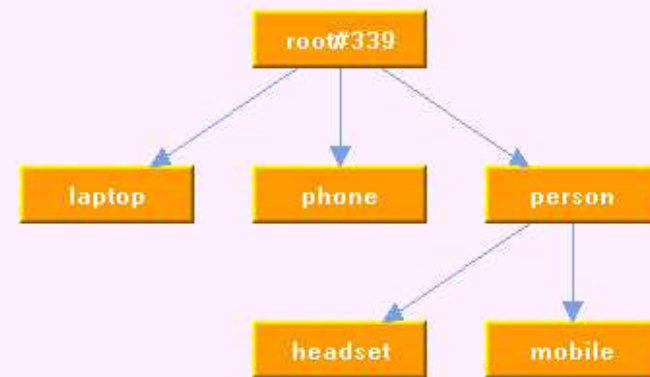
Bigraphs

- If we take the place graph

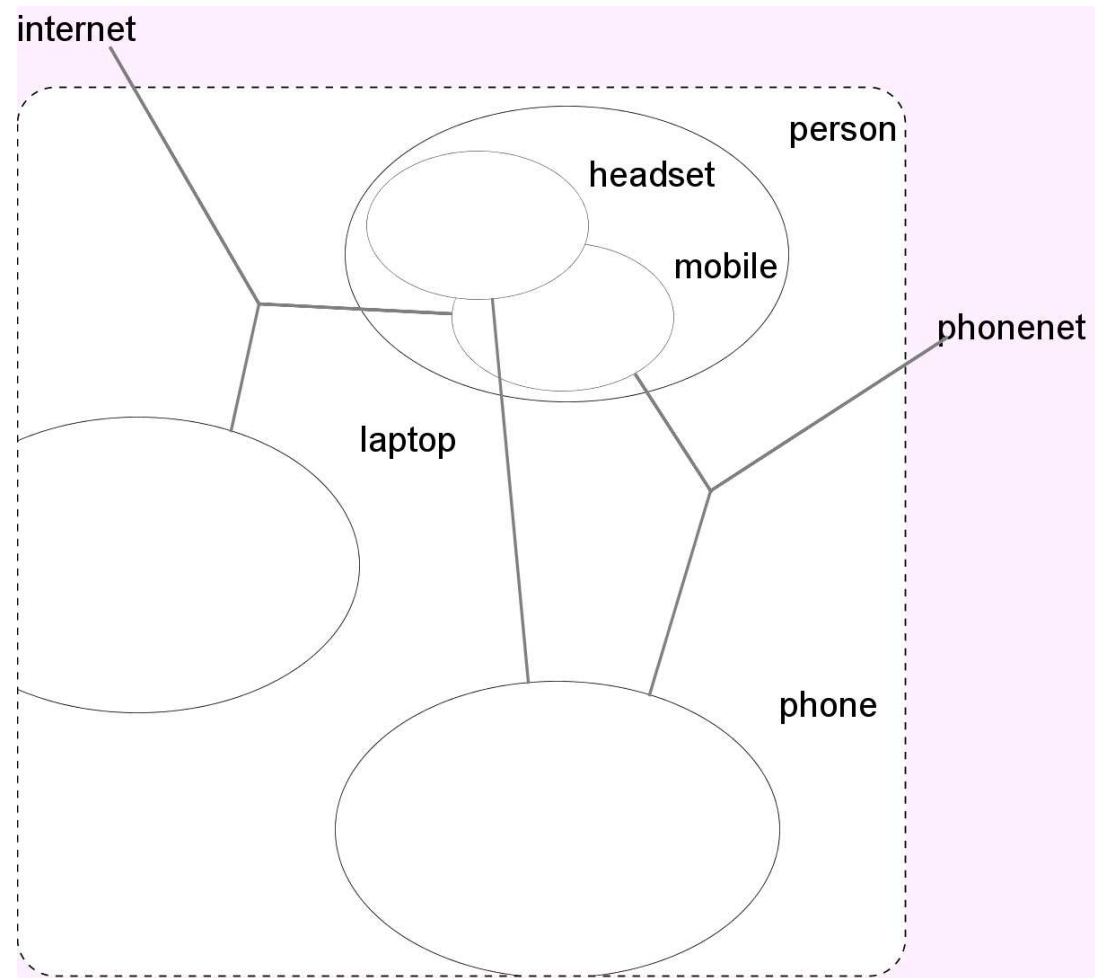


Bigraphs

- If we take the place graph
- ...and add the links from the link graph



We Obtain the Bigraph...



Bigraphs

- Bigraphs can be used to describe the state of a system, as we have just seen
- ...but the world is not static...

Bigraphical Reactive Systems

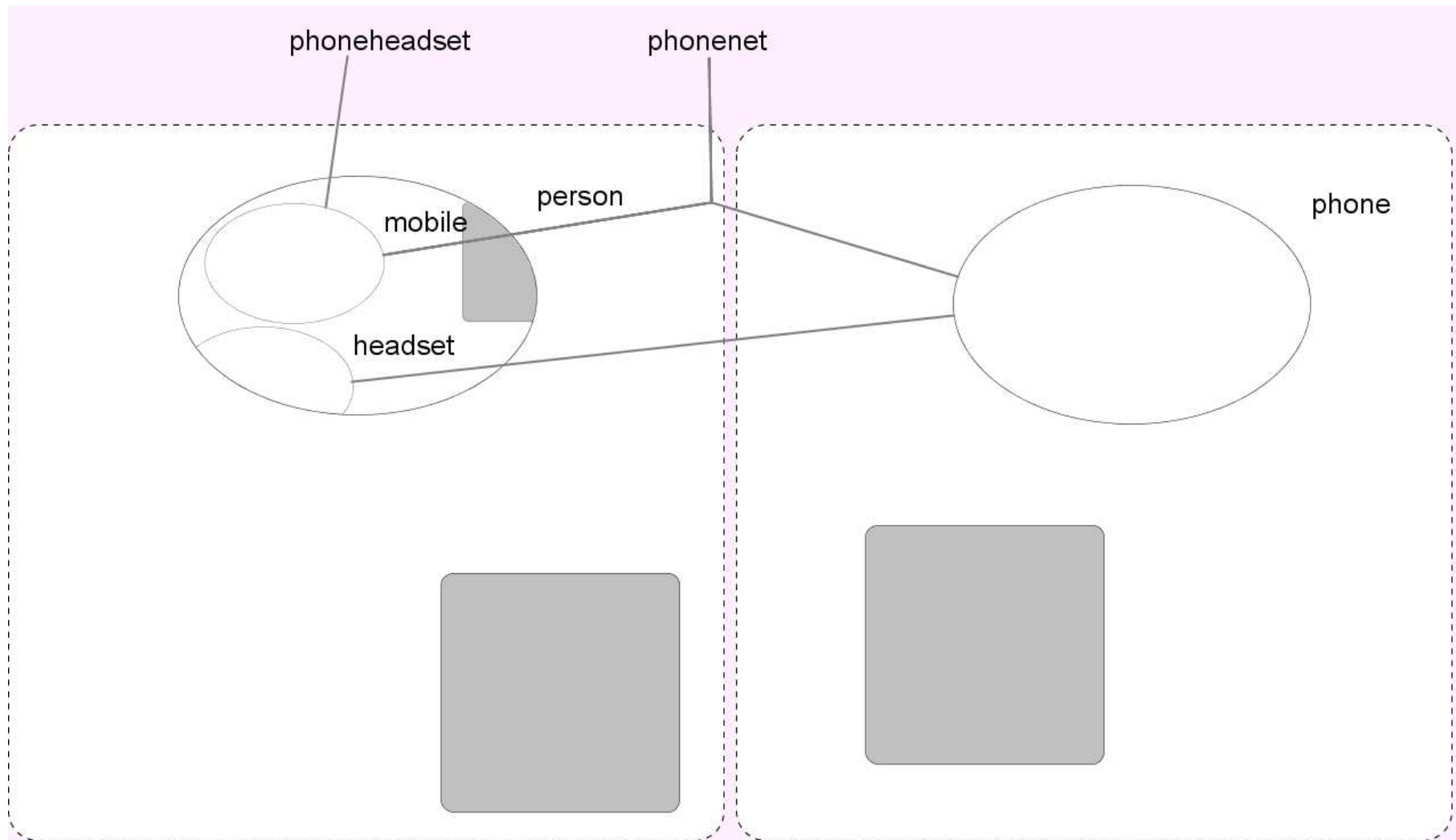
Scenario

- The person is talking on his phone using the head-set
- The person leaves the room
- The head-set should hand over to the mobile phone

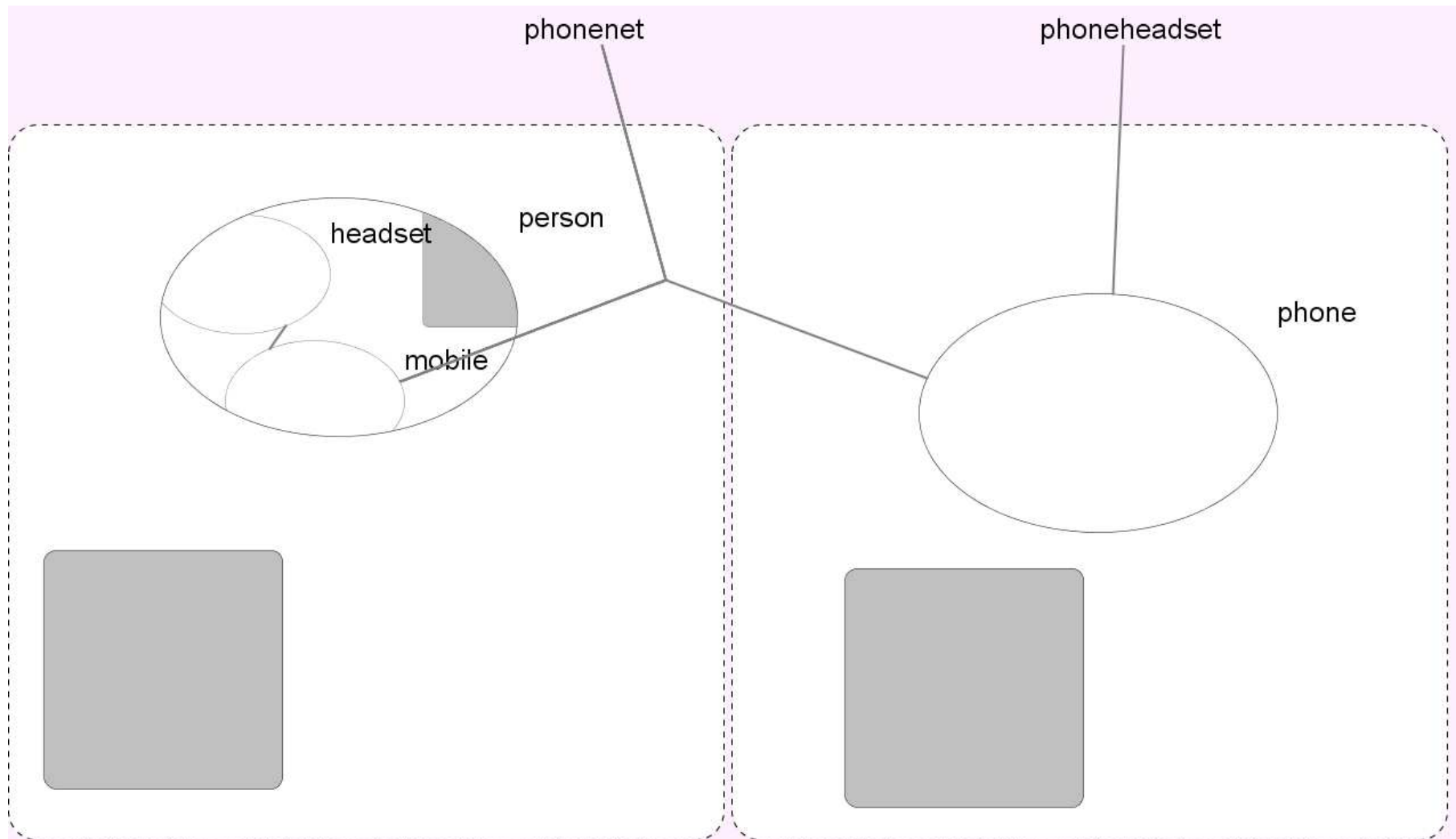
Reorganisations

- Reorganisations are changes of the configuration
- We describe the situation before the reorganisation (redex)
- ...and the situation after the reorganisation (reactum)

Reorganisations – Redex



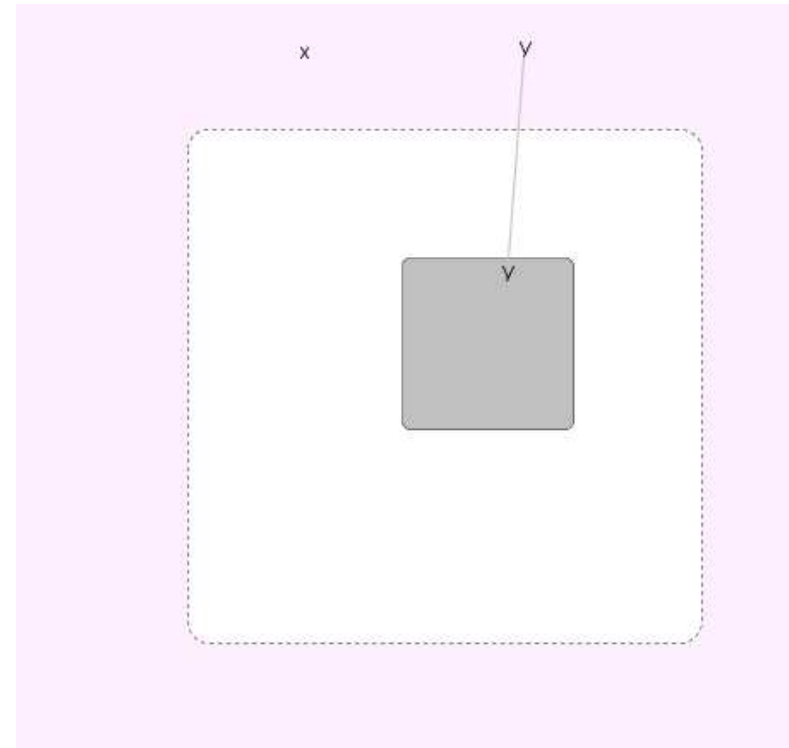
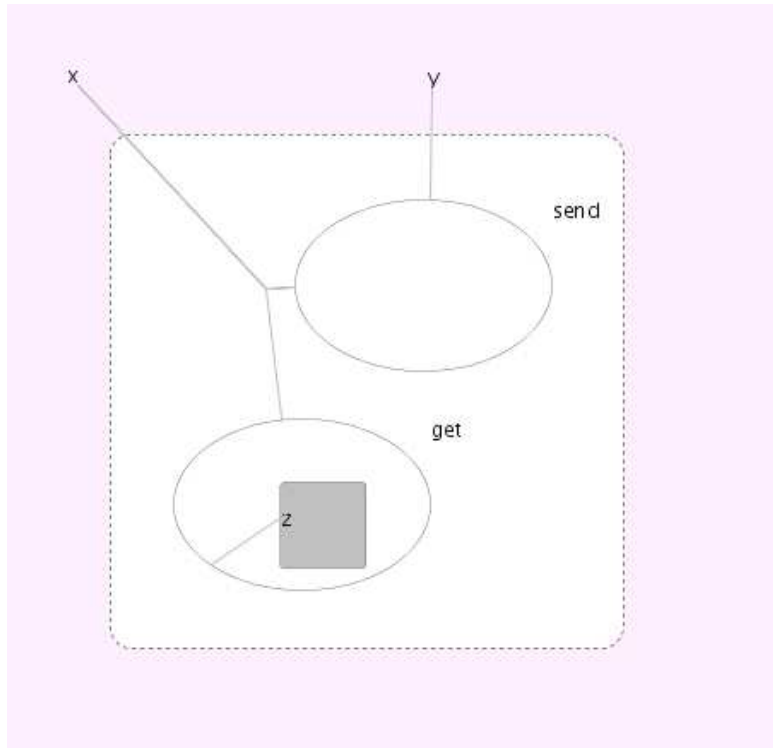
Reorganisations – Reactum



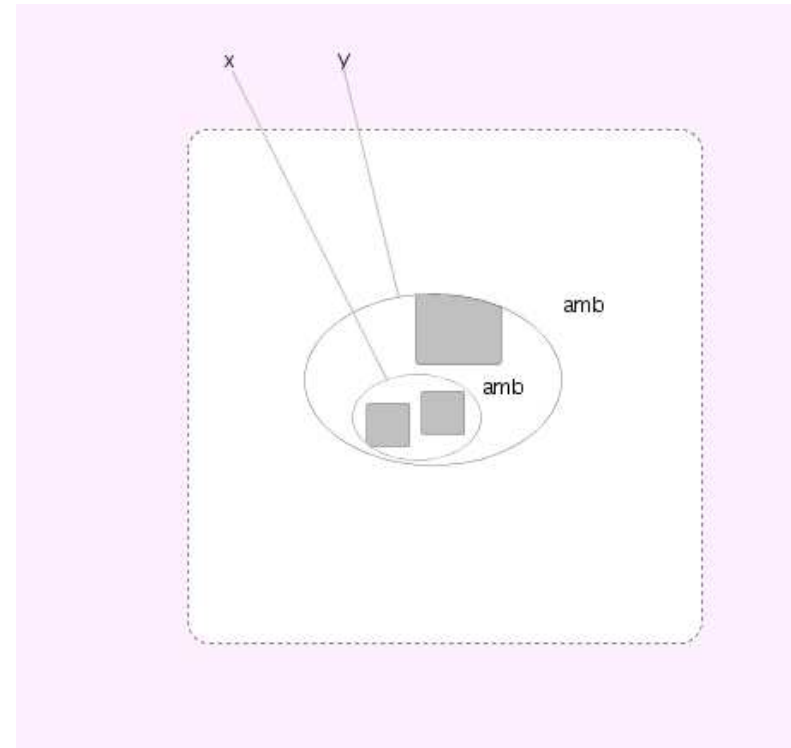
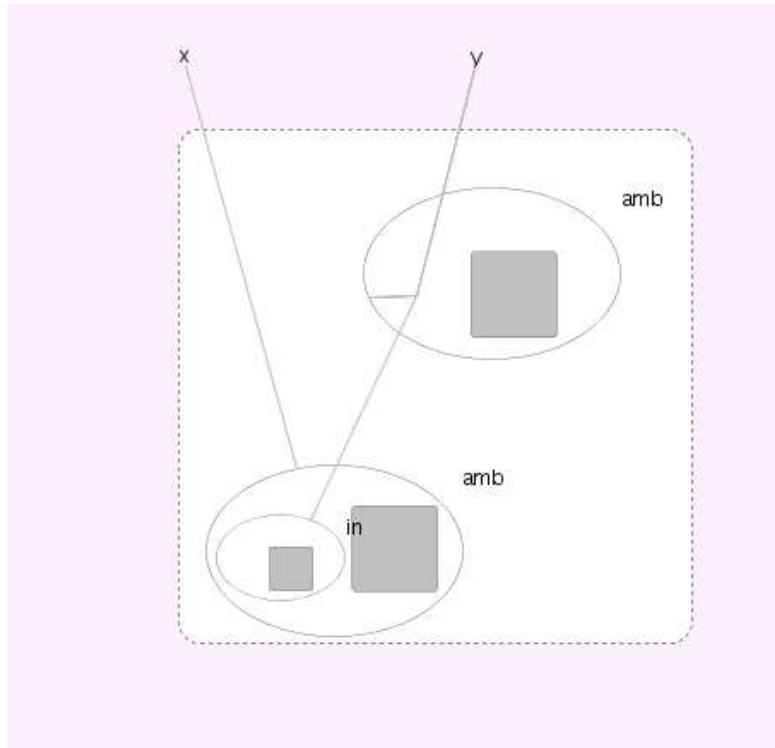
Expressiveness

- A lot of well-known mobile calculi can be expressed using Bigraphical Reactive Systems
 - ◆ π -calculus (asynchronous, synchronous)
 - ◆ Mobile Ambients
 - ◆ Condition-Event Petri nets
 - ◆ ...

Synchronisation for Async. π



Synchronisation for Ambients



Further Topics

We did not go through...

- Theoretical foundations
- Algebra for bigraphs (and DNF, CNF)
- Labelled transition systems for bigraphs
($L \circ a \rightarrow a' \iff a \xrightarrow{L} a'$)

More on Bigraphs

Robin Milners homepage:

<http://www.cl.cam.ac.uk/~rm135/>

TIN-CPN:

<http://wiki.daimi.au.dk/tincpn/>

Conclusions

- Bigraphs can describe *location* and *linking*
- Bigraphical Reactive Systems makes it easy to declaratively and intuitively describe system reconfigurations
- Bigraphical Reactive Systems are (at least) as powerfull as other well-known calculi
- Open and very interesting topic!