## Finite Automata Exercises

Deadline: 03/04 09:00

## Exercise 1

Explain what a language is. When is a language regular? What does it mean for a language to be recognized by an NFA.

Consider the regular language  $(a \cup b)^* a(ab)^*$ 

- 1. construct an NFA recognizing this language;
- 2. translate this NFA to an equivalent DFA; and
- 3. minimise the resulting DFA.

## Exercise 2

What does Kleene's Theorem tell us?

Let L and M be two languages recognized by NFAs, say  $\mathcal{A}$  and  $\mathcal{B}$ , respectively. Show that the following languages are recognizable as well.

- 1. concatenation  $L \cdot M$ ;
- 2. union  $L \cup M$ ; and
- 3. intersection  $L \cap M$ .

Hint: Construct corresponding new automatons based on  $\mathcal{A}$  and  $\mathcal{B}$ . For the last point, use a product construction, that runs  $\mathcal{A}$  and  $\mathcal{B}$  in parallel.

## Exercise 3

What is a decision problem, and what does it mean for such a problem to be in PTIME?

Define an algorithm that checks if a NFA  $\mathcal{A}$  accepts at least the words accepted by  $\mathcal{B}$ . What is the complexity of your algorithm. Is it optimal?

*Hint:* You may exploit the closure properties of recognizable languages and the known complexity bounds discussed in the lecture.