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# Semantic Formalisms 1: An Overview

- **Formal Methods**  
Operational Semantics  
CCS, Equivalences
- **Software Components**  
Fractal : hierarchical components  
Deployment, transformations  
Specification of components
- **Application to distributed applications**  
Active object and distributed components  
Behaviour models  
An analysis and verification platform

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# Program of the course:

## 1: Semantic Formalisms

- Semantics and formal methods:
  - motivations, definitions, examples
- Operational semantics, behaviour models :  
represent the complete behaviour of the system
  - CCS, Labelled Transition Systems
  - Equivalences

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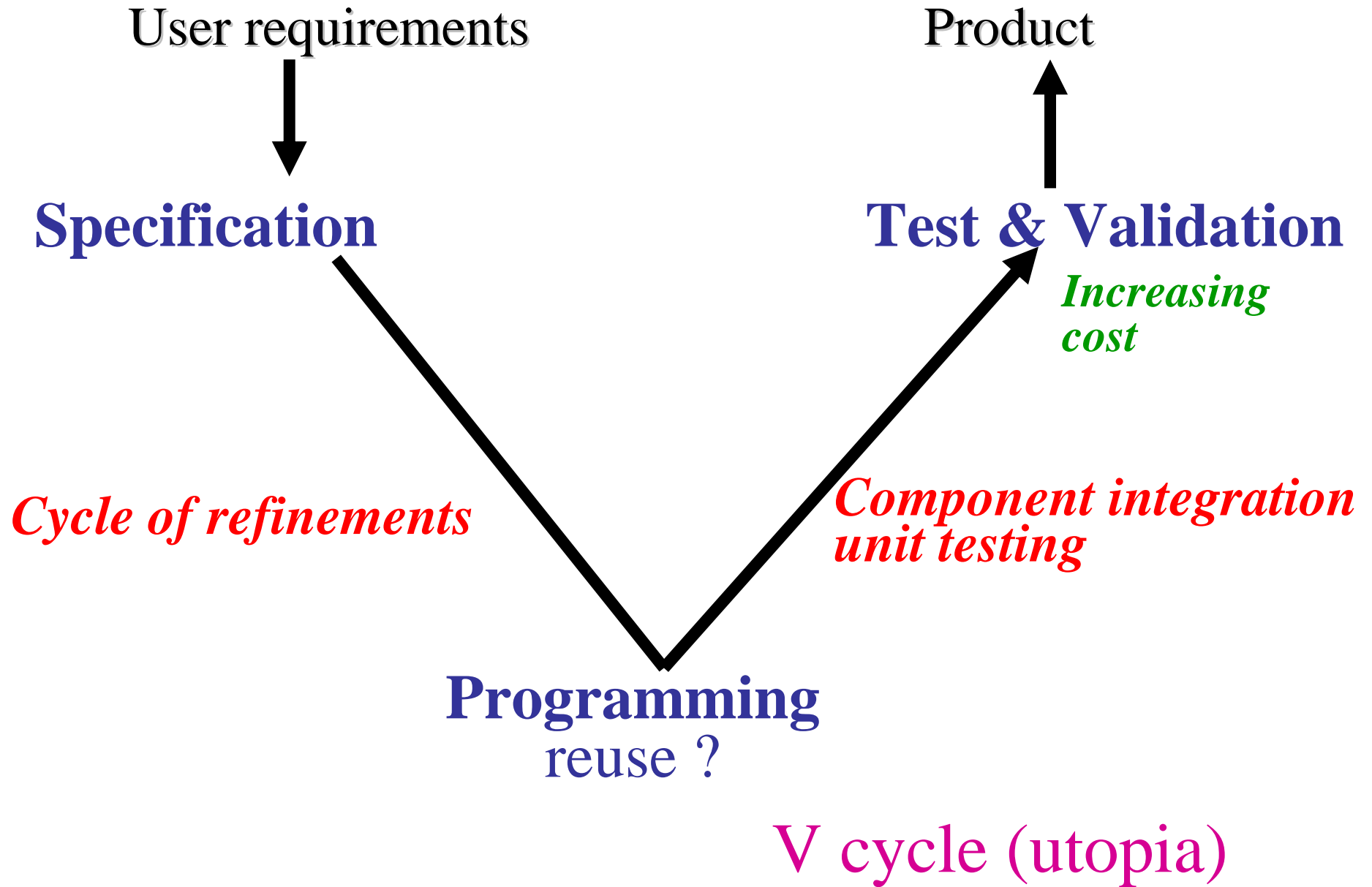
# Goals of (semi) Formal Methods

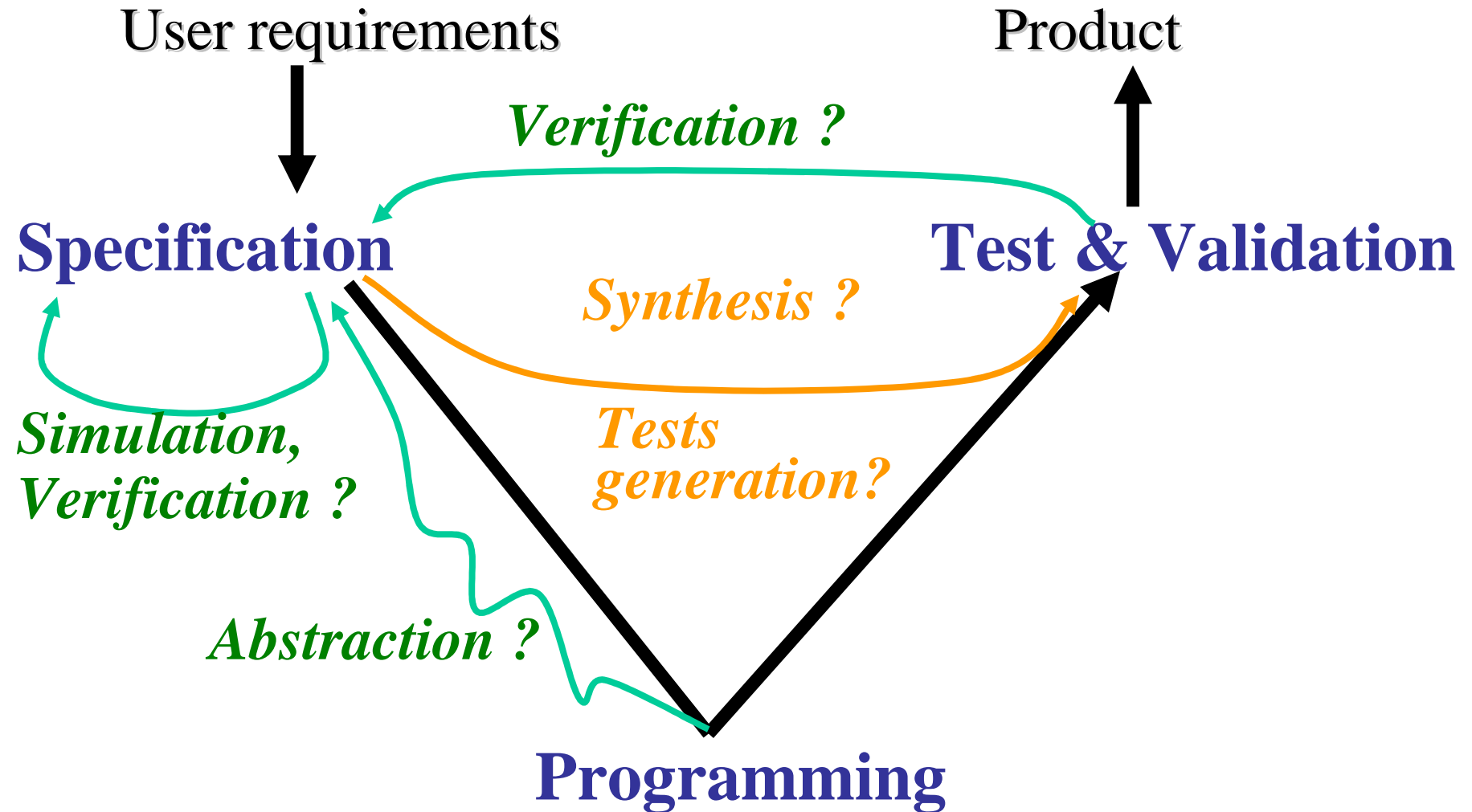
- Develop programs and systems as mathematical objects
- Represent them (**syntax**)
- Interpret/Execute them (**semantics**)
- Analyze / reason about their behaviours (**algorithmic, complexity, verification**)
- In addition to debug, using exhaustive tests and property checking.

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# Software engineering (ideal view)

- Requirements **informal**
  - User needs, general functionalities.
  - incomplete, unsound, *open*
- Detailed specification **formal ?**
  - Norms, standards?..., at least a reference
  - Separation of architecture and function. *No ambiguities*
- development
  - Practical implementation of components
  - Integration, deployment
- Tests (units then global) **vs verification ?**
  - Experimental simulations, certification





Benefits from formal methods ?  
*automatisation?*

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# Developer Needs

- Notations, syntax
  - textual
  - graphical (charts, diagrams...)
- Meaning, semantics
  - Non ambiguous signification, executability
  - interoperability, standards
- Instrumentation analysis methods
  - prototyping, light-weight simulation
  - verification

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# How practical is this ?

- Currently an utopia for large software projects, but :
  - Embedded systems
    - **Safety is essential** (no possible correction)
  - Critical systems
    - **Safety**, human lives (travel, nuclear)
      - Ligne Meteor, Airbus, route intelligente
    - **Safety**, economy (e-commerce, cost of bugs)
      - Panne réseau téléphonique US, Ariane 5
    - **Safety**, large volume (microprocessors)
      - Bug Pentium



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# Industry succes-stories

- Model-checking for circuit development
  - Finite systems, mixing combinatory logics with register states
- Specification of telecom standards
- Proofs of Security properties for Java code and crypto-protocols.
- Certification of embedded software (trains, aircrafts)

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# Semantics: definition, motivations

- **Give a (formal) meaning to words, objects, sentences, programs...**

## Why ?

- Natural language specifications are not sufficient
- A need for understanding languages: eliminate ambiguities, get a better confidence.
- Precise, compact and complete definition.
- Facilitate learning and implementation of languages

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# Formal semantics, Proofs, and Tools

- **Manual proofs are error-prone !**
- **Tools for Execution and Reasoning**
  - semantic definitions are input for meta-tools
- **Integrated in the development cycle**
  - consistent and safe specifications
  - requires validation (proofs, tests, ...)
- **Challenge:**

Expressive power versus executability...

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# Concrete syntax, Abstract syntax, and Semantics

- **Concrete syntax:**
  - scanners, parsers, BNF, ... many tools and standards.
- **Abstract syntax:**
  - operators, types,  $\Rightarrow$  *tree representations*
- **Semantics:**
  - based on abstract syntax
  - static semantics: typing, analysis, transformations
  - dynamic: evaluation, behaviours, ...

This is not only a concern for theoreticians: it is the very basis for compilers, programming environments, testing tools, etc...

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# Static semantics : examples

Checks non-syntactic constraints

- compiler front-end :
  - declaration and utilisation of variables,
  - typing, scoping, ... static typing => no execution errors ???
- or back-ends :
  - optimisers
- defines legal programs :
  - Java byte-code *verifier*
  - JavaCard: legal acces to shared variables through firewall

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# Dynamic semantics

- Gives a meaning to the program (a semantic value)
- Describes the behaviour of a (legal) program
- Defines a language interpreter

$\vdash e \rightarrow e'$

let  $i=3$  in  $2*i \rightarrow$  semantic value = 6

- Describes the properties of legal programs

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# The different semantic families (1)

- **Denotational semantics**
  - mathematical model, high level, abstract
- **Axiomatic semantics**
  - provides the language with a theory for proving properties / assertions of programs
- **Operational semantics**
  - computation of the successive states of an abstract machine
  - used to build evaluators, simulators.

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# Semantic families (2)

- **Denotational semantics**

- defines a model, an abstraction, an interpretation

*⇒ for the language designers*

- **Axiomatic semantics**

- builds a logical theory

*⇒ for the programmers*

- **Operational semantics**

- builds an interpreter, or a finite representation

*⇒ for the language implementors*



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# Operational Semantics (Plotkin 1981)

- Describes the computation
- States and configuration of an abstract machine:
  - Stack, memory state, registers, heap...
- Abstract machine transformation steps
- Transitions: current state  $\rightarrow$  next state

**Several different operational semantics**

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## Natural Semantics : big steps (Kahn 1986)

- **Defines the results of evaluation.**
- **Direct relation from programs to results**

$$\text{env} \mid\text{- prog} \Rightarrow \text{result}$$

- env: binds variables to values
- result: value given by the execution of prog

## Reduction Semantics : small steps

describes **each elementary step** of the evaluation

- **rewriting relation** : reduction of program terms
- **stepwise reduction**:  $\langle \text{prog}, s \rangle \rightarrow \langle \text{prog}', s' \rangle$ 
  - infinitely, or until reaching a normal form.

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# Differences: small / big steps

- Big steps:
  - abnormal execution : add an « error » result
  - non-terminating execution : problem
    - deadlock (no rule applies, evaluation failure)
    - looping program (infinite derivation)
- Small steps:
  - explicit encoding of non termination, divergence
  - confluence, transitive closure  $\rightarrow^*$

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# Natural semantics: examples (big steps)

- **Type checking :**

Terms:  $X \mid tt \mid ff \mid \text{not } t \mid n \mid t1 + t2 \mid \text{if } b \text{ then } t1 \text{ else } t2$

Types: Bool, Int

- **Judgements :**

**Typing:**  $\Gamma \vdash P : \tau$

**Reduction:**  $\Gamma \vdash P \Rightarrow v$

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# Deduction rules

## Values and expressions:

$$\Gamma \vdash tt : \mathbf{Bool}$$
$$\Gamma \vdash ff : \mathbf{Bool}$$
$$\Gamma \vdash tt \Rightarrow \mathbf{true}$$
$$\Gamma \vdash ff \Rightarrow \mathbf{false}$$
$$\Gamma \vdash t1 : \mathbf{Int} \quad \Gamma \vdash t2 : \mathbf{Int}$$

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$$\Gamma \vdash t1 + t2 : \mathbf{Int}$$
$$\Gamma \vdash t1 \Rightarrow n1 \quad \Gamma \vdash t2 \Rightarrow n2$$

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$$\Gamma \vdash t1 + t2 \Rightarrow n1+n2$$

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# Deduction rules

- Environment :

$$\delta :: \{x \rightarrow v\} \vdash x \Rightarrow v$$

$$\delta :: \{x : \tau\} \vdash x : \tau$$

- Conditional :

$$\Gamma \vdash b \Rightarrow \text{true} \quad \Gamma \vdash e1 \Rightarrow v$$

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$$\Gamma \vdash \text{if } b \text{ then } e1 \text{ else } e2 \Rightarrow v$$

**Exercice : typing rule ?**

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# Operational semantics: big steps for reactive systems

## **Behaviours**

- **Distributed, synchronous/asynchronous programs:**
  - transitions represent communication events
- **Non terminating systems**
- **Application domains:**
  - telecommunication protocols
  - reactive systems
  - internet (client/server, distributed agents, grid, e-commerce)
  - mobile / pervasive computing



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# Synchronous and asynchronous languages

- Systems build from communicating components :  
**parallelism, communication, concurrency**
- **Asynchronous Processes**
  - Synchronous communications (**rendez-vous**)  
Process calculi: CCS, CSP, Lotos
  - Asynchronous communications (**message queues**)  
**SDL**      modelisation of channels
- **Synchronous Processes** (**instantaneous diffusion**)  
Esterel, Sync/State-Charts, Lustre

**Question on D. Caromel course: how do you classify ProActive ?**

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# Labelled Transition Systems (LTS)

- Basic model for representing reactive, concurrent, parallel, communicating systems.

- Definition:

$\langle S, s_0, L, T \rangle$

$S$  = set of states

$s_0 \in S$  = initial state

$L$  = set of labels (events, communication actions, etc)

$T \subseteq S \times L \times S$  = set of transitions

Notation:  $s_1 \xrightarrow{a} s_2 = (s_1, a, s_2) \in T$

# CCS

(R. Milner, “A Calculus of Communicating Systems”, 1980)

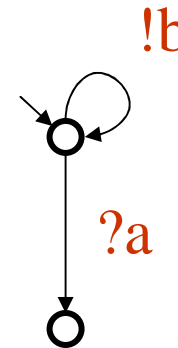
- Parallel processes communicating by Rendez-vous :

$$?a:!b:nil \xrightarrow{?a} !b:nil \xrightarrow{!b} nil$$

$$?a:P \parallel !a:Q \xrightarrow{\tau} P \parallel Q$$

- Recursive definitions :

$$\text{let rec } \{ st0 = ?a:st1 + !b:st0 \} \text{ in } st0$$



# CCS : behavioural semantics (1)

## Operators and rules

Inactivity

*nil (or skip)*

Action prefix

$\mathbf{a:P} \xrightarrow{\mathbf{a}} P$

Non deterministic  
choice

$$\frac{P \xrightarrow{\mathbf{a}} P'}{P+Q \xrightarrow{\mathbf{a}} P'}$$
$$\frac{Q \xrightarrow{\mathbf{a}} Q'}{P+Q \xrightarrow{\mathbf{a}} Q'}$$

# CCS : behavioural semantics (2)

## More operators, more rules

Emissions & réceptions  
are dual actions

$$\frac{P \xrightarrow{a} P' \quad Q \xrightarrow{a} Q'}{P \parallel Q \xrightarrow{a} P' \parallel Q} \quad \frac{Q \xrightarrow{a} Q'}{P \parallel Q \xrightarrow{a} P \parallel Q'}$$

$\tau$  invisible action  
(internal communication)

$$\frac{P \xrightarrow{!a} P' \quad Q \xrightarrow{?a} Q'}{P \parallel Q \xrightarrow{\tau} P' \parallel Q'}$$

Recursion :

$$\frac{[\mu X.P/X]P \xrightarrow{a} P'}{\mu X.P \xrightarrow{a} P'}$$

Local action :

Tool for forcing synchronisation

$$\frac{P \xrightarrow{a} P' \quad a \notin \{?b, !b\}}{\text{local } \mathbf{b} \text{ in } P \xrightarrow{a} \text{local } \mathbf{b} \text{ in } P'}$$

# Derivations

(construction of each transition step)

$$\begin{array}{c}
 \frac{}{?a:P \xrightarrow{?a} P} \text{Prefix} \\
 \frac{}{?a:P \parallel Q \xrightarrow{?a} P \parallel Q} \text{Par-L} \qquad \frac{}{!a:R \xrightarrow{!a} R} \text{Prefix} \\
 \frac{}{(?a:P \parallel Q) \parallel !a:R \xrightarrow{\tau} (P \parallel Q) \parallel R} \text{Par-2}
 \end{array}$$

Par-2(Par\_L(Prefix), Prefix)

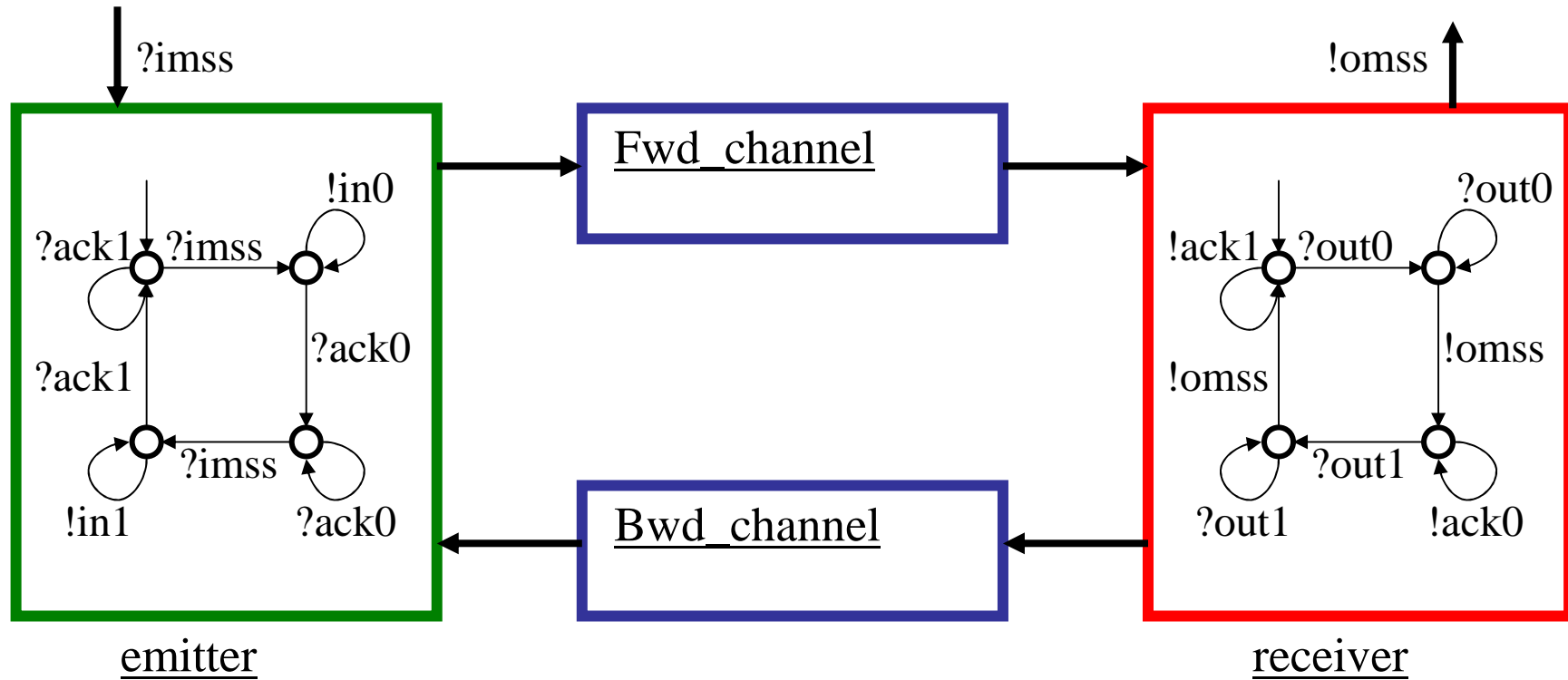
One amongst 3 possible derivations

Another one :

Par-L(Par\_L(Prefix))

$$(?a:P \parallel Q) \parallel !a:R \xrightarrow{?a} (P \parallel Q) \parallel !a:R$$

# Example: Alternated Bit Protocol



*Hypotheses: channels can loose messages*

Write in CCS ?

*Requirement:*

*the protocol ensures no loss of messages*



## Example: Alternated Bit Protocol (2)

- **emitter** =

```
let rec {em0 = ?ack1 :em0 + ?imss:em1
  and em1 = !in0 :em1 + ?ack0 :em2
  and em2 = ?ack0 :em2 + ?imss :em3
  and em3 = !in1 :em3 + ?ack1 :em0
}
in em0
```

- **ABP** = local {in0, in1, out0, out1, ack0, ack1, ...}  
in emitter || Fwd\_channel || Bwd\_channel || receiver

---

## Example: Alternated Bit Protocol (3)

*Channels that loose and duplicate messages (in0 and in1) but preserve their order ?*

- Exercise :
  - 1) Draw an LTS describing the loosy channel behaviour
  - 2) Write the same description in CCS

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# Behavioural Equivalences

- **Intuition:**
  - Same possible sequences of observable actions
  - Finite / infinite sequences
  - Various refinements of the concept of observation
- **Definition: Trace Equivalence**

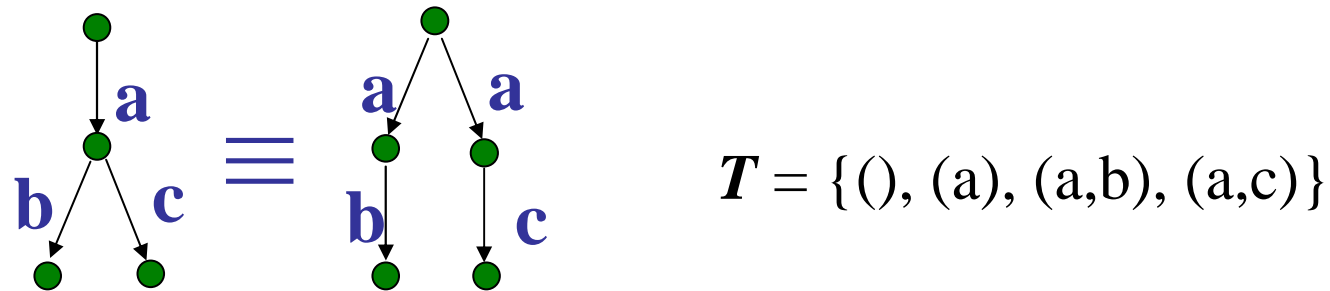
For a LTS  $(S, s_0, L, T)$  its **Trace language**  $T$  is the set of finite sequences  $\{t = t_1, \dots, t_n \text{ such that } \exists s_0, \dots, s_n \in S^{n+1}, \text{ and } (s_{n-1}, t_n, s_n) \in T\}$

Two LTSs are **Trace equivalent** iff their **Trace languages** are equal.

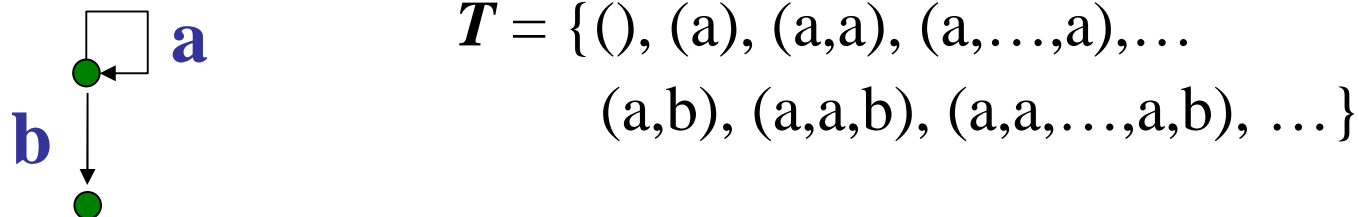
Corresponding Ordering: **Trace inclusion**

# Trace Languages, Examples

1. Those 2 systems are trace equivalent:



2. A trace language can be an infinite set:



# Bisimulation

- **Behavioural Equivalence**

- non distinguishable states by observation:

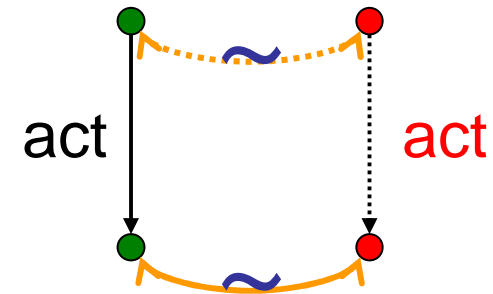
two states are equivalent if for all possible transitions labelled by the same action, there exist equivalent resulting states.

- **Bisimulations**

$R \subseteq S \times S$  is a bisimulation iff

- It is a equivalence relation

- $\forall (p,q) \in R,$   
 $(p,l,p') \in T \Rightarrow \exists q' / (q,l,q') \in T \text{ and } (p',q') \in R$

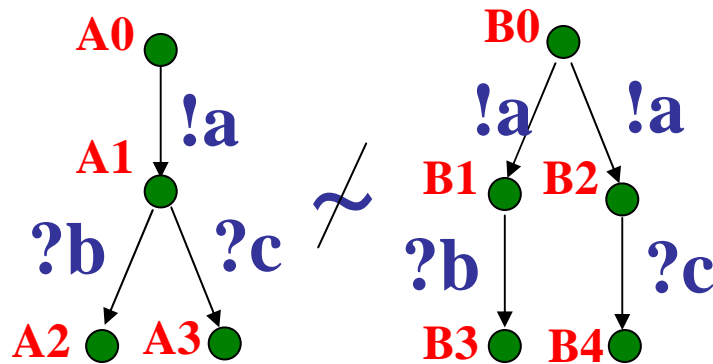


- **$\sim$  is the coarsest bisimulation**

2 LTS are bisimilar iff their initial states are in  $\sim$   
quotients = canonical normal forms

# Bisimulation (3)

- More precise than trace equivalence :



**No state in B is equivalent to A1**

- Preserves deadlock properties.

# Bisimulation (4)

- Congruence laws:

$$P1 \sim P2 \Rightarrow a:P1 \sim a:P2 \quad (\forall P1, P2, a)$$

$$P1 \sim P2, \quad Q1 \sim Q2 \Rightarrow P1+Q1 \sim P2+Q2$$

$$P1 \sim P2, \quad Q1 \sim Q2 \Rightarrow P1 \parallel Q1 \sim P2 \parallel Q2$$

**Etc...**

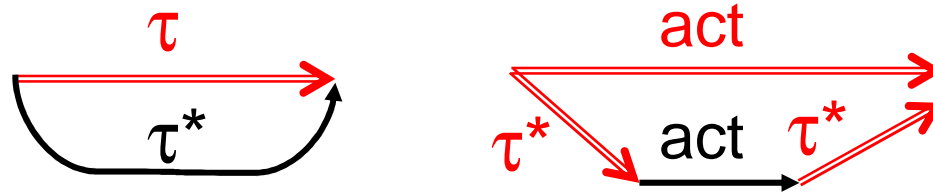
- $\sim$  is a congruence for all CCS operators :  
for any CCS context  $C[.]$ ,  $C[P] \sim C[Q] \Leftrightarrow P \sim Q$

Basis for compositional proof methods

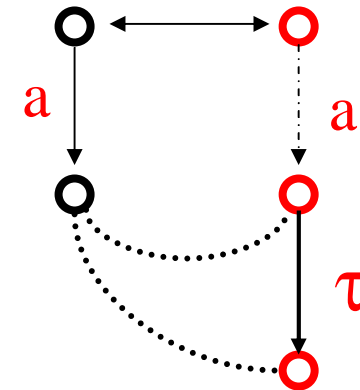


# Observational Equivalences

- Weak bisimulation
  - Abstraction: hidden actions
  - allows for arbitrary many internal actions

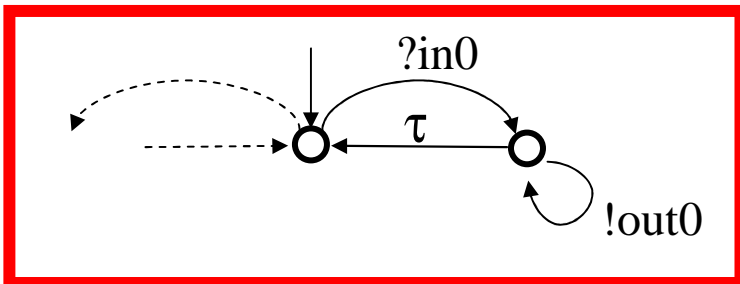
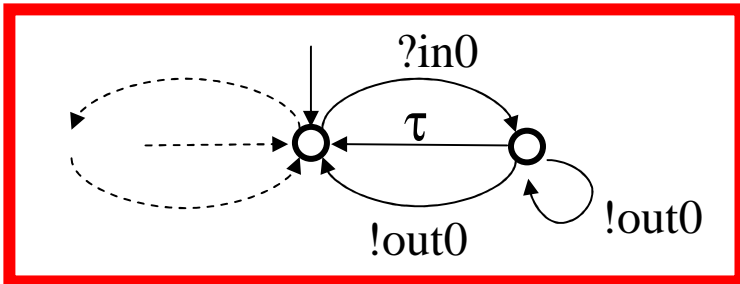


- Branching bisimulation
  - ... only staying in equivalent states



**Still existence of a canonical minimal automata**  
**Computation is polynomial**

## Exercice 2 : Bisimulations



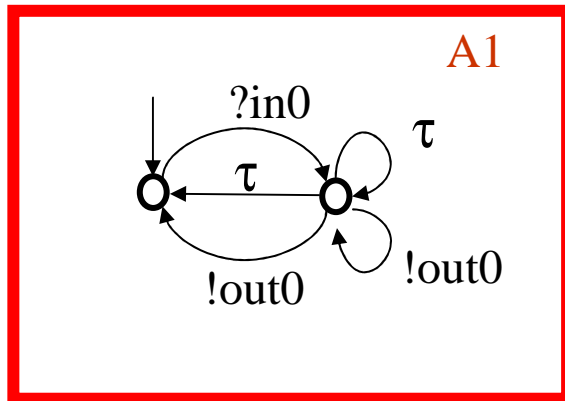
*Are those LTSs equivalent by:*

*- Strong bisimulation?*

*- Weak bisimulation ?*

*In each case, give a proof.*

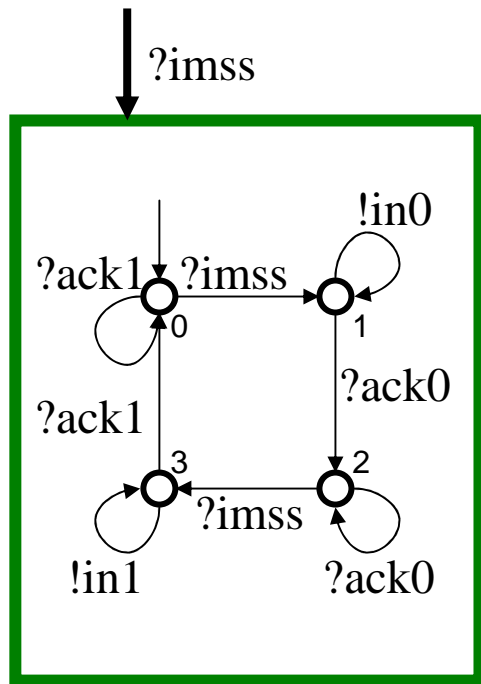
## Exercice 3 : Bisimulation



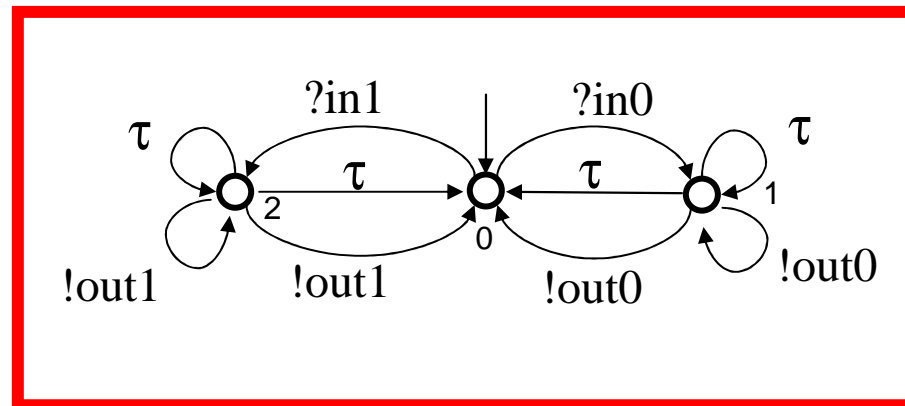
- Exercice :
  - 1) Compute the strong minimal automaton for A1.
  - 2) Compute the weak minimal automaton for A1.

# Exercice 4 : Synchronized Product

*Compute the synchronized product of the LTS representing the ABP emitter with the (forward) Channel:*



local {in0, in1} in  
(Emitter || Channel)



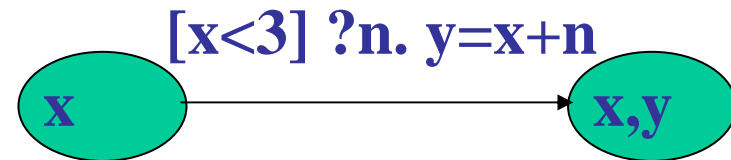
# Automatas with data

from state  $\langle i \rangle$

provided  $\text{guard\_cond}(\text{vars})$

then execute  $\text{body}$

goto state  $\langle j \rangle$



- We need add:  $\text{if\_then\_else}$  : tree of successor states  
 $\text{guards}$  and  $\text{conditions}$  on external  $\text{signals}$   
 $\text{local variables}$  (scoping)



*Graphical specifications languages :*  
*SDL, Statecharts, etc.*

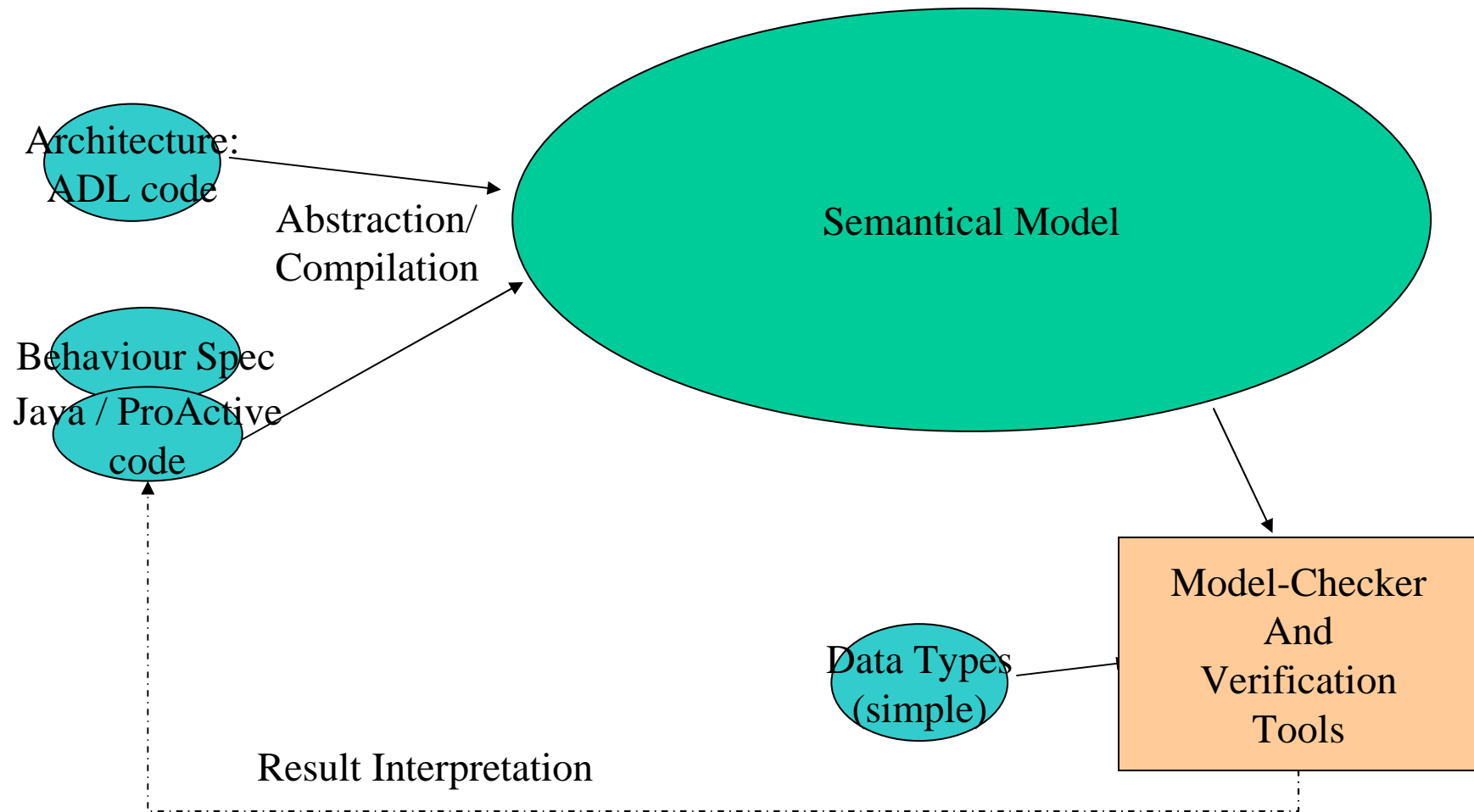
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# The Dream

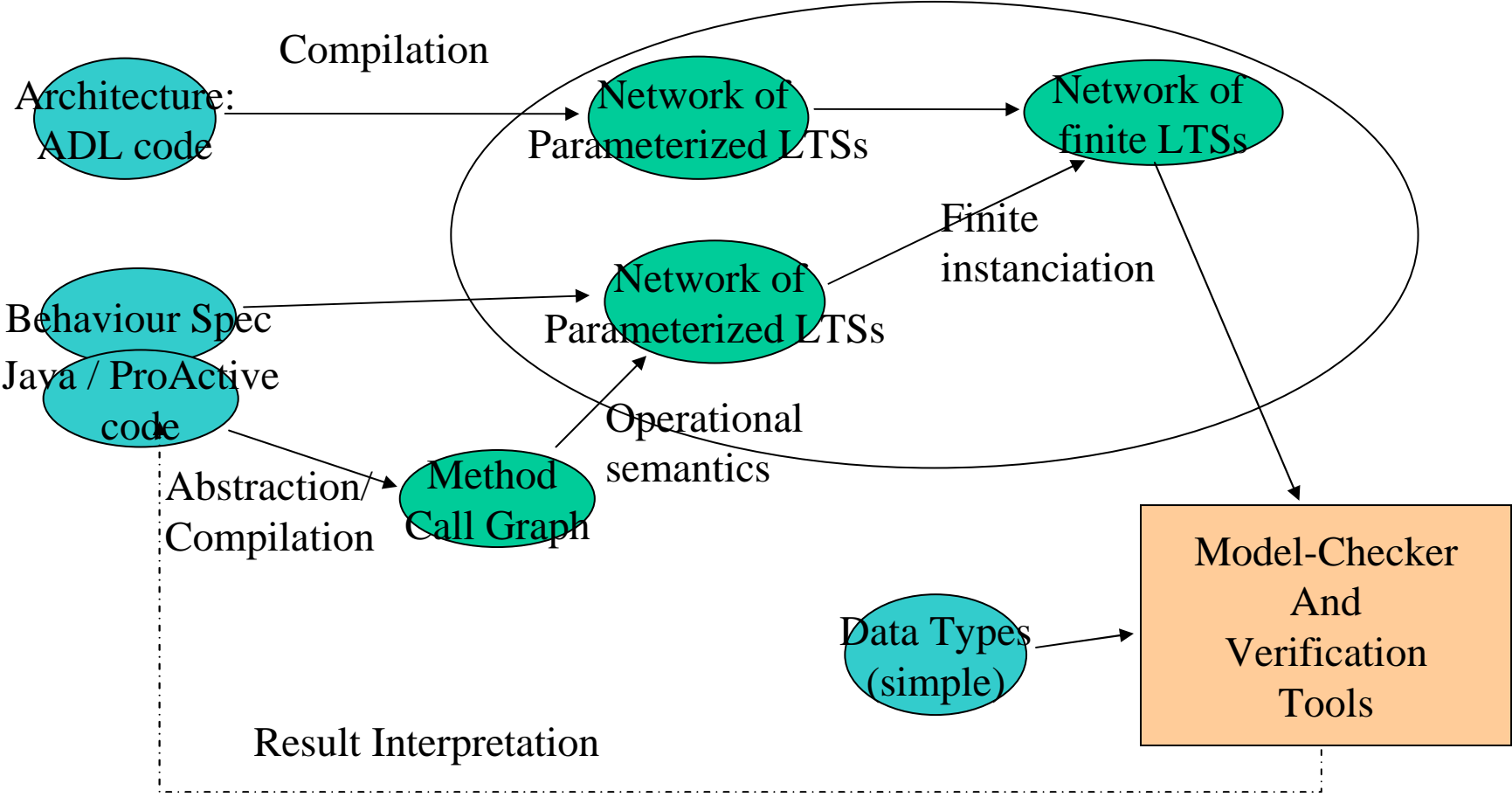
Provide Analysis and Verification Tools to the  
(non-specialist) programmer

- Specification Language (textual or graphical)
- Code analysis tools
- Automatic Model-Checking

# Tool Set (future...)



# Tool Set (future...)





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# Next courses

## 3) Software Components

- Fractal : main concepts
- Deployment, management, transformations
- Specification of components

## 2) Application to distributed applications

- ProActive : active object and distributed components
- Behaviour models
- Tools : build an analysis and verification platform

**[www-sop.inria.fr/oasis/Eric.Madelaine](http://www-sop.inria.fr/oasis/Eric.Madelaine)**

 **Teaching/RSD-2006**