

# Sinus For Ever

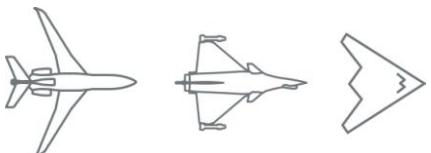
30 ans de simulation et optimisation  
aérodynamique

Bruno Stoufflet,

Frédéric Chalot, Michel Mallet, Michel Ravachol, Gilbert Rogé

10/04/2015

HIGHER TOGETHER™



# Aerodynamics Optimisation: Gradient computation



*State equation*

$$E(\mu, W(\mu)) = 0$$

*Cost function*

$$j(\mu) = J(\mu, W(\mu))$$

*Constraints functions*

$$g(\mu) = G(\mu, W(\mu))$$

*Minimizing  $j(\mu)$  while respecting constraints  $g_i(\mu) \leq 0$*

We observe

$$f(\mu) = F(\mu, W(\mu)) = (J(\mu, W(\mu)), G(\mu, W(\mu)))$$

$$\mu = (\nu, l)$$

with  $\nu$  = aerodynamic parameters

and  $l$  = geometric parameters (CAD modeler)

PDE control theory  
J-L Lions

Dunod, 1968

# Aerodynamics Optimisation: Gradient computation



To estimate

$$\mu = (\nu, l)$$

$$\delta f = \frac{df(\mu)}{d\mu} \cdot \delta \mu = \frac{dF(\mu, W(\mu))}{d\mu} \cdot \delta \mu$$

$$\delta f = \frac{\partial F}{\partial W} \frac{\partial W}{\partial l} \cdot \delta l + \frac{\partial F}{\partial W} \frac{\partial W}{\partial \nu} \cdot \delta \nu + \frac{\partial F}{\partial l} \cdot \delta l + \frac{\partial F}{\partial \nu} \cdot \delta \nu$$

Thanks to the state equation

$$E(\mu, W(\mu)) = 0$$

and then

$$\delta E(\mu, W(\mu)) = \frac{\partial E}{\partial W} \cdot \delta W + \frac{\partial E}{\partial \mu} \cdot \delta \mu = 0$$

Thanks to the mesh deformation equation

$$L(d(\nu), D(\nu)) = 0$$

and then

$$\delta L(d(\nu), D(\nu)) = \frac{\partial L}{\partial d} \cdot \delta d + \frac{\partial L}{\partial D} \cdot \delta D = 0$$

# Aerodynamics Optimisation: Gradient computation



- Evaluate variations of the Lagrangian

$$\delta \mathcal{F}^* = \delta \mathcal{F} - \Psi(\mu)^T \delta E - \Phi(v)^T \delta L$$

- with

$$\left( \frac{\partial E}{\partial W}(l, D(v), W(\mu)) \right)^T \Psi(\mu) = \left[ \frac{\partial F}{\partial W}(\mu, W(\mu)) \right]^T$$
$$\frac{\partial F}{\partial D}(l, D(v), W(\mu)) - \Psi^T \frac{\partial E}{\partial D}(l, D(v), W(\mu)) = \Phi^T \frac{\partial L}{\partial D}(d(v), D(v))$$

- to obtain

$$\begin{cases} \frac{dF}{dl} = \frac{\partial F}{\partial l} - \Psi^T \left[ \frac{\partial E}{\partial l} \right] \\ \frac{dF}{dv} = -\Phi^T \left[ \frac{\partial L}{\partial d} \frac{\partial d}{\partial v} \right] \end{cases}$$

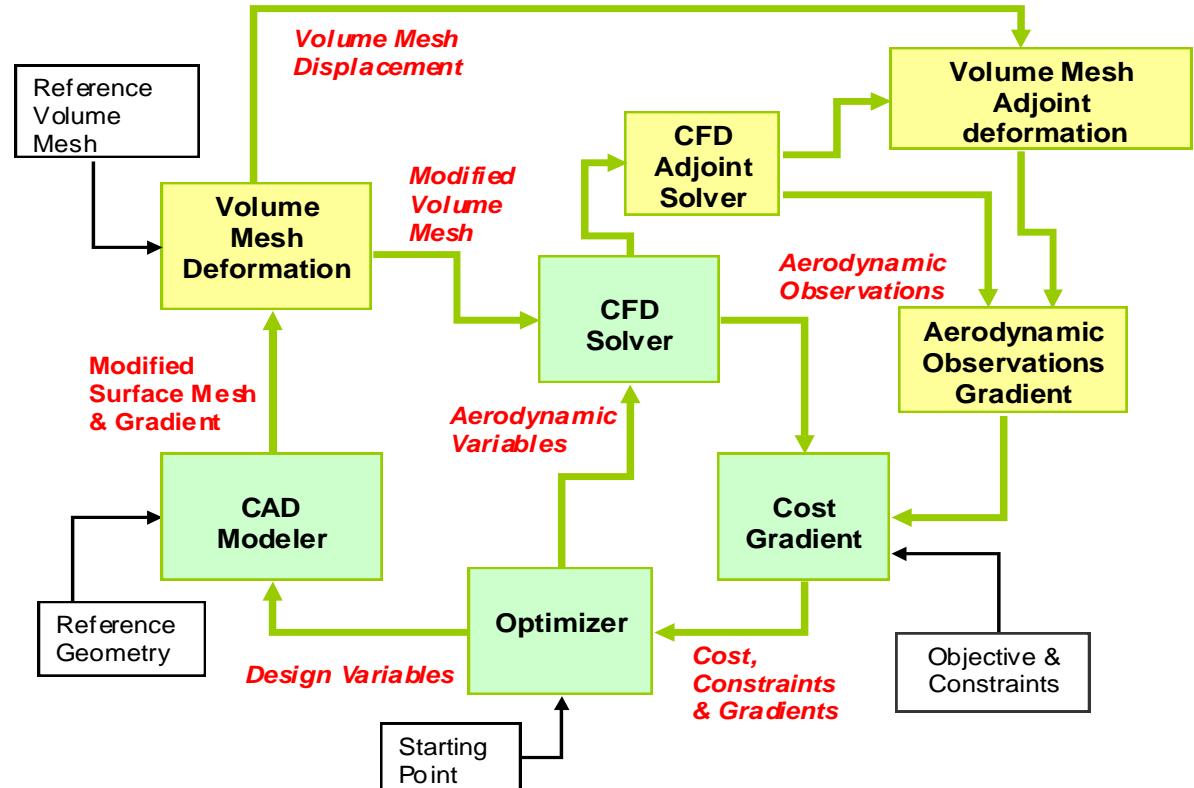
# Automatic shape optimization

## Introduction

(1/5)



- Complex process : large effort to develop and mature
- Key ingredients:
  - Adjoint approach including mesh motion
  - Parameterization (CAD + features)
  - Extensive library of cost functions
- Process progressively applied to many real life design problems
  - Strong interaction with design team to define relevant formulation of the problem



# Aerodynamics Optimisation: Optimization techniques



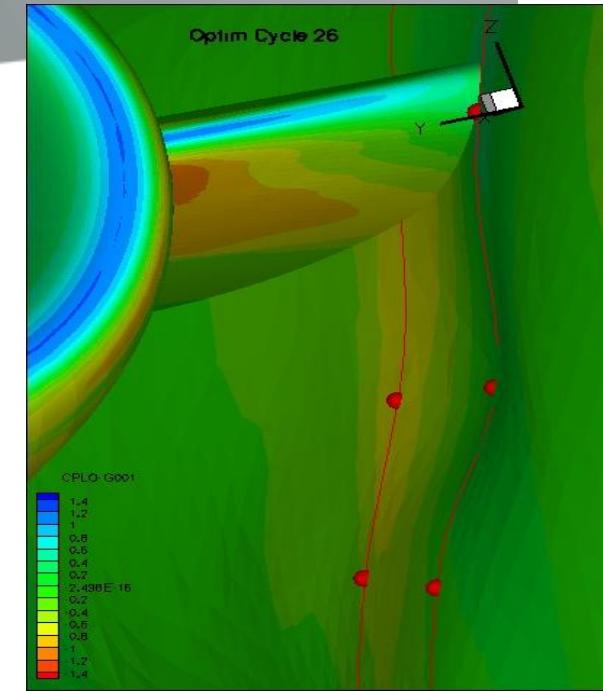
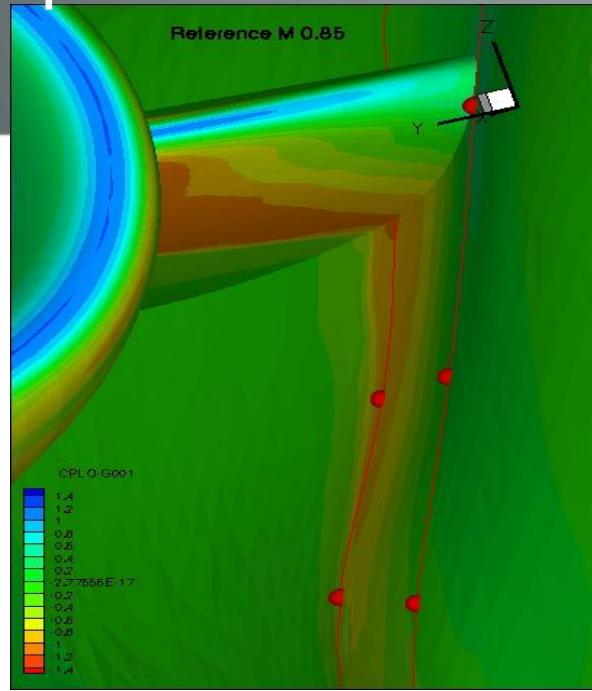
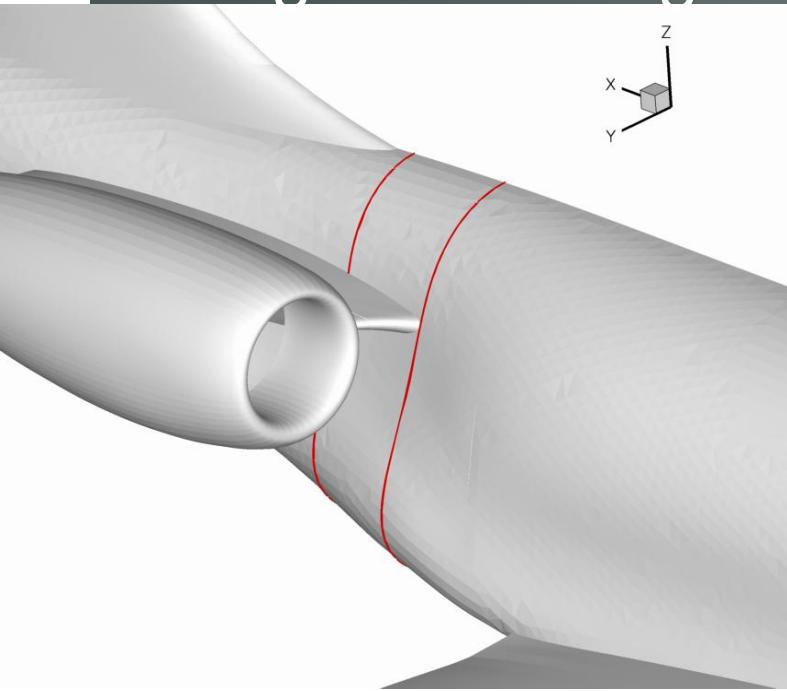
*Automatic Differentiation software Tapenade (INRIA-Sophia-Antipolis).*

*Gradient-based optimization*

*Feasible (direction) Sequential Quadratic Programming*

*Feasible Arc Interior Point Algorithm (FAIPA) developed by Prof. J.N. Herskovits & co-workers*

# Aerodynamics Optimisation: Design of fuselage shape



*Optimization based on 3D Navier-Stokes*

*Large degree of automatisation required for the design of a complex area*

*Complex aerodynamics*

*Fully 3D shape design*

*Trade off with internal layout*

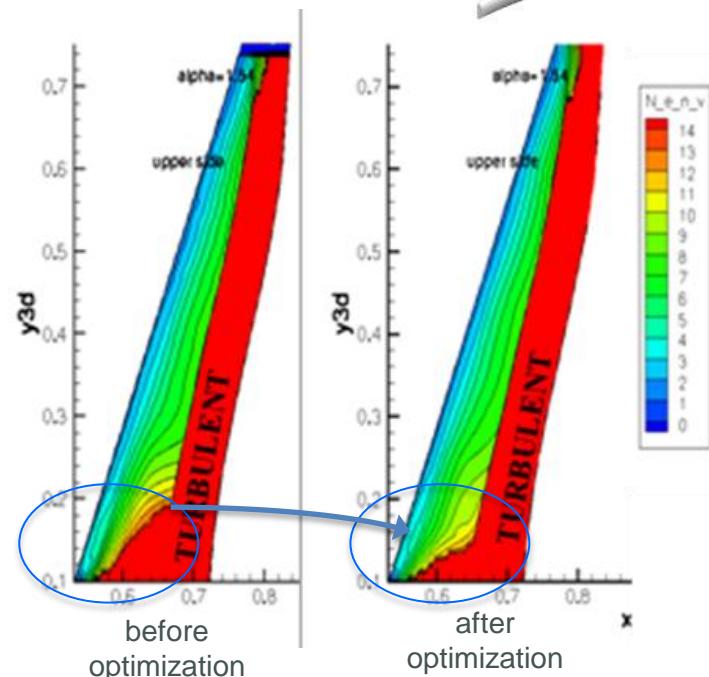
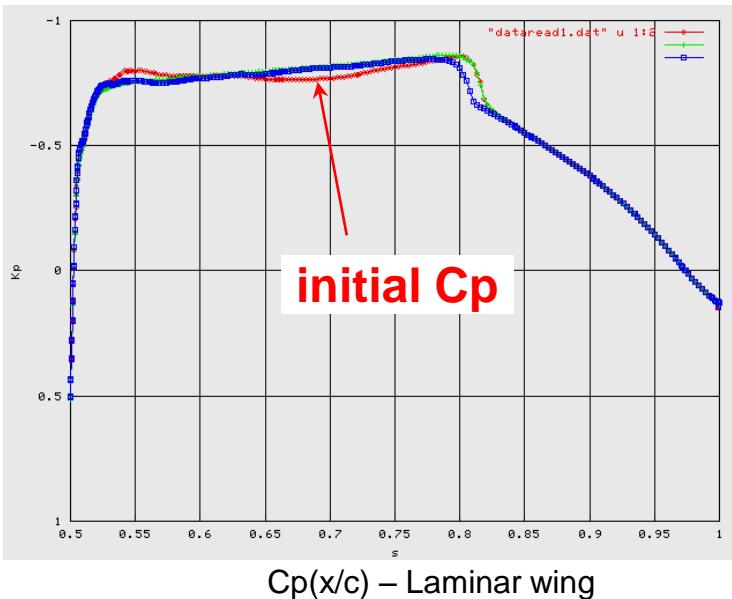
# Automatic shape optimization

(2/5)

## Laminar wing optimization to increase laminar area on wing next to the fuselage



- Laminar wing,  $\Phi = 20^\circ$
- Mach = 0.75, angle of attack= 3°
- Objective : increase laminar area on wing next to the fuselage →  $C_p$  &  $\delta C_p / \delta x$  target locally
- Leeward wing section profile
- Navier-Stokes with adjoint



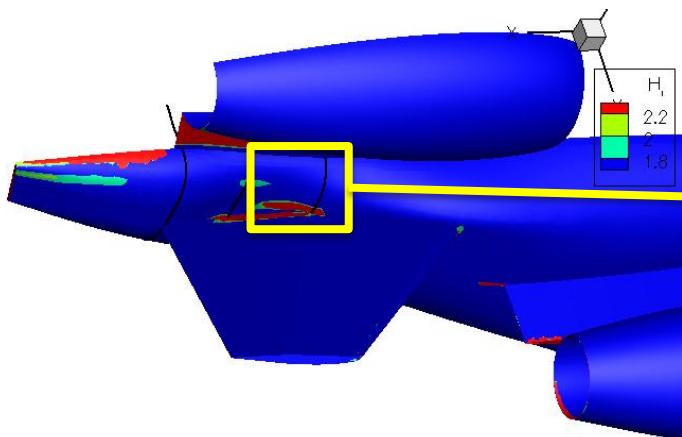
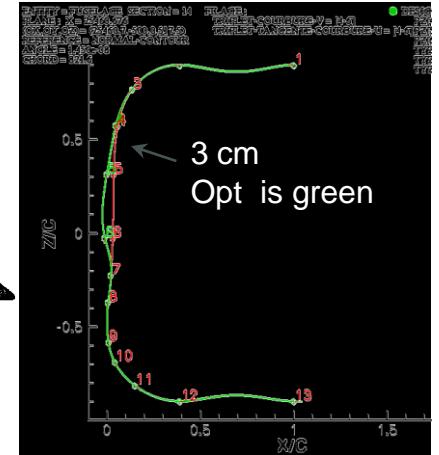
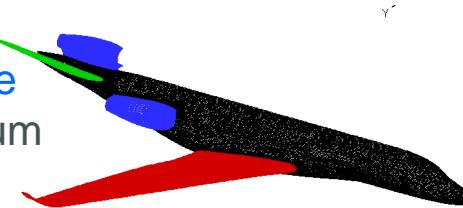
# Automatic shape optimization (3/5)

## Afterbody optimization of innovative configuration

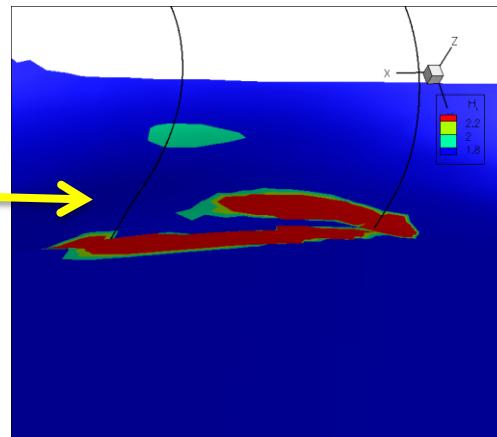
### Example of complex objective functions



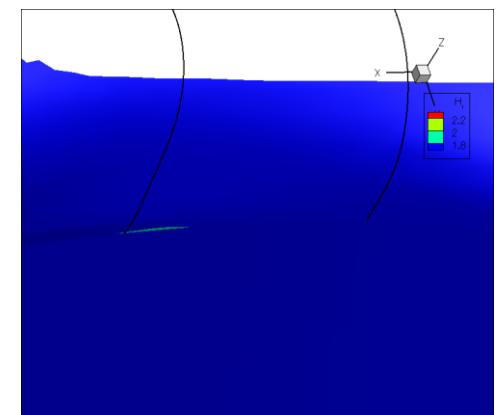
- Mach = 0.85, angle of attack = 1.5°
- Cost function is based on the boundary layer shape parameter  $H_i$  (ratio of displacement and momentum thickness)
- fuselage shape: 10 variables
- Adjoint approach - Convergence requires about 20 NS computations



Recirculation zone ( $H_i > 2.2$ ) red

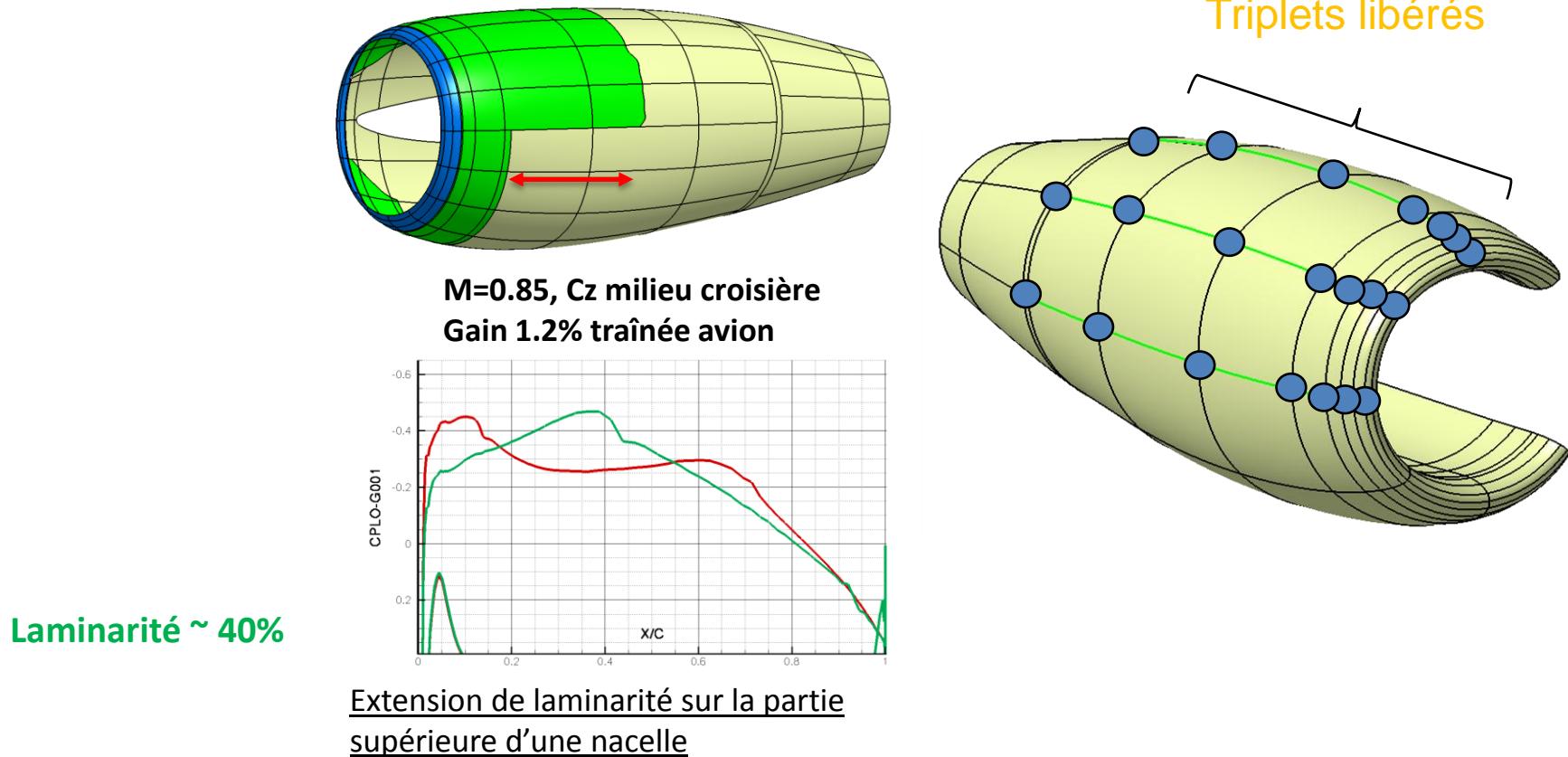


$H_i$  before optimization



$H_i$  after optimization

# Optimisation nacelle laminaire

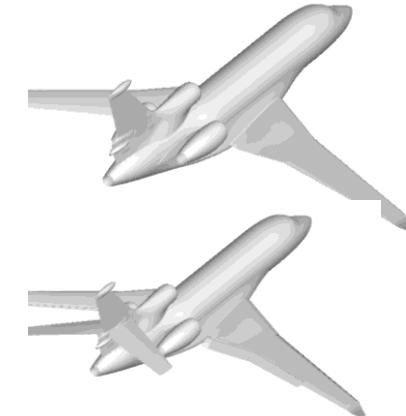


# Automatic shape optimization (4/5)

## Low speed – high speed wing tip optimization



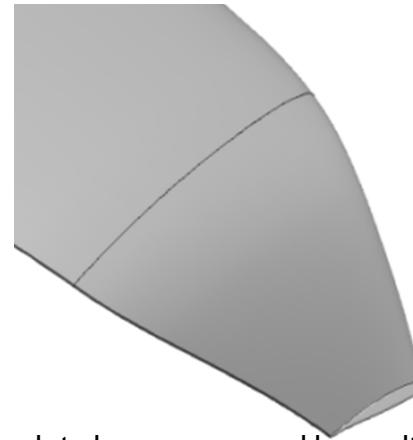
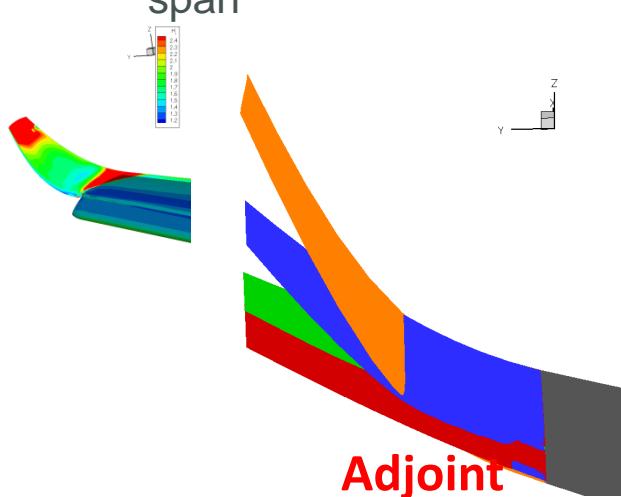
Multipoint optimization : low speed (Mach = 0.18, high lift configuration) – high speed (Mach = 0.8, cruise configuration)



Minimize

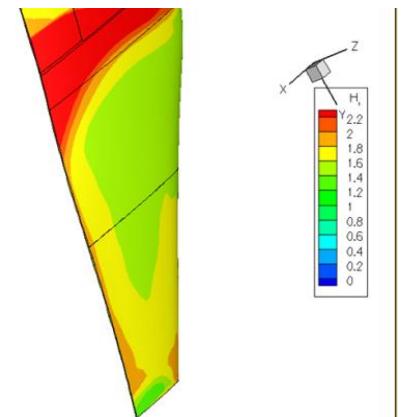
- drag at high speed (constraints on lift +trimmed+ bending moment at  $y = 8 \text{ m}$ )
- surface  $H_i > 2$  at low speed

Parameters: aoa (at High speed), twist, sweep angle, dihedral, thickness, span



winglet shape proposed by multipoint optimization

1 % reduction of drag



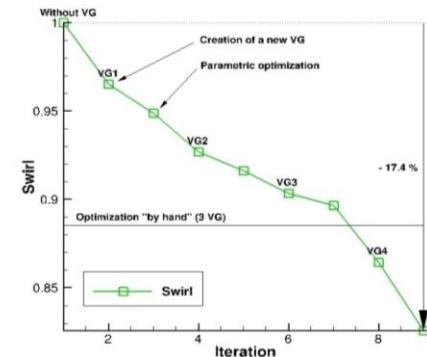
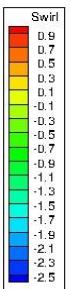
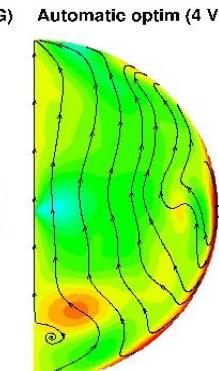
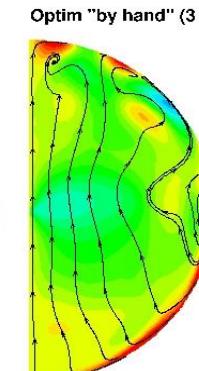
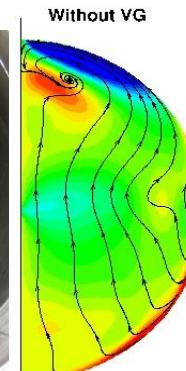
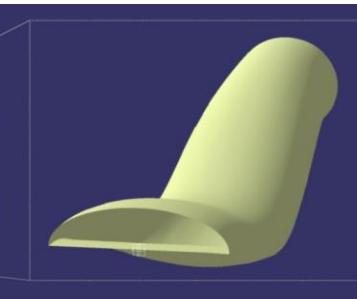
Boundary layer shape factor on the optimized winglet – high lift configuration

# Automatic shape optimization (5/5)

## Control and optimization of separated flows



- PhD thesis J. Chetboun : Dassault Aviation / Ecole Polytechnique / DGA.
- Development of automated methods for the control and the optimization of separated flows.
- Application to curved air ducts for UCAV.
- Use of mechanical or fluidic vortex generators (VG)
- Optimization: **topological + shape**

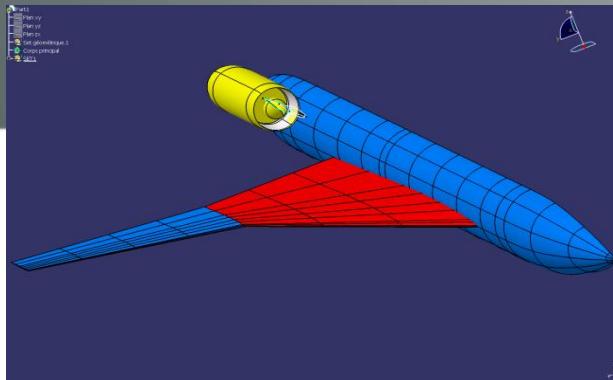


# Engine integration optimization

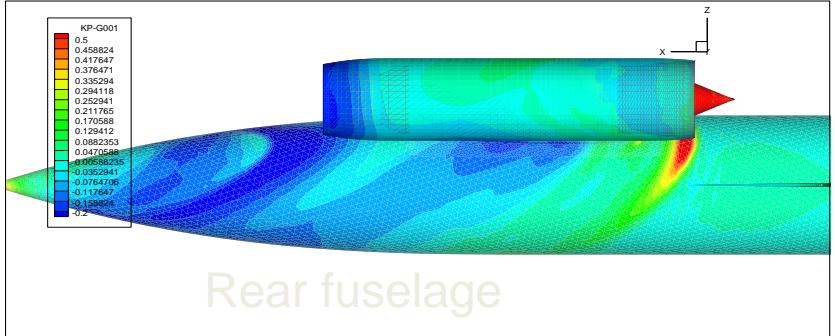
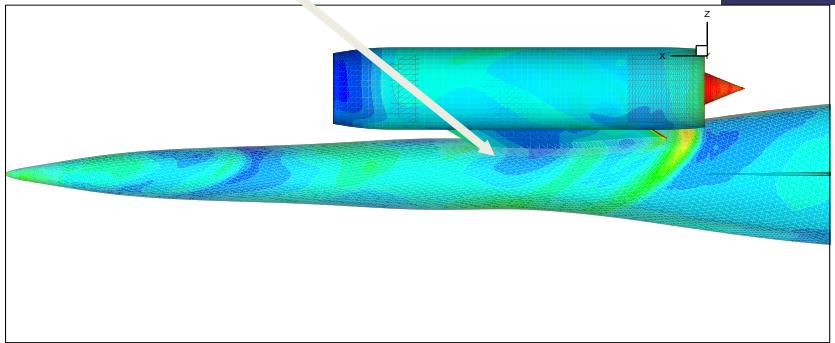


L'optimiseur ne devine pas les contraintes oubliées

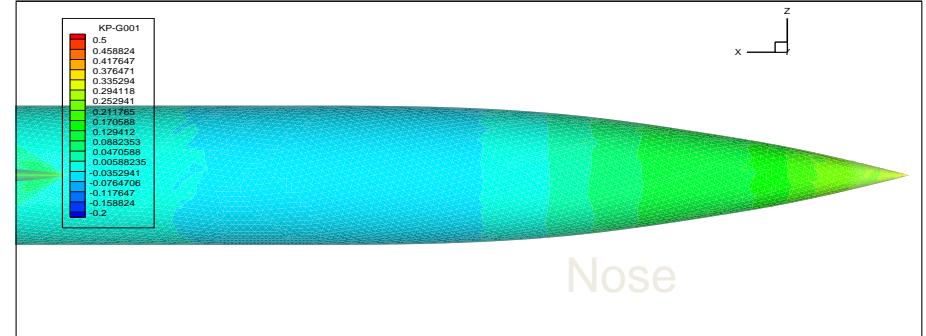
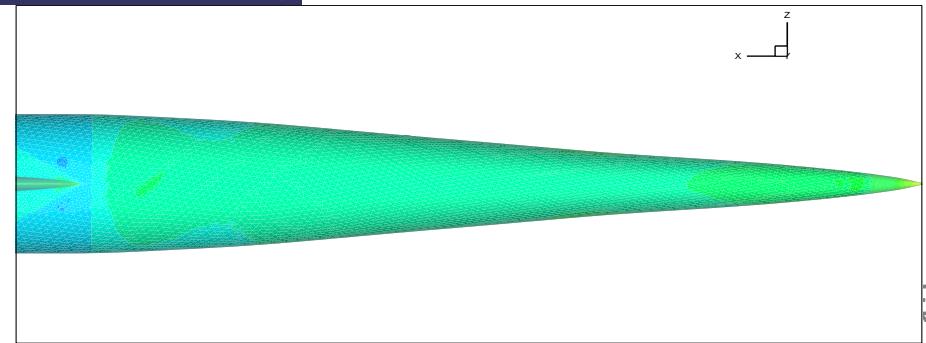
HISAC project (IP - 6th FP)



Gain: 60 %  
on zero-lift drag  
Sears-Haack ...



Rear fuselage



Nose



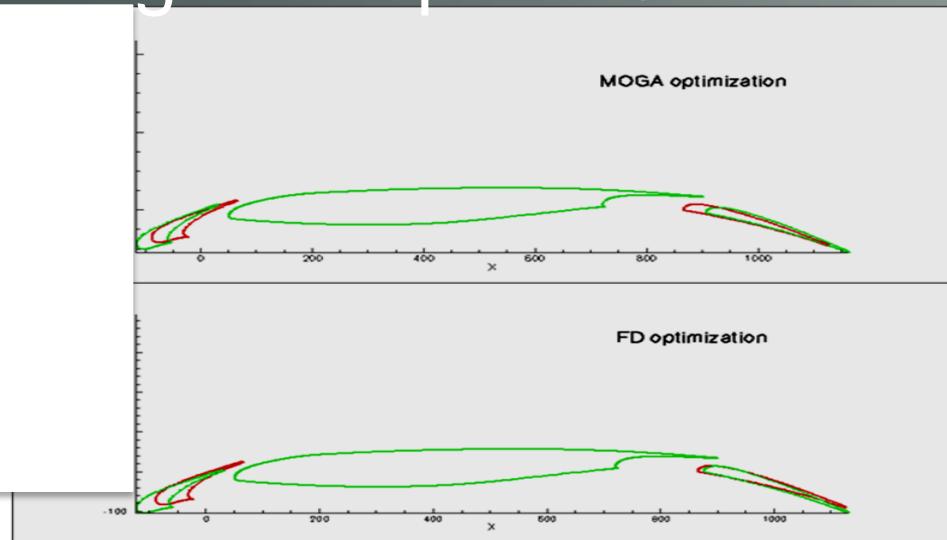
# **Optimization of High Lift configuration within European project DESIREH**

**(Design, Simulation and Flight Reynolds Number testing for advanced High Lift  
Solutions)**

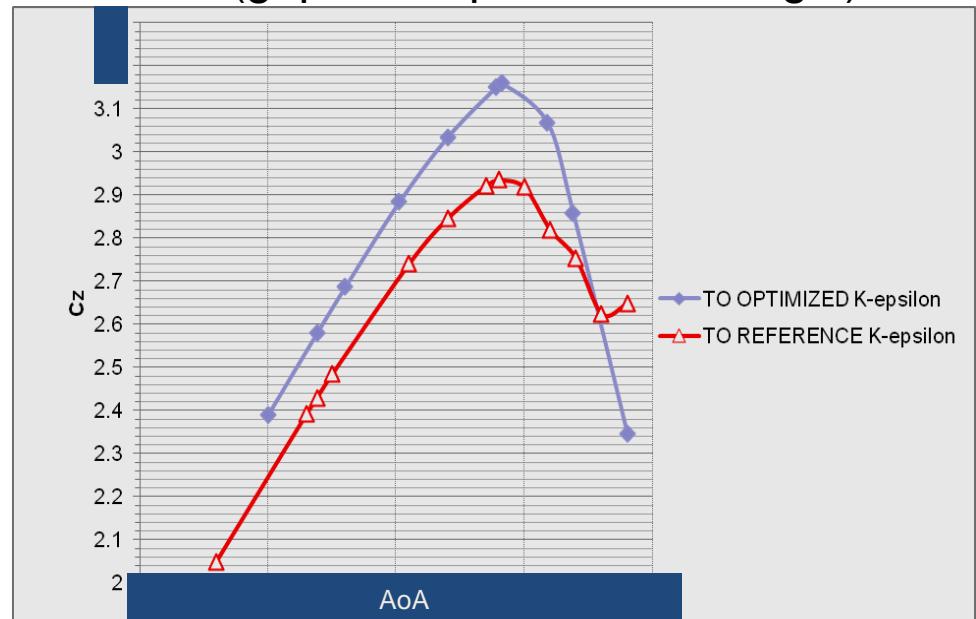
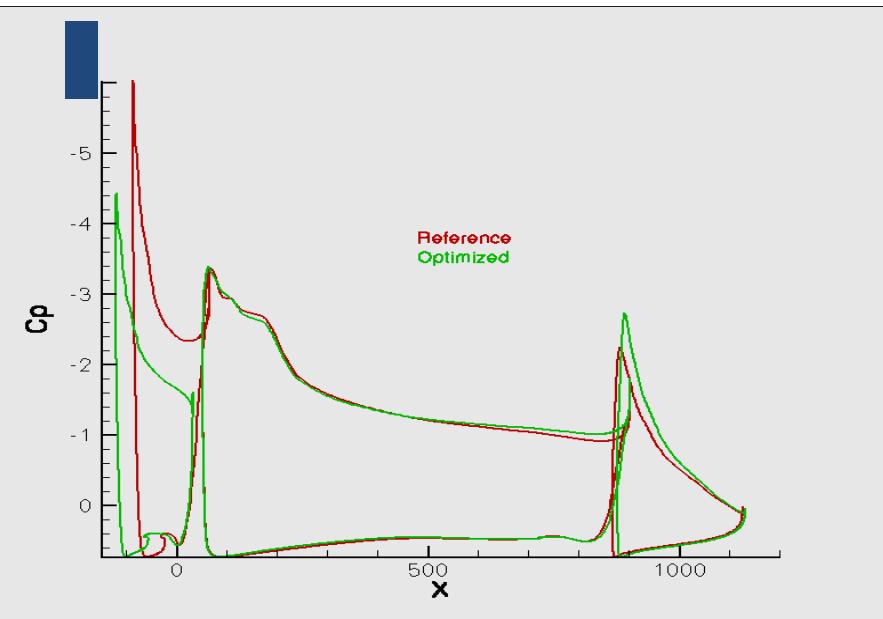
**Presentation with kind permission of activities funded within Seventh Framework Programme  
EC – Grant Agreement N° ACP8-GA-2009-233607**

**Steven Kleinveld**

# 2.5D High Lift optimization

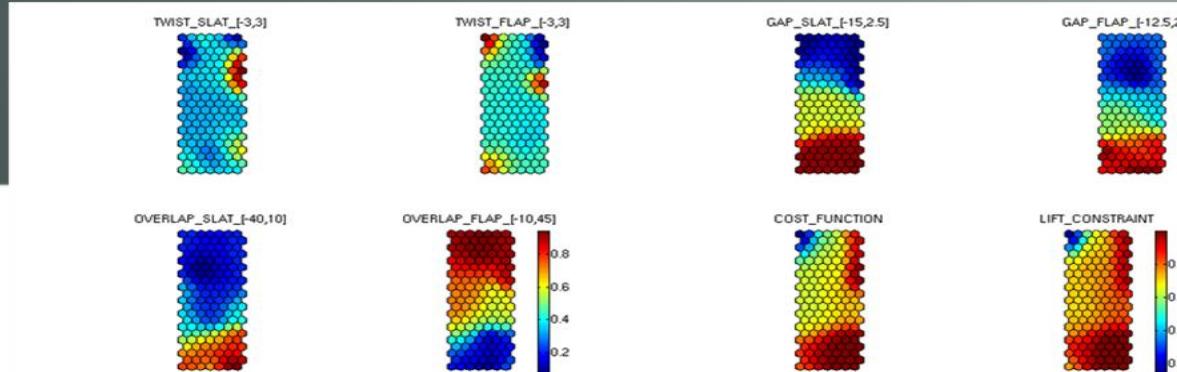


Example of performance improvement through optimization at Take-Off conditions for classical high lift configuration using setting variables (gap,overlap,deflection angle)



# 2.5D High Lift optimization

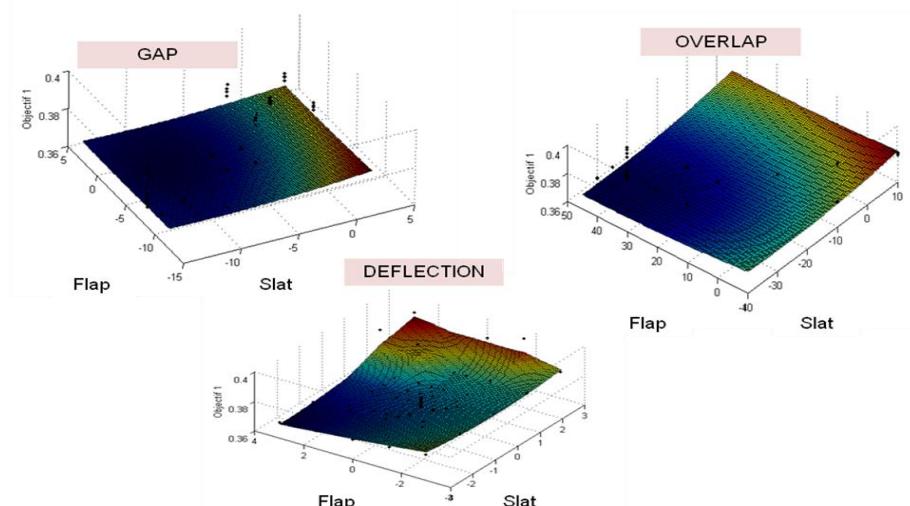
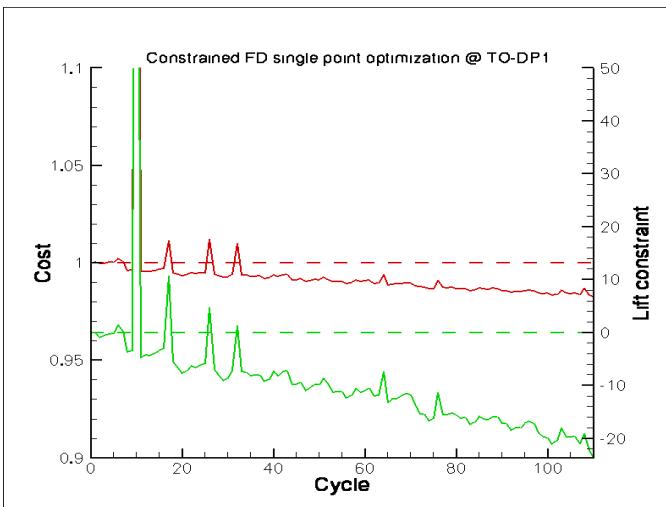
SOM



Use of various techniques to search for improved performance at take-off and landing

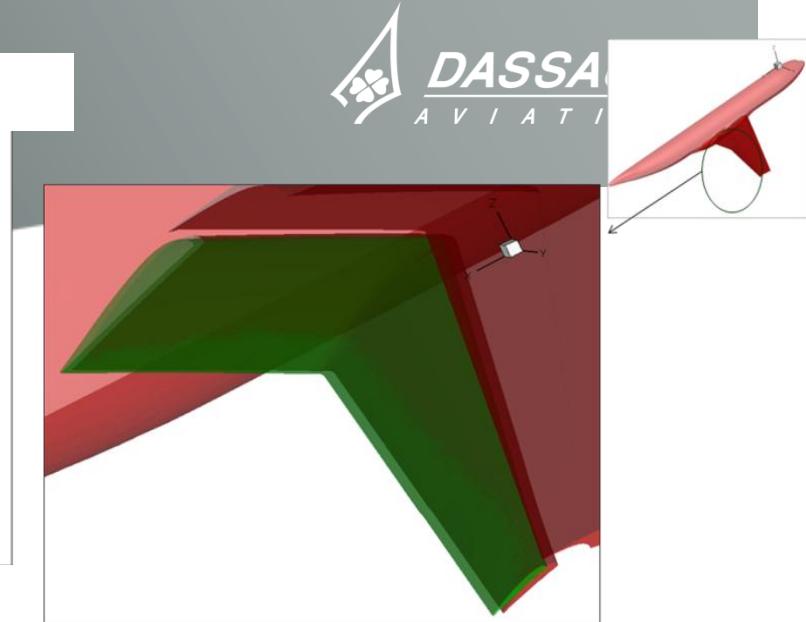
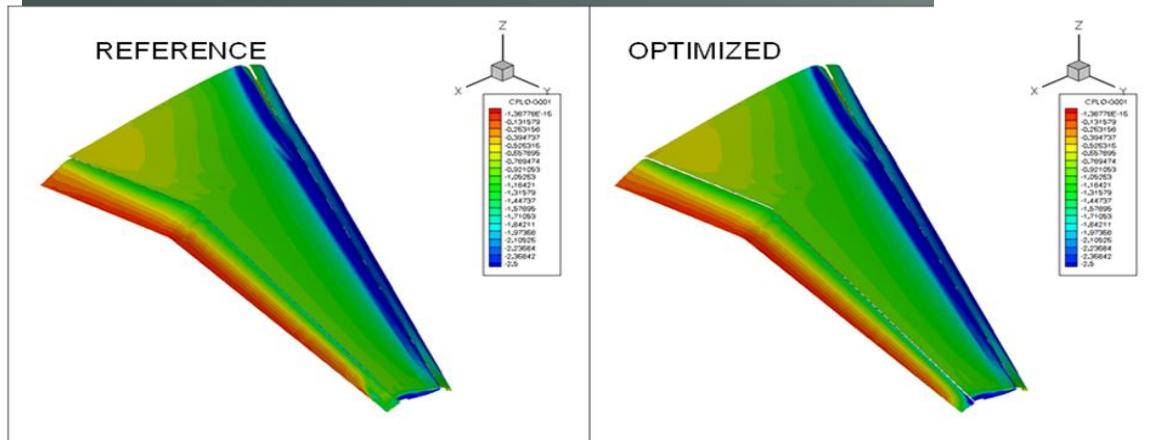
FD

$$\begin{aligned} \text{Cost Function } F(x) &= F_{\text{reference}}(x) \quad [=1] \\ \text{Lift Constraint } g(x) &= 0 \quad [=1] \end{aligned}$$

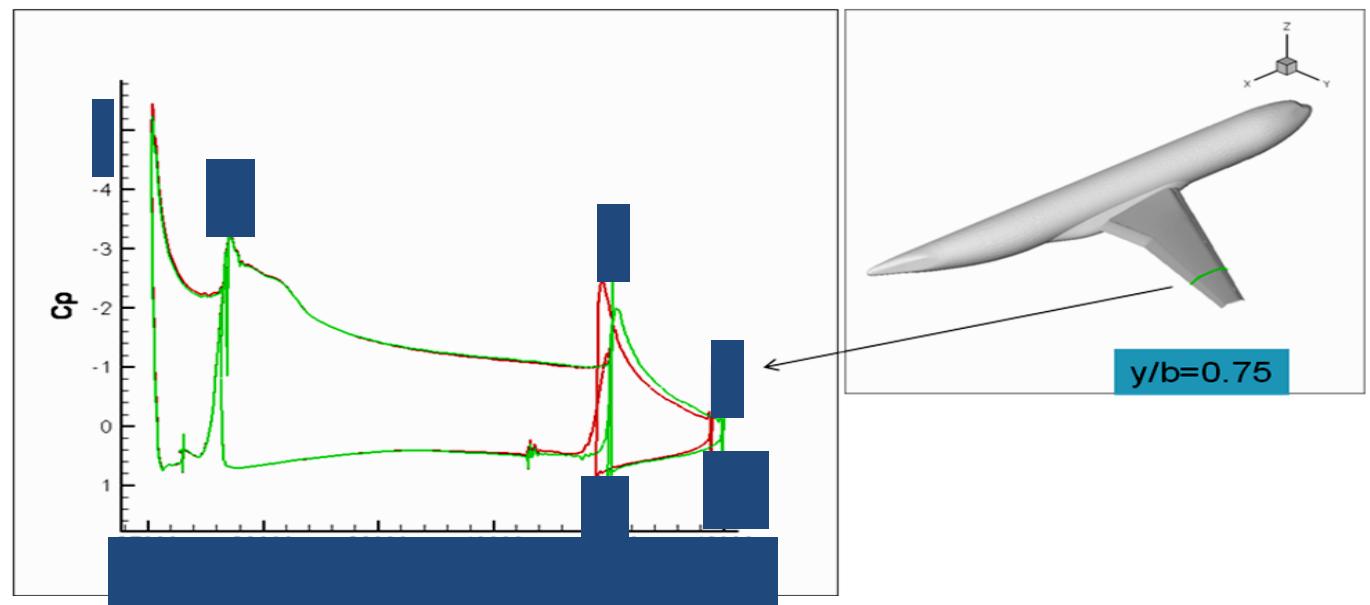


MOGA

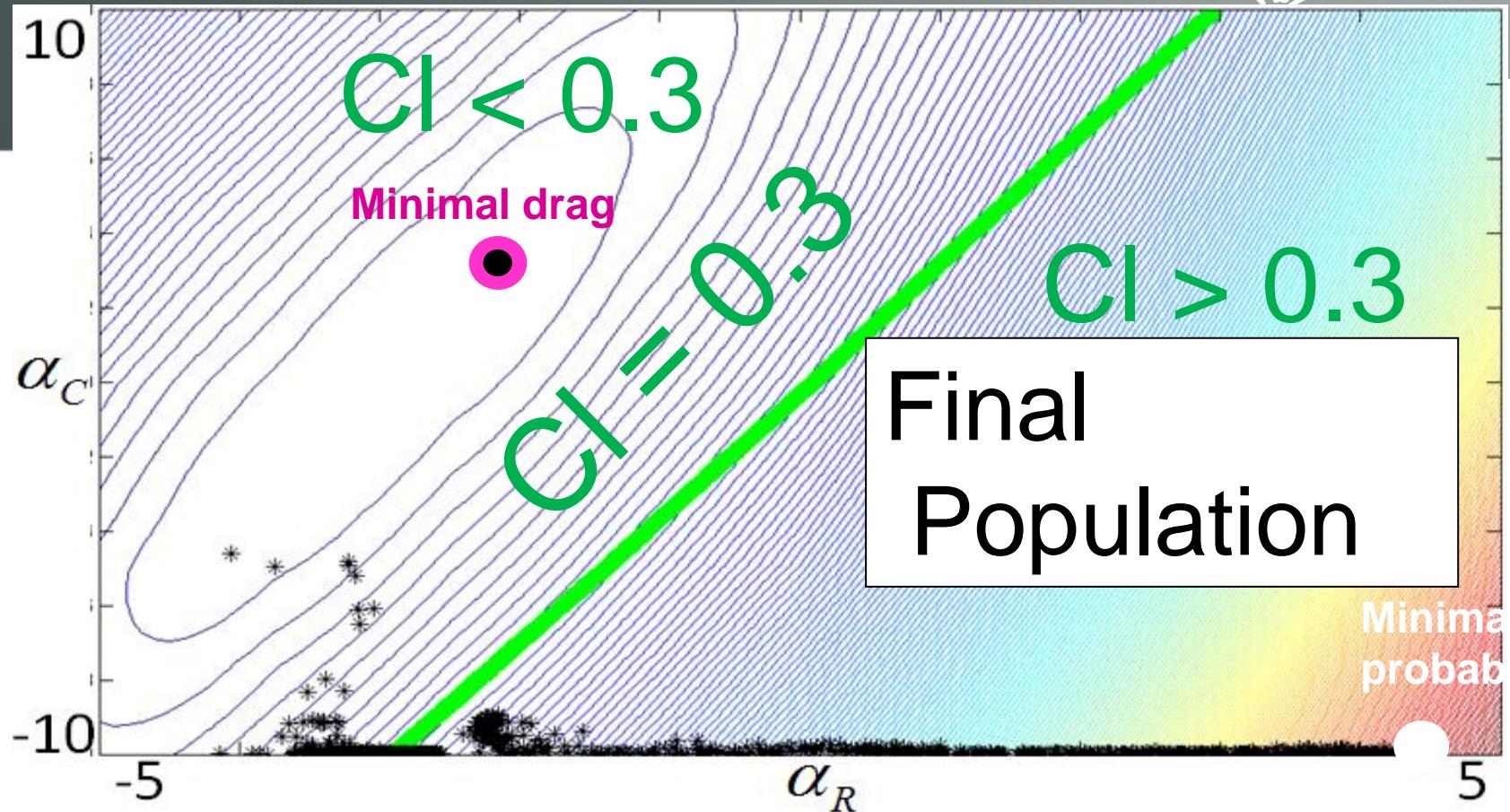
# 3D High Lift optimization



Example of flap position optimization at Take-Off conditions of 3D configuration taking into account variations of the intersection with fuselage



# Robust Design (1)

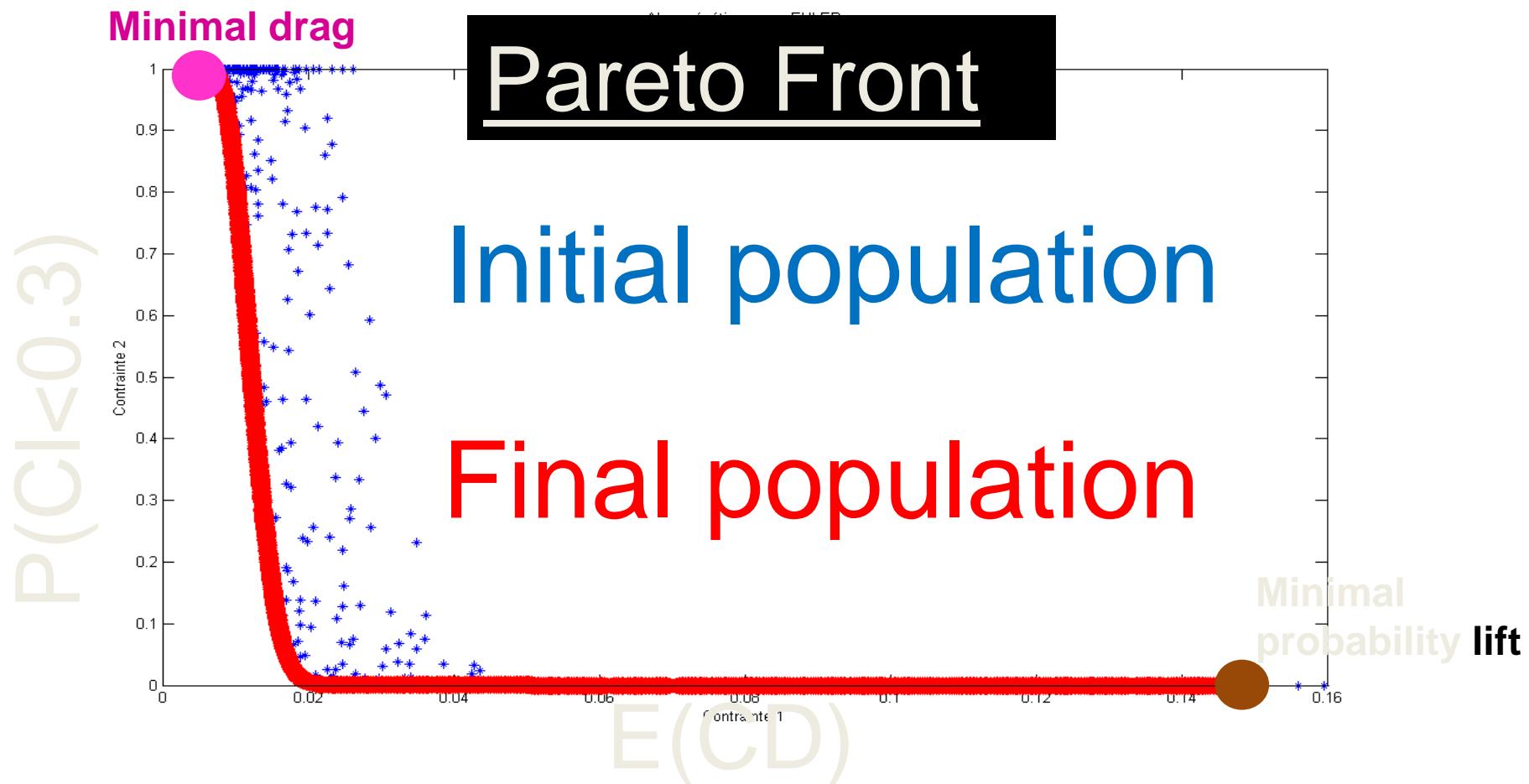


ONERA M6 wing, 2 design parameters: twist and TE camber angles

Euler, RSM RBF like but with 1rst and 2nd derivatives (original approach, Duchon extension)

MOGA, Robust design. Objectives: to control Drag and P(CL<0.3)

# Robust Design (2)

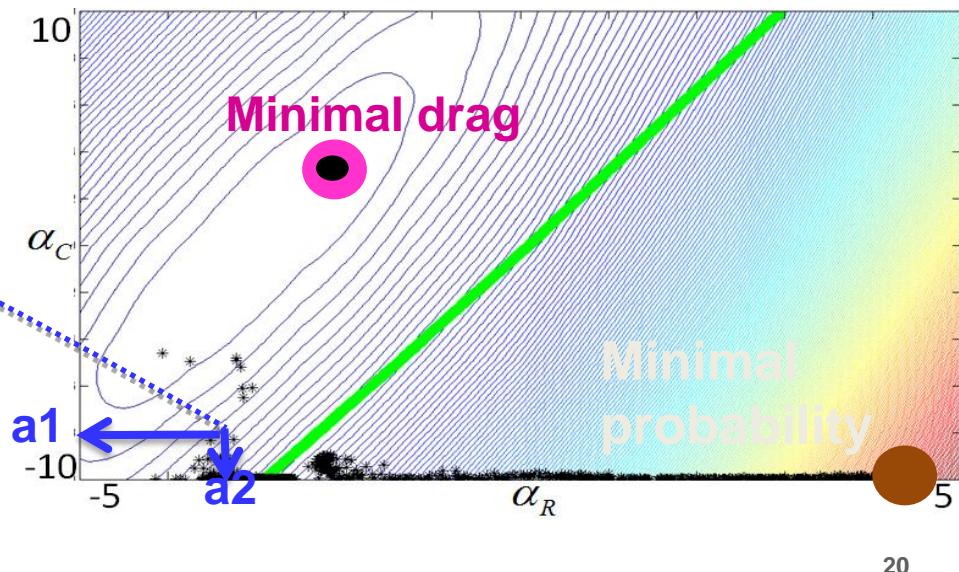
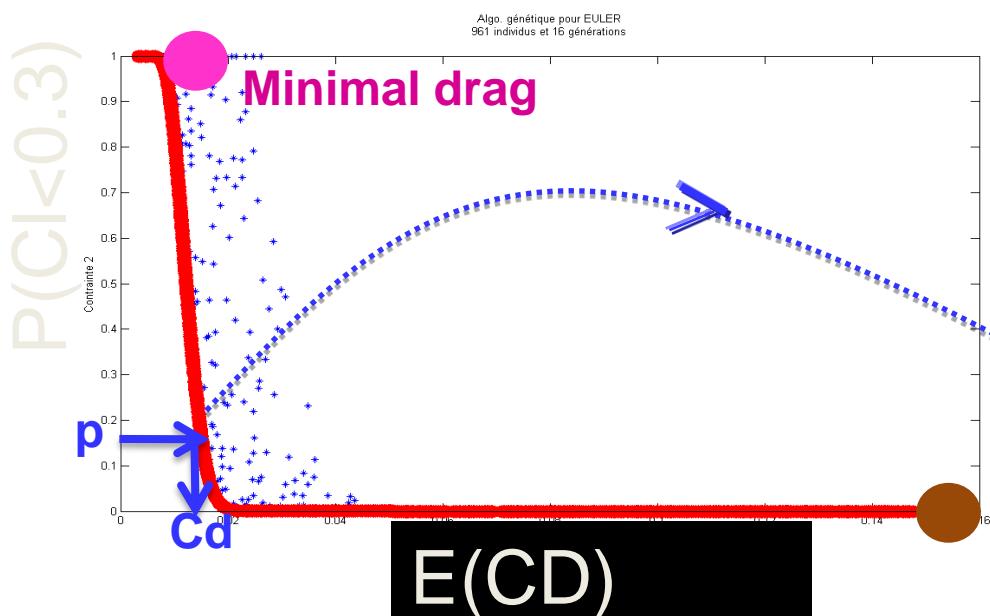


# Robust Design (3)



**Decision:** we accept a probability lift of  $p = x\%$  with minimal drag

- Determination of drag mean **CD** (Pareto front)
- Determination of nominal values of geometrical parameters **a1** and **a2** (camber and twist angles)

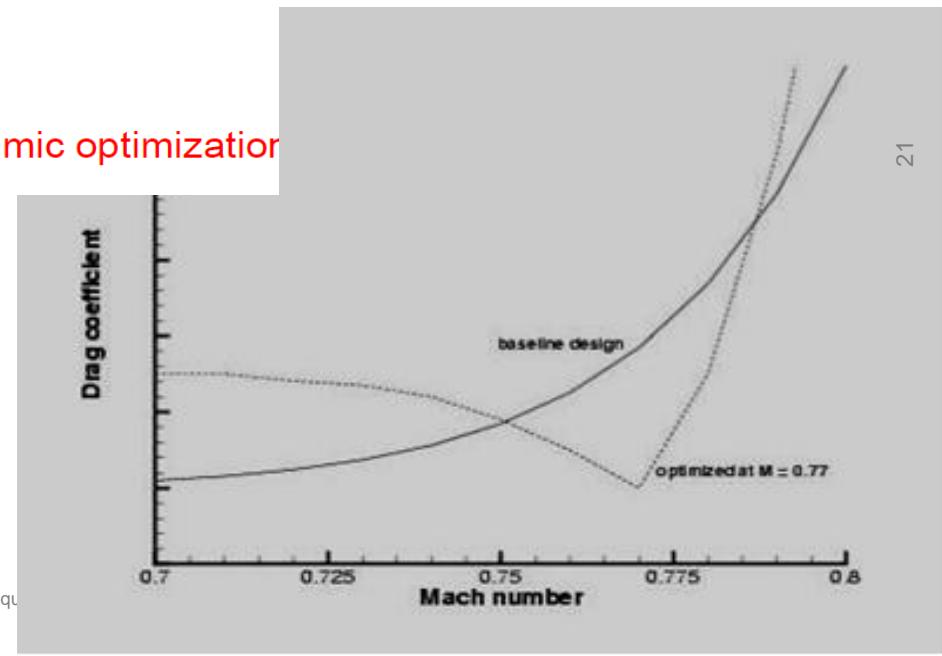
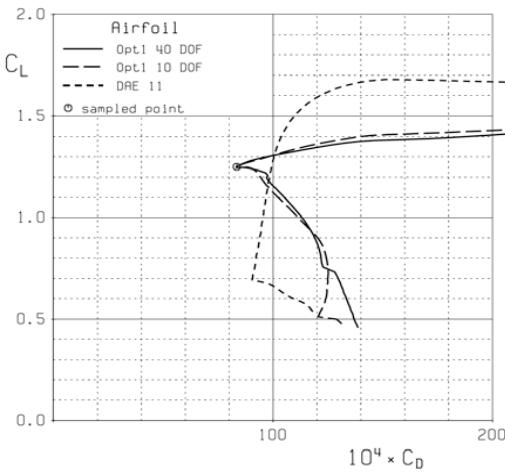


# Robustesse – optimisation multipoints

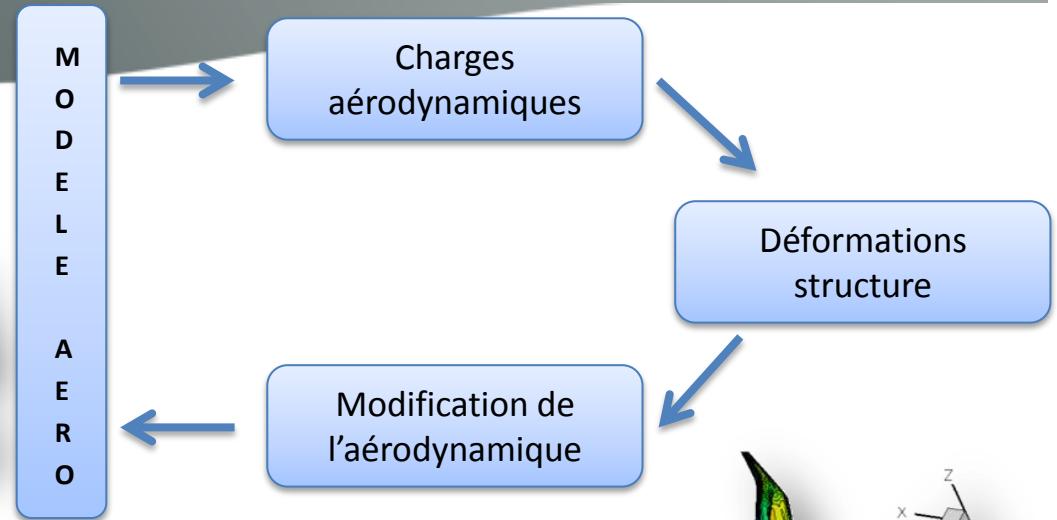
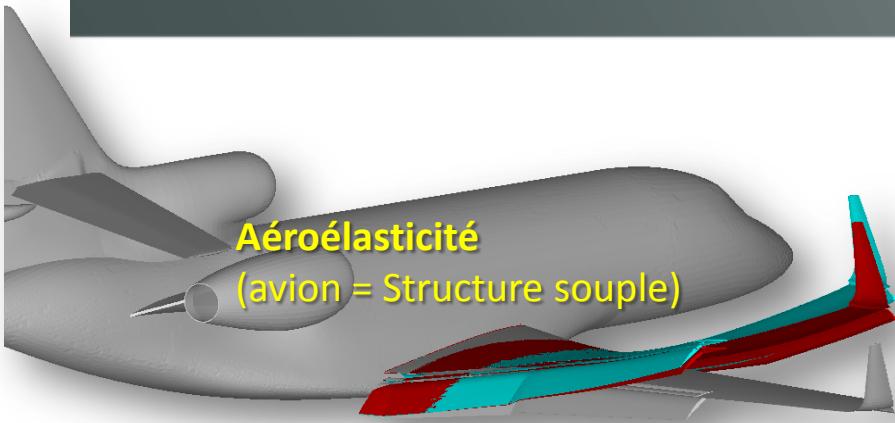
Need for a multi-mission approach

- The aircraft flies **multiple missions**, which implies
  - Multiple Mach numbers
  - Multiple Reynolds numbers
  - Large mass variations and then Cl variations
- At the aerodynamic design phase, missions are not precisely known
- We know at this step the expected lift, Mach and Reynolds variation ranges

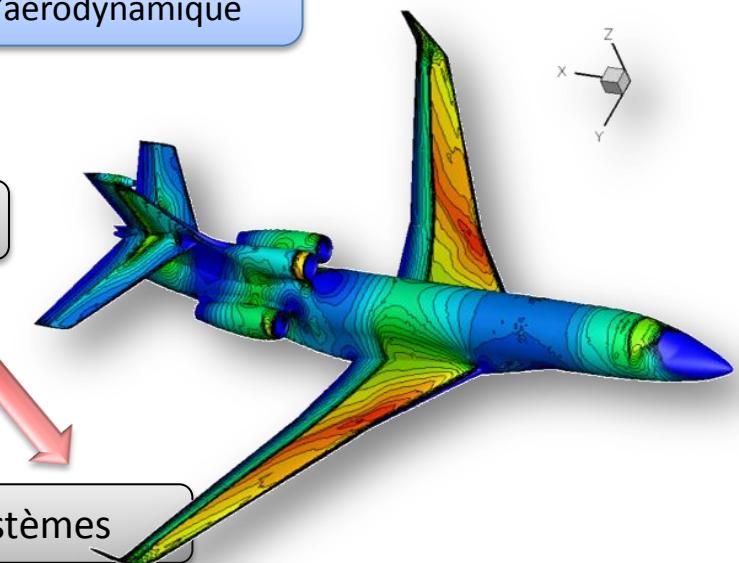
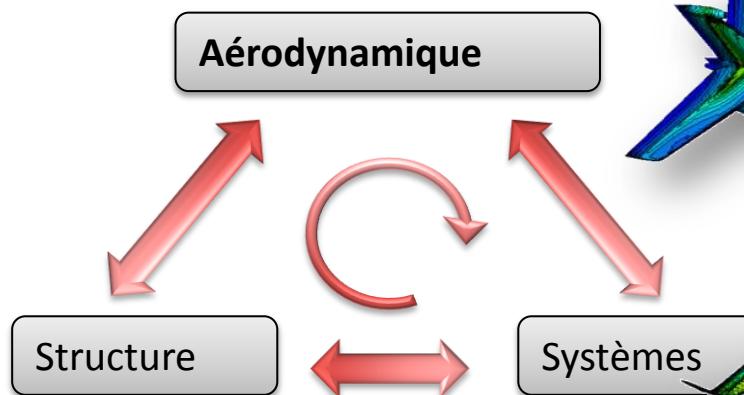
Need for a multi-lift, multi-Mach, multi-Reynolds aerodynamic optimization



# Un domaine en interaction avec les autres disciplines



**Boucle de conception**



# Analyse / Optimisation



Euler, Navier-Stokes,  
Maxwell,  
élastodynamique

Couplage fluide-structure  
(aéroelasticité),  
aéroacoustique, ...

.....

Analyse  
Monodisciplinaire

Analyse avec  
couplage entre 2  
disciplines

Analyse  
Multidisciplinaire  
(MDA)

Optimisation  
Monodisciplinaire

Optimisation avec  
couplage entre 2  
disciplines

Optimisation  
Multidisciplinaire  
(MDO)

