

Summer School CEA-EDF-INRIA

Toward petaflop numerical simulation
on parallel hybrid architectures

INRIA CENTRE DE RECHERCHE
SOPHIA ANTIPOLIS, FRANCE

Wavelet-Based DFT calculations on Massively Parallel Hybrid Architectures

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L_Sim – CEA Grenoble

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1 Review of Atomistic Simulations

- Density Functional Theory
- Ab initio codes

2 The BigDFT project

- Formalism and properties
- The needs for hybrid DFT codes
- Main operations, parallelisation

3 Performance evaluation

- Evaluating GPU gain
- Practical cases

4 Concrete examples

- Messages

Review of Atomistic Simulations



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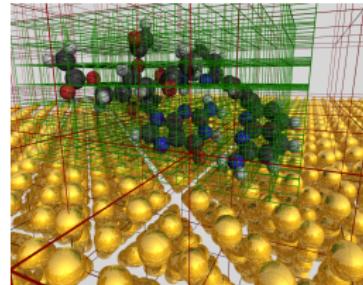
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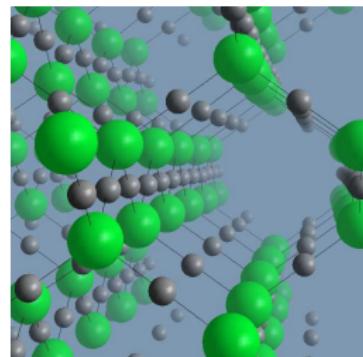
A interdisciplinary domain

- Theory – Experiment – Simulation
- Hardware – Computers
- Algorithms



Different Atomistic Simulations

- Force fields (interatomic potentials)
- Tight Binding Methods
- Hartree-Fock
- **Density Functional Theory**
- Configuration interactions
- Quantum Monte-Carlo



Can we do quantum mechanics on systems of many atoms?

Decoupling of the nuclei and electron dynamics

Born-Oppenheimer approximation:

The position of the nuclei can be considered as fixed, obtaining the potential “felt” by the electrons

$$V_{\text{ext}}(r, \{R_1, \dots, R_n\}) = - \sum_{a=1}^n \frac{Z_a}{|r - R_a|}$$

Electronic Schrödinger equation

The system properties are described by the **ground state wavefunction** $\psi(r_1, \dots, r_N)$, which solves Schrödinger equation

$$H[\{R\}] \psi = E \psi$$

The quantum hamiltonian depends on the set of the atomic positions $\{R\}$.



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Two intrinsic difficulties for numerical atomistic simulations, related to complexity:

- **Interactions** The way that atoms interact is known:

$$i\hbar \frac{\partial \Psi}{\partial t} = \mathcal{H}\Psi \quad \mathcal{H}\Psi = E_0\Psi$$

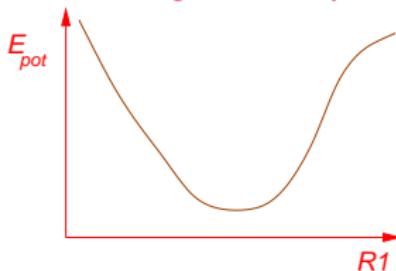
- **Exploration of the configuration space**

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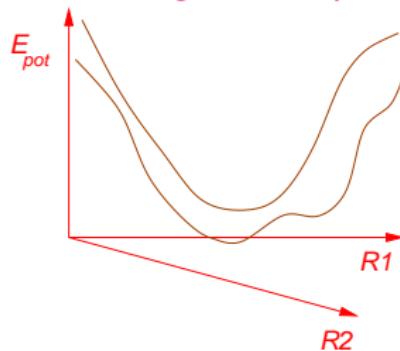


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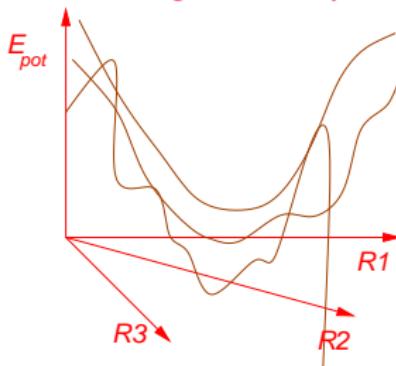


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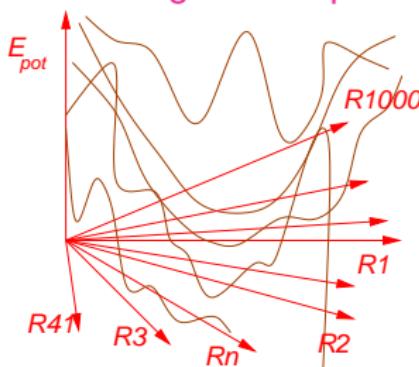


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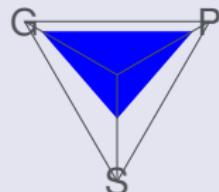
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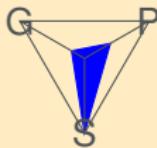
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3 criteria

- 1 → Generality (elements, alloys)
- 2 → Precision (Δr , ΔE)
- 3 → System size (N , Δt)



Chemistry and Physics



- Force Fields
- Tight Binding
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- Conf. Inter.
- Quantum Monte-Carlo

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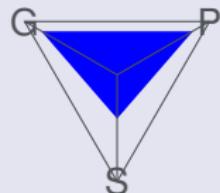
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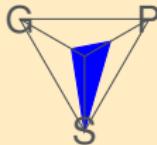
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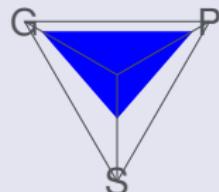
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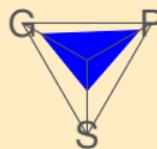
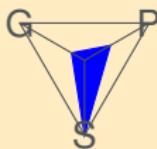
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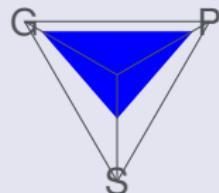
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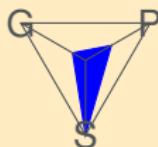
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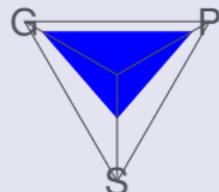
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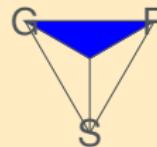
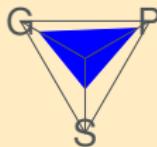
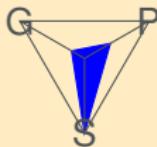
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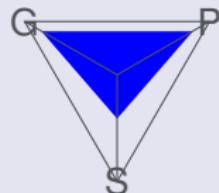
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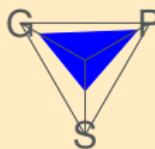
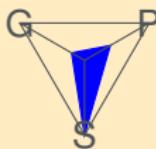
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The Hohenberg-Kohn theorem

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A tremendous numerical problem

$$H = \sum_{i=1}^N -\frac{1}{2} \nabla_{r_i}^2 + V_{\text{ext}}(r_i, \{R\}) + \frac{1}{2} \sum_{i \neq j} \frac{1}{|r_i - r_j|}$$

The Schrödinger is very difficult to solve for more than two electrons! Another approach is imperative

The fundamental variable of the problem is however **not** the wavefunction, but the **electronic density**

$$\rho(r) = N \int dr_2 \cdots dr_N \psi^*(r, r_2, \dots, r_N) \psi(r, r_2, \dots, r_N)$$

Hohenberg-Kohn theorem (1964)

The ground state density $\rho(r)$ of a many-electron system uniquely determines (up to a constant) the external potential .

The external potential is a functional of the density

$$V_{\text{ext}} = V_{\text{ext}}[\rho]$$



The Kohn-Sham approximation

Given the H-K theorem, it turns out that **the total electronic energy is an unknown functional of the density**

$$E = E[\rho] \implies \text{Density Functional Theory}$$

DFT (Kohn-Sham approach)

Mapping of a interacting many-electron system into a system with independent particles moving into an **effective** potential.

Find a set of orthonormal orbitals $\Psi_i(\mathbf{r})$ that minimizes:

$$E = -\frac{1}{2} \sum_{i=1}^{N/2} \int \Psi_i^*(\mathbf{r}) \nabla^2 \Psi_i(\mathbf{r}) d\mathbf{r} + \frac{1}{2} \int \rho(\mathbf{r}) V_H(\mathbf{r}) d\mathbf{r} \\ + E_{xc}[\rho(\mathbf{r})] + \int V_{ext}(\mathbf{r}) \rho(\mathbf{r}) d\mathbf{r}$$

$$\rho(\mathbf{r}) = 2 \sum_{i=1}^{N/2} \Psi_i^*(\mathbf{r}) \Psi_i(\mathbf{r}) \quad \nabla^2 V_H(\mathbf{r}) = -4\pi\rho(\mathbf{r})$$



Ab initio calculations with DFT

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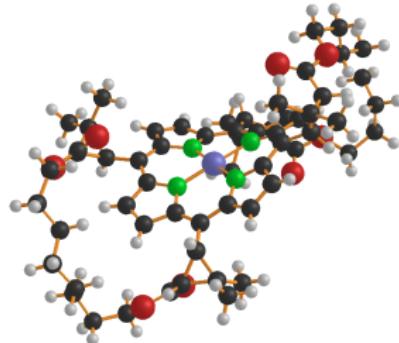
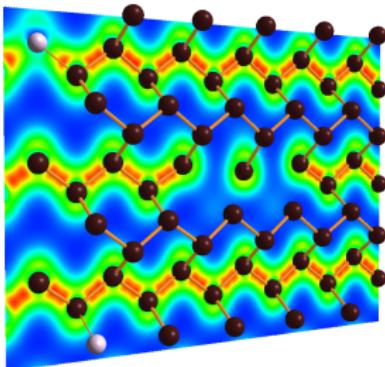
Several advantages

- ✓ **Ab initio:** No adjustable parameters
- ✓ **DFT:** Quantum mechanical (fundamental) treatment

Main limitations

- ✗ Approximated approach
- ✗ Requires high computer power, limited to few hundreds atoms in most cases

Wide range of applications: nanoscience, biology, materials



Performing a DFT calculation



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A self-consistent equation

Then $\rho = 2 \sum_i \langle \psi_i | \psi_i \rangle$, where $|\psi_i\rangle$ satisfies

$$\left(\frac{1}{2} \nabla^2 + V_H[\rho] + V_{xc}[\rho] + V_{ext} + V_{pseudo} \right) |\psi_i\rangle = \sum_j \Lambda_{i,j} |\psi_j\rangle ,$$

Now in practice: implementing a DFT code

(Kohn-Sham) DFT “Ingredients”

- An XC potential, functional of the density
several approximations exists (LDA,GGA,...)
- A choice of the pseudopotential (if not all-electrons)
(norm conserving, ultrasoft, PAW,...)
- An (iterative) algorithm for finding the wavefunctions $|\psi_i\rangle$
- **A basis set for expressing the $|\psi_i\rangle$**
- A (good) computer...

KS Equations: Self-Consistent Field

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Set of self-consistent equations:

Hamiltonian (H)

$$\left\{ -\frac{1}{2} \frac{\hbar^2}{m_e} \nabla^2 + V_{\text{eff}} \right\} \psi_i = \varepsilon_i \psi_i$$

with an effective potential:

$$V_{\text{eff}}(r) = V_{\text{ext}}(r) + \underbrace{\int_V dr' \frac{\rho(r')}{|r - r'|}}_{\text{Hartree}} + \underbrace{\frac{\delta E_{xc}}{\delta \rho(r)}}_{\text{exchange-correlation}}$$

and:

$$\rho(r) = \sum_i f_i |\psi_i(r)|^2$$

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and:

$$\rho(r) = \sum_i f_i |\psi_i(r)|^2$$

Poisson Equation: $\Delta V_{\text{Hartree}} = \rho$

$$(\text{Laplacian: } \Delta = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2})$$

Real Mesh ($100^3 = 10^6$): $10^6 \times 10^6 = 10^{12}$ evaluations !

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$V_{\text{eff}}(r)$

$$= V_{\text{ext}}(r) +$$

$$\int_V dr' \underbrace{\frac{\rho(r')}{|r - r'|}}_{\text{Hartree}}$$

+

$$\underbrace{\frac{\delta E_{xc}}{\delta \rho(r)}}_{\text{exchange-correlation}}$$

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Real Mesh ($100^3 = 10^6$): $10^6 \times 10^6 = 10^{12}$ evaluations !

Performing a DFT calculation (KS formalism)

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Find a set of orthonormal orbitals $\Psi_i(\mathbf{r})$ that minimizes:

$$E = \sum_i \langle \Psi_i | H[\rho] | \Psi_i \rangle$$

with:

- $i = 1, \dots, N$ (one Ψ per electron)
- $\rho(\mathbf{r}) = \sum_i \Psi_i^*(\mathbf{r}) \Psi_i(\mathbf{r})$

(Kohn-Sham) DFT “Actors”

- A set of **wavefunctions** $|\Psi_i\rangle$, one for each electron
- A computational approach on a **finite basis**
 - ⇒ One **array** for each Ψ_i
 - ⇒ A set of **computational operations** on these arrays which depend on the basis set
- A (even more) good computer...

Basis sets for electronic structure calculation

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Plane Waves

ABINIT, CPMD, VASP,...

Systematic convergence.

- ✓ Accuracy increases with the number of basis elements
- ✓ Non-localised, optimal for periodic, homogeneous systems
- ✗ Non adaptive

Gaussians, Slater Orbitals

CP2K, Gaussian, AIMPRO,...

Real space localized

- ✓ Small number of basis functions for moderate accuracy
- ✓ Well suited for molecules and other open structures
- ✗ Non systematic

FFT

Robust, Easy to parallelise

Analytic functions

Kinetic and overlap matrices can be calculated analytically



List of *ab initio* Codes

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- Plane Waves

- ABINIT — Louvain-la-Neuve — <http://www.abinit.org>
- CPMD — Zurich, Lugano — <http://www.cpmd.org>
- PWSCF — Italy — <http://www.pwscf.org>
- VASP — Vienna — <http://cms.mpi.univie.ac.at/vasp>

- Gaussian

- Gaussian — <http://www.gaussian.com>
- DeMon — <http://www.demon-software.com>
- CP2K — <http://cp2k.berlios.de>

- Numerical-like basis sets

- Siesta — Madrid —
<http://www.uam.es/departamentos/ciencias/fismateriac/siesta>
- Wien2K — Vienna — <http://www.wien2k.at> (FPLAPW,
all electrons)

- Real space basis set

- ONETEP — <http://www.onetep.soton.ac.uk>
- BigDFT — http://inac.cea.fr/L_Sim/BigDFT

A basis for nanosciences: the BigDFT project

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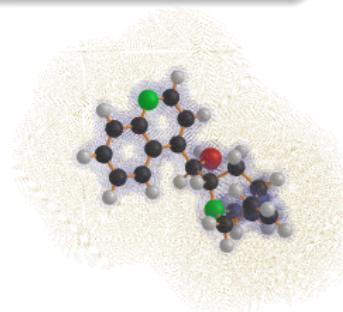
STREP European project: BigDFT(2005-2008)

Four partners, 15 contributors:

CEA-INAC Grenoble (T.Deutsch), U. Basel (S.Goedecker),
U. Louvain-la-Neuve (X.Gonze), U. Kiel (R.Schneider)

Aim: To develop an ab-initio DFT code
based on **Daubechies Wavelets**, to be
integrated in ABINIT.

BigDFT 1.0 → January 2008



... why have we done this? Was it worth it?

- Test the potential advantages of a new formalism
- A lot of outcomes and interesting results
- A lot can be done starting from present know-how

A DFT code based on Daubechies wavelets

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BigDFT: a PSP Kohn-Sham code

A Daubechies wavelets basis has unique properties for DFT usage

- Systematic, Orthogonal
- Localised, Adaptive
- Kohn-Sham operators are **analytic**

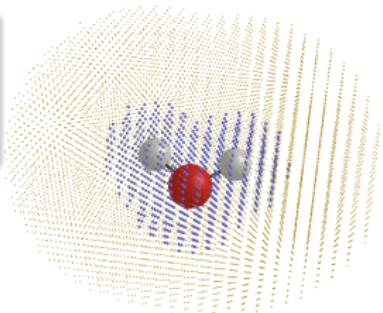
Short, Separable convolutions

$$\tilde{c}_\ell = \sum_j a_j c_{\ell-j}$$

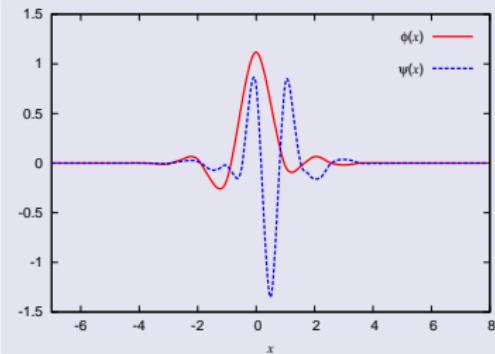
- Peculiar numerical properties

Real space based, highly flexible

Big & inhomogeneous systems



Daubechies Wavelets



Wavelet properties: multi-resolution

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Example of two resolution levels: step function (Haar Wavelet)

Scaling Functions: Multi-Resolution basis

Low and High resolution functions related each other

$$\dots \bullet \bullet \bullet \bullet \dots = \dots \bullet \bullet \bullet \bullet \bullet \bullet \bullet \bullet \dots + \dots \bullet \bullet \bullet \bullet \bullet \bullet \bullet \bullet \dots$$

Wavelets: complete the low resolution description

Defined on the same grid as the **low resolution** functions

$$\dots \bullet \bullet \bullet \bullet \bullet \bullet \bullet \dots = \frac{1}{2} \bullet \bullet \bullet \bullet \bullet \bullet \bullet \dots + \frac{1}{2} \bullet \dots$$

Scaling Function + Wavelet = High resolution

We increase the resolution without modifying the grid spacing

Wavelet properties: adaptivity

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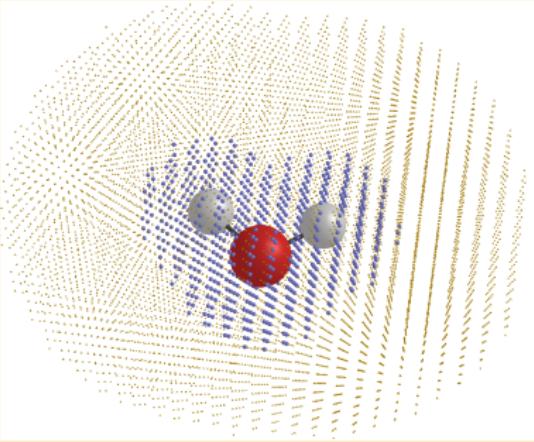
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Adaptivity

Resolution can be refined following the grid point.



The grid is divided in **Low** (1 DoF) and **High** (8 DoF) resolution points. Points of different resolution belong to **the same** grid. Empty regions must not be “filled” with basis functions.

Localization property, real space description

Optimal for **big & inhomogeneous** systems, **highly flexible**

Basis set features

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BigDFT features in a nutshell

- ✓ Arbitrary absolute **precision** can be achieved
Good convergence ratio for real-space approach ($O(h^{14})$)
- ✓ Optimal usage of the degrees of freedom (**adaptivity**)
Optimal speed for a systematic approach (**less memory**)
- ✓ Hartree potential accurate for **various boundary conditions**
Free and Surfaces BC Poisson Solver
(present also in CP2K, ABINIT, OCTOPUS)
- ✗ Data repartition is suitable for optimal scalability
Simple communications paradigm, **multi-level parallelisation** possible (and implemented)

Improve and develop know-how

Optimal for *advanced DFT functionalities in HPC framework*



BigDFT version 1.5.2: (ABINIT-related) capabilities

http://inac.cea.fr/L_Sim/BigDFT

- Isolated, surfaces and 3D-periodic boundary conditions (k-points, **symmetries**)
- All XC functionals of the ABINIT package (libXC library)
- Hybrid functionals, Fock exchange operator
- Direct Minimisation and **Mixing routines (metals)**
- Local geometry optimizations (with constraints)
- External electric fields (surfaces BC)
- Born-Oppenheimer MD, ESTF-IO
- Vibrations
- Unoccupied states
- Empirical van der Waals interactions
- Saddle point searches (NEB, Granot & Bear)
- All these functionalities are GPU-compatible

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Laboratoire de Simulation Atomistique

http://inac.cea.fr/L_Sim

Luigi Genovese

Operations performed

The SCF cycle

Orbital scheme:

- Hamiltonian
- Preconditioner

Coefficient Scheme:

- Overlap matrices
- Orthogonalisation

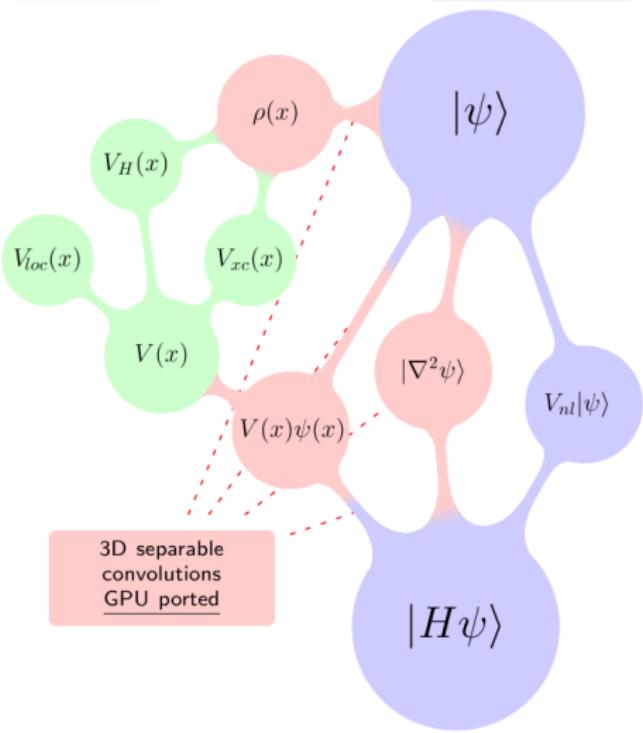
Comput. operations

- Convolutions
- BLAS routines
- FFT (Poisson Solver)

Why not GPUs?

Real Space

Daub. Wavelets



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Hybrid Supercomputing nowadays

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GPGPU on Supercomputers

- Traditional architectures are somehow saturating
More cores/node, memories (slightly) larger but not faster
- Architectures of Supercomputers are becoming hybrid
3 out to 4 Top Supercomputers are hybrid machines
- Extrapolation: In 2015, No. 500 will become petaflopptic
Likely it will be a hybrid machine

Codes should be conceived differently

- # MPI processes is limited for a fixed problem size
- Performances increase only by enhancing parallelism
- Further parallelisation levels should be added (OpenMP, GPU)

Does electronic structure calculations codes are suitable?



How far is petaflop (for DFT)?

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At present, with traditional architectures

Routinely used DFT calculations are:

- Few dozens (hundreds) of processors
 - Parallel intensive operations (blocking communications, 60-70 percent efficiency)
 - Not *freshly* optimised (legacy codes, monster codes)
- ☞ Optimistic estimation: $5 \text{ GFlop/s per core} \times 2000 \text{ cores} \times 0.9 = 9 \text{ TFlop/s} = \text{200 times less than Top 500's #1!}$

It is such as

Distance Earth-Moon = 384 Mm

Distance Earth-Mars = 78.4 Gm = **200** times more

Are we able to go to Mars? (... in 2015?)



Reliable formalism

- Systematic convergence properties
- Explicit environments, analytic operator expressions

State-of-the-art computational technology

- Data locality optimal for operator applications
- Massive parallel environments
- Material accelerators (GPU)

New physics can be approached

- Enhanced functionalities can be applied relatively easily
- Limitation of DFT approximations can be evidenced
- A formalism of interest for Post-DFT treatments

Separable convolutions

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We must calculate

$$\begin{aligned}F(l_1, l_2, l_3) &= \sum_{j_1, j_2, j_3=0}^L h_{j_1} h_{j_2} h_{j_3} G(l_1 - j_1, l_2 - j_2, l_3 - j_3) \\&= \sum_{j_1=0}^L h_{j_1} \sum_{j_2=0}^L h_{j_2} \sum_{j_3=0}^L h_{j_3} G(l_1 - j_1, l_2 - j_2, l_3 - j_3)\end{aligned}$$

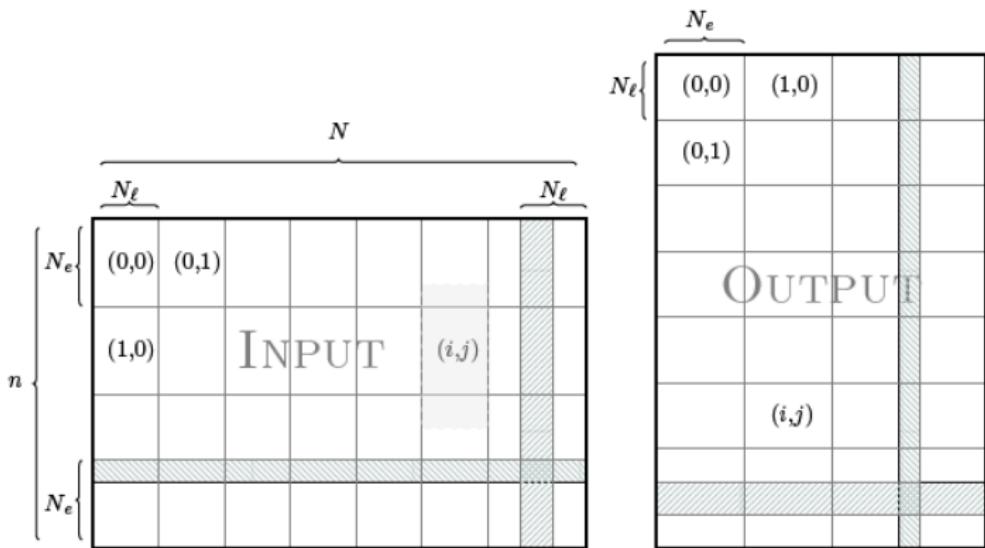
Application of three successive operations

- ① $A_3(l_3, i_1, i_2) = \sum_j h_j G(i_1, i_2, l_3 - j) \quad \forall i_1, i_2;$
- ② $A_2(l_2, l_3, i_1) = \sum_j h_j A_3(l_3, i_1, l_2 - j) \quad \forall l_3, i_1;$
- ③ $F(l_1, l_2, l_3) = \sum_j h_j A_2(l_2, l_3, l_1 - j) \quad \forall l_2, l_3.$

Main routine: Convolution + transposition

$$F(a, l) = \sum_j h_j G(a, l - j) \quad \forall a;$$

Basic Input-Output operation



From sequential to GPU

Same operation schedule for monocore, multithread, GPU

➡ Can be treated as a library

CPU performances of the convolutions

Initially, naive FORTRAN routines

$$y(j, l) = \sum_{\ell=L}^U h_\ell x(l + \ell, j)$$

- Easy to write and debug
- Test the formalism
- Define reference results

```
do j=1,ndat  
do i=0,n1  
tt=0.d0  
do l=lowfil,lupfil  
tt=tt+x(i+l,j)*h(l)  
enddo  
y(j,i)=tt  
enddo  
enddo
```

Optimisation can then start

(Ex. X5550, 2.67 GHz)

Method	GFlop/s	% of peak	SpeedUp
Naive (FORTRAN)	0.54	5.1	1/(6.25)
Current (FORTRAN)	3.3	31	1
Best (C, SSE)	7.8	73	2.3

How to optimize?

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A trade-off between benefit and effort

FORTRAN based

- ✓ Relatively accessible (loop unrolling)
- ✓ Moderate optimisation can be achieved relatively fast
- ✗ Compilers fail to use vector engine efficiently

Push optimisation at the best

- Only one out of 3 convolution type has been implemented
- About 20 different patterns have been studied for one 1D convolution
- Tedious work, huge code → Maintainability?

👉 Automatic code generation under study



MPI parallelization I: Orbital distribution scheme



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Used for the application of the hamiltonian

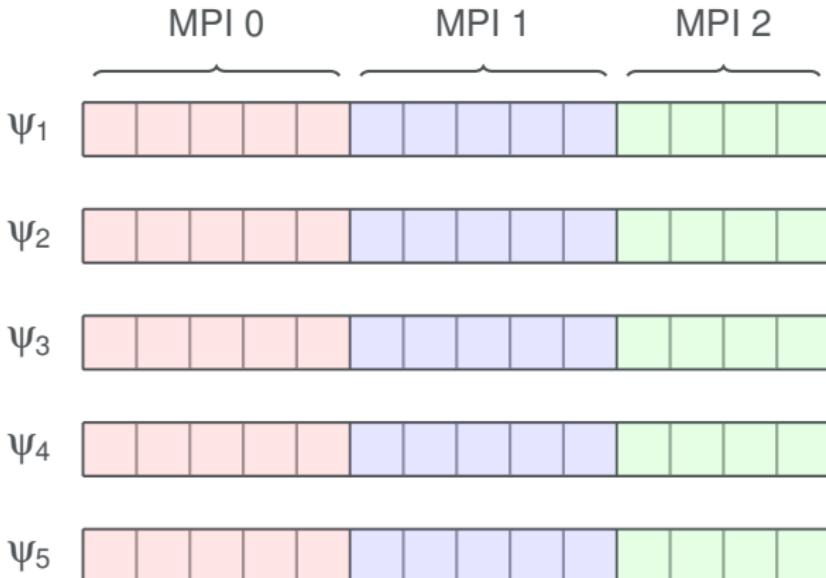
Operator approach: The hamiltonian (**convolutions**) is applied separately onto each wavefunction



MPI parallelization II: Coefficient distribution scheme

Used for scalar products & orthonormalisation

BLAS routines (level 3) are called, then result is reduced



At present, MPI_ALLTOALL(V) is used to switch

OpenMP parallelisation

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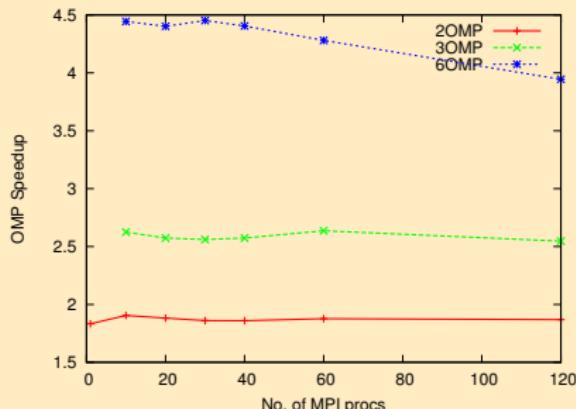
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Innermost parallelisation level

(Almost) Any BigDFT operation is parallelised via OpenMP

- ✓ Useful for memory demanding calculations
- ✓ Allows further increase of speedups
- ✓ Saves MPI processes and intra-node Message Passing
- ✗ Less efficient than MPI
- ✗ Compiler and system dependent
- ✗ OMP sections should be regularly maintained



Task repartition for a small system (ZnO, 128 atoms)

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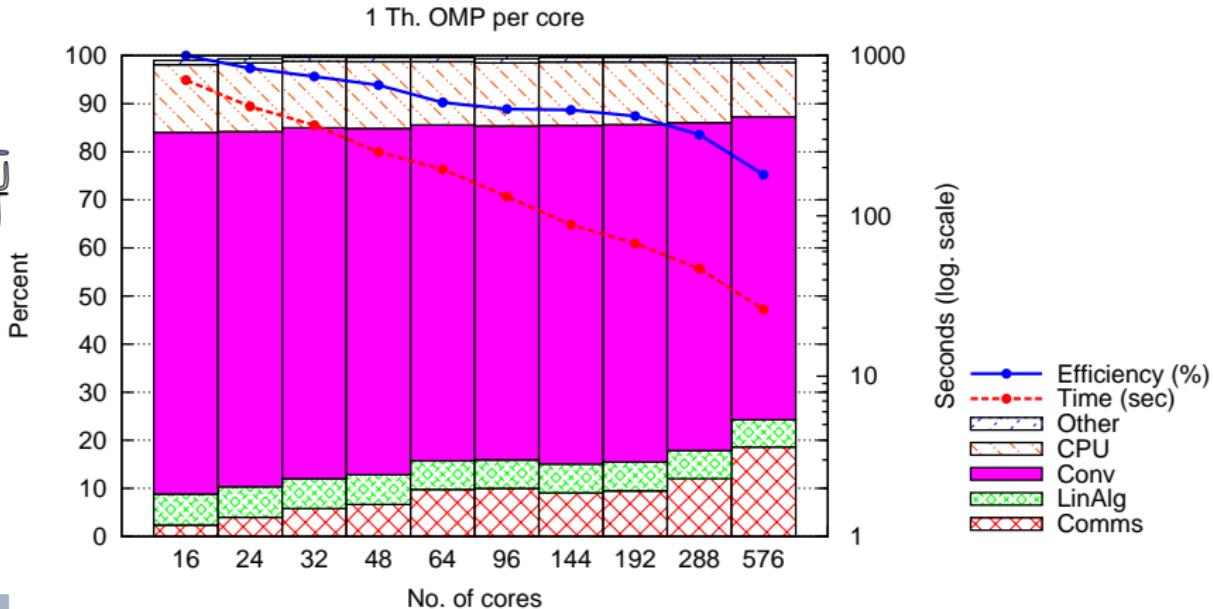
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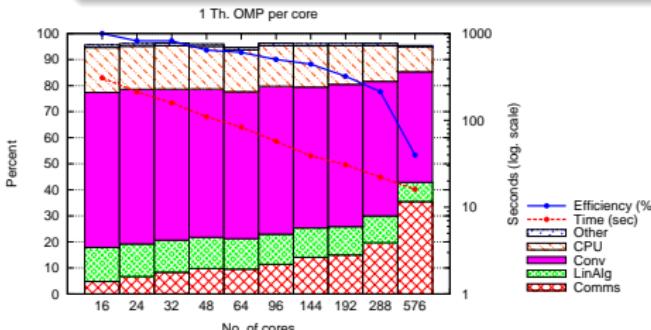
What are the ideal conditions for GPU

GPU-ported routines should take the majority of the time

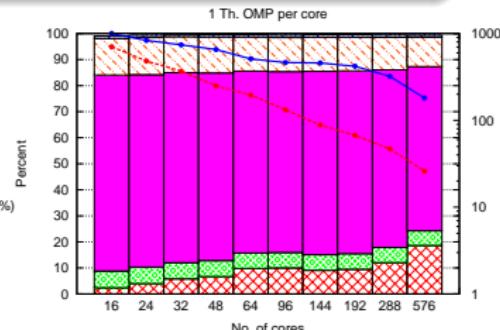
What happens to parallel efficiency?

Parallelisation and architectures

Same code, same runs. Which is the best?



CCRT Titane (Nehalem, Infiniband)



CSCS Rosa (Opteron, Cray XT5)

Titane is 2.3 to 1.6 times faster than Rosa!

Degradation of parallel performances: why?

- ① Calculation power has increased more than networking
- ② Better libraries (MKL)
- ③ Walltime reduced, but lower parallel efficiency

This will always happen while using GPU!

Architectures, libraries, networking

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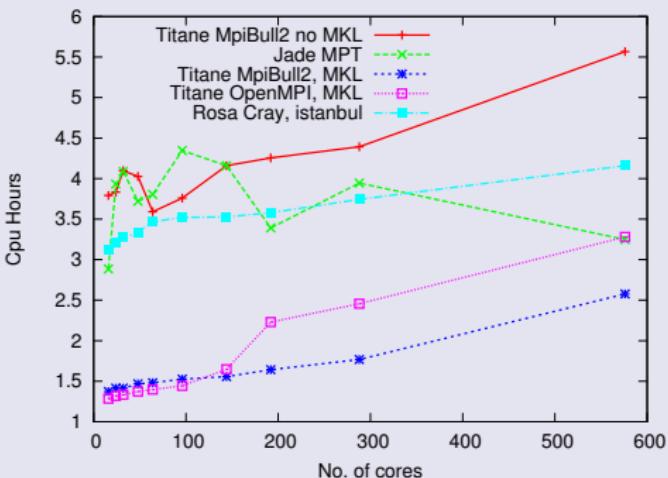
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Same runs, same sources; different user conditions



Differences up to a factor of 3!

A case-by-case study

Considerations are often system-dependent, a thumb rule not always exists.

☛ Know your code!



Nature of the operations

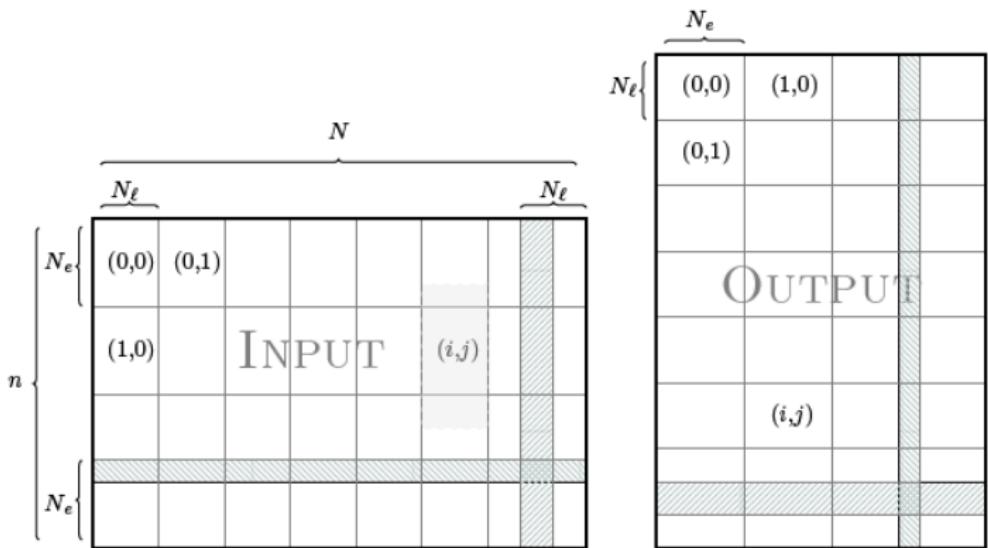
- Operators approach via convolutions
- Linear Algebra due to orthogonality of the basis
- Communications and calculations do not interfere
- A number of operations which can be accelerated

Evaluating GPU convenience

Three levels of evaluation

- ➊ Bare speedups: GPU kernels vs. CPU routines
Does the operations are suitable for GPU?
- ➋ Full code speedup on one process
Amdahl's law: are there hot-spot operations?
- ➌ Speedup in a (massively?) parallel environment
The MPI layer adds an extra level of complexity

Convolutions and Transposition in GPU



Blocking operations

A work group performs convolutions plus transpositions
Different boundary conditions can be implemented

OpenCL data management

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Example of 4×4 block with a filter of length 5

0,0	1,0	2,0	3,0
0,1	1,1	2,1	3,1
0,2	1,2	2,2	3,2
0,3	1,3	2,3	3,3
0,0	1,0	2,0	3,0
0,1	1,1	2,1	3,1
0,2	1,2	2,2	3,2
0,3	1,3	2,3	3,3

0,0	0,1	0,2	0,3
1,0	1,1	1,2	1,3
2,0	2,1	2,2	2,3
3,0	3,1	3,2	3,3

SIMD implementation

Each work item is associated to a single output element
Convolution buffers → data reuse

Convolution kernel with OpenCL

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Comparison with CPU work (Ex. X5550, 2.67 GHz)

Method	GFlop/s	% of peak	SpeedUp
Naive (FORTRAN)	0.54	5.1	1/(6.25)
Current (FORTRAN)	3.3	31	1
Best (C, SSE)	7.8	73	2.3
OpenCL (Fermi)	97	20	29 (12.4)

Very good and promising results

- No need of data transfer for 3D case (chain of 1D kernels)
- Deeper optimisation still to be done (20% of peak)
- Require less manpower than deep CPU optimisation
 - Automatic generation will be considered

GPU-ported operations in BigDFT (double precision)

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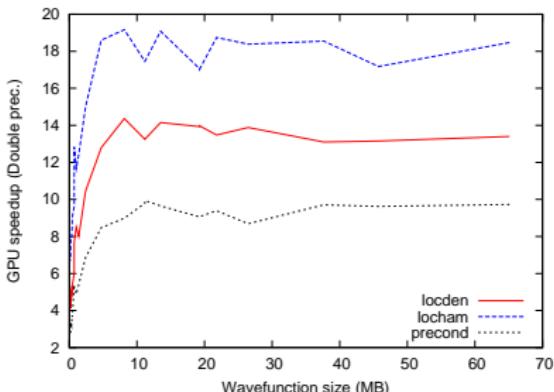
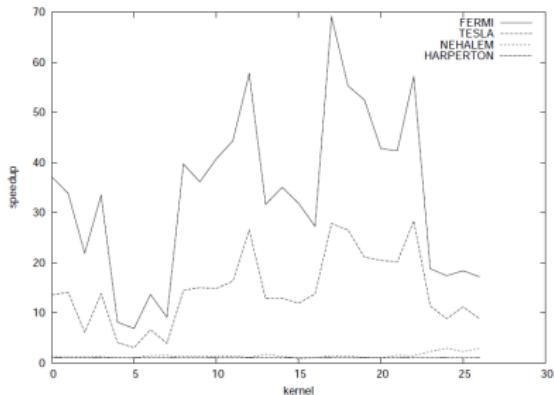
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Convolutions Kernels

- ☛ (OpenCL (re)written)
- ✓ Fully functional (all BC)
- ✓ Based on the former CUDA version
- ✓ A 10 to 50 speedup



GPU BigDFT sections

GPU speedups between 5 and 20, depending of:

- ✓ Wavefunction size
- ✓ CPU-GPU Architecture

BigDFT in hybrid codes

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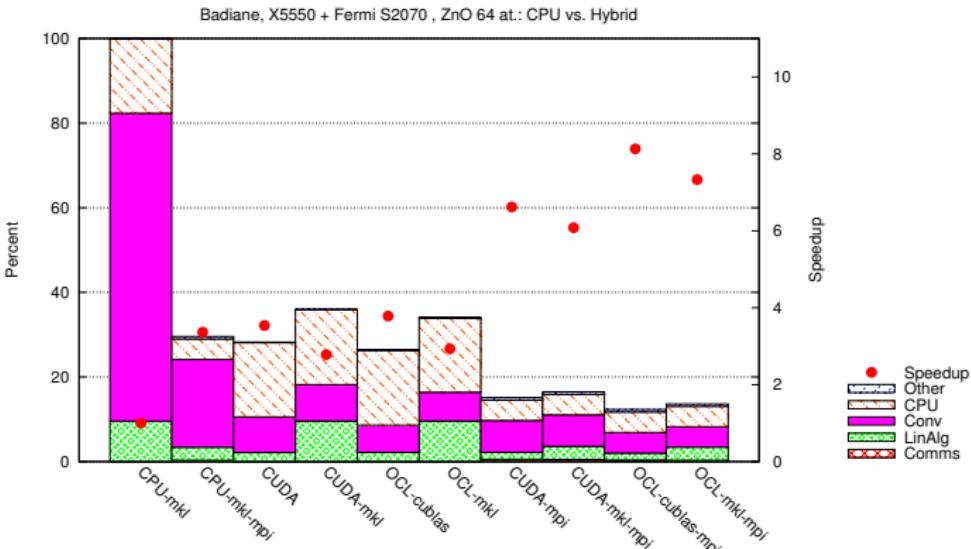
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Acceleration of the full BigDFT code

- Considerable gain may be achieved for suitable systems
Amdahl's law should always be considered
- Resources can be used concurrently (OpenCL queues)
More MPI processes may share the same card!



The time-to-solution problem I: Efficiency

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Good example: 4 C at, surface BC, 113 Kpts

Parallel efficiency of 98%, convolutions largely dominate.

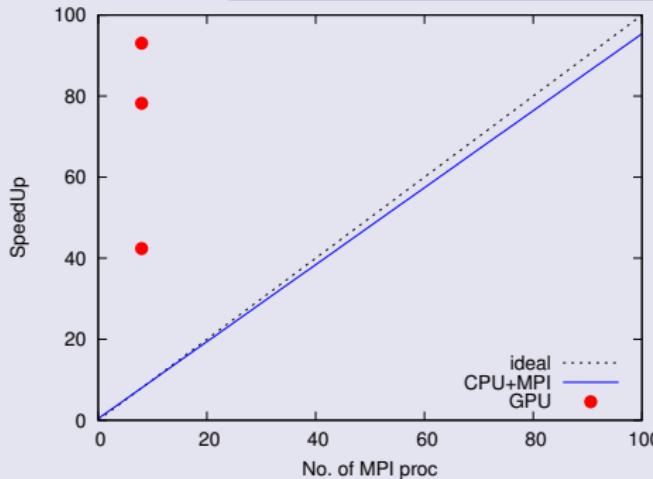
Node:

2× Fermi + 8 ×

Westmere

8 MPI processes

# GPU added	2	4	8
SpeedUp (SU)	5.3	9.8	11.6
# MPI equiv.	44	80	96
Acceler. Eff.	1	.94	.56



The time-to-solution problem II: Robustness

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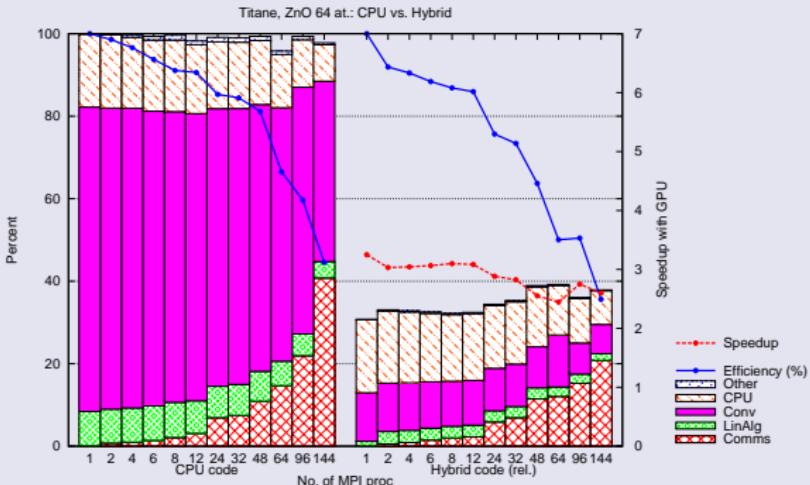
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Not so good example: A too small system



- ✗ CPU efficiency is poor (calculation is too fast)
- ✗ Amdahl's law not favorable (5x SU at most)
- ✓ GPU SU is almost independent of the size
- ✓ The hybrid code *always* goes faster

Hybrid and Heterogeneous runs with OpenCL

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NVidia S2070



Connected each to a Nehalem Workstation

BigDFT may run on both

ATI HD 6970



Sample BigDFT run: Graphene, 4 C atoms, 52 kpts

No. of Flop: $8.053 \cdot 10^{12}$

MPI	1	1	4	1	4	8
GPU	NO	NV	NV	ATI	ATI	NV + ATI
Time (s)	6020	300	160	347	197	109
Speedup	1	20.07	37.62	17.35	30.55	55.23
GFlop/s	1.34	26.84	50.33	23.2	40.87	73.87

Next Step: handling of Load (un)balancing

Concrete examples with BigDFT code

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MD simulation, 32 water molecules, 0.5 fs/step

Mixed MPI/OpenMP BigDFT parallelisation vs. GPU case

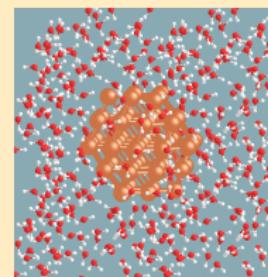
MPI+OMP	32•1	128•1	32•6	128•6	128+128
s/SCF	7.2	2.0	1.5	0.44	0.3
MD ps/day	0.461	1.661	2.215	7.552	11.02

An example: challenging DFT for catalysis

Multi-scale study for OR mechanism on PEM fuel cells

- Explicit model of H_2O/Pt interface
- Absorbtion properties, reaction mechanisms

Outcomes from the understanding of catalytic mechanism at atomic scale:



- Conception of new active and selective materials
- Fuels cell ageing, more efficient and durable devices

The fuel: Scientific Topics

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Scientific directions: Energy conversion

A scientific domain which embodies a number of challenges:

- ✓ The quantities are “complicated” (many body effects)
Study/prediction of fundamental properties: band gaps, band offsets, excited state quantities,...
- ✓ Objects are “big” and the environment matters
Systems react with the surroundings
- ↳ Building new modelisation paradigms

How to achieve these objectives?

Short and medium term objectives

- State-of-the art functionalities of DFT for complex environments
- Explore new formalisms for Post DFT treatments



A concerted set of actions

- Improve codes functionalities for present-day and next generation supercomputers
- Test and develop new formalisms
- Insert ab-initio codes in new scientific workflows
(Multiscale Modelling)

The Mars mission

Is Petaflop performance possible?

- GPU acceleration → one order of magnitude
- Bigger systems, heavier methods → (more than) one order of magnitude bigger

BigDFT experience makes this feasible

An opportunity to achieve important outcomes and know-how

General considerations

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Optimisation effort

- Know the code behaviour and features
Careful performance study of the complete algorithm
- Identify and *make modular* critical sections
Fundamental for maintainability and architecture evolution
- Optimisation cost: consider *end-user* running conditions
Robustness is more important than best performance

Performance evaluation know-how

- No general thumb-rule: what means High Performance?
A multi-criterion evaluation process
- Multi-level parallelisation always to be used
Your code will not (anymore) become faster via hardware

Conclusions



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BigDFT code: a modern approach for nanosciences

- ✓ Flexible, reliable formalism (wavelet properties)
- ✓ Easily fit with massively parallel architecture
- ✓ Open a path toward the diffusion of Hybrid architectures

Messages from GPU experience with BigDFT

- ✓ GPU allow a significant reduction of the time-to-solution
- ✓ Require a well-structured underlying code which makes multi-level parallelisation possible
- ✓ **To be taken into account while evaluating performances**

Parallel efficiency \Leftarrow dimensioning of system wrt architecture

CECAM BigDFT tutorial next October

A tutorial on BigDFT code is scheduled!

Grenoble, 19-21 October 2011



Acknowledgments



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GPU

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Code details

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GPU

Practical cases

Discussion

Messages

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