

Filtering, reconstruction and registration of 3D Ultrasound Images

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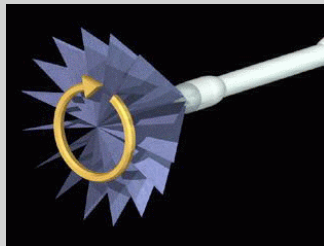
Overview

- Three Topics for 3D US imaging
 - Filtering
 - 3D Reconstruction
 - Registration

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3D Ultrasound Images

- Cylindrical geometry of image acquisition

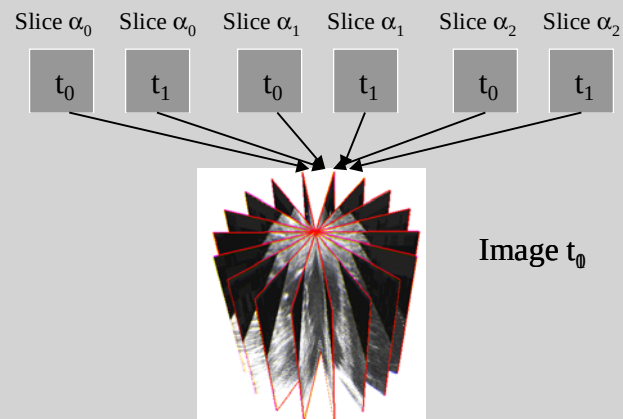


- 3D+T Imaging Systems
 - ATL Corporation (courtesy of G. Schwartz)
 - Echocard3D (courtesy of M-O. Berger)
 - HP Corporation (courtesy of A. Noble)

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4D Ultrasound images

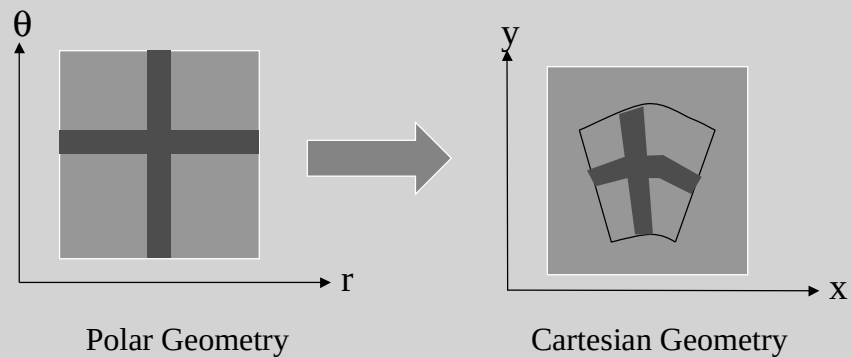
- Time series of images gated on ECG signal



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2D Image Storage Format

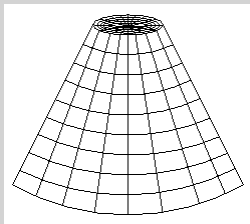
- Acquisition in polar geometry



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3D Image Storage Format

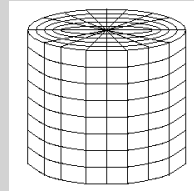
- Spherical Image Acquisition



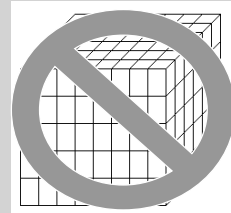
Spherical Geometry



Cylindrical
Geometry



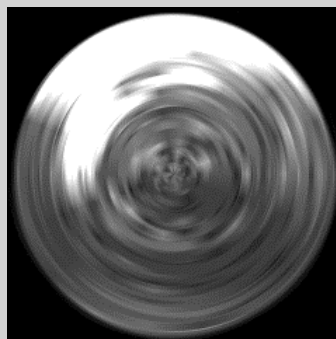
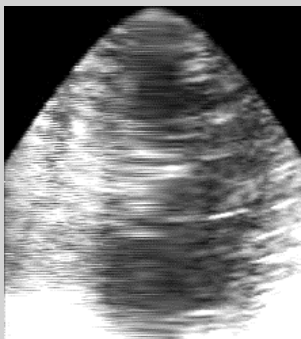
Cartesian
Geometry



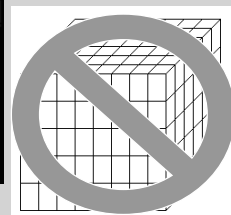
7

3D Image Storage Format

- Spherical Image Acquisition

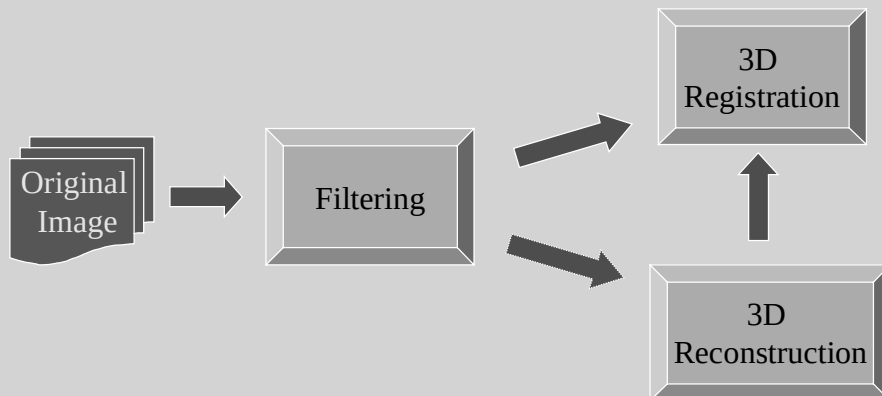


Cartesian
Geometry



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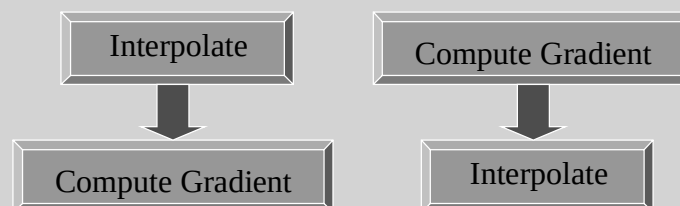
Global Scheme



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Gradient Computation

- 2D and 3D gradient information:
 - Used for 2D, 3D and 4D Anisotropic Diffusion
 - Used for segmentation based on deformable contours/surfaces
- Two options:



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Gradient Computation (2)

- Previous Work : (Herlin and Ayache 92)
- Cylindrical Filtering

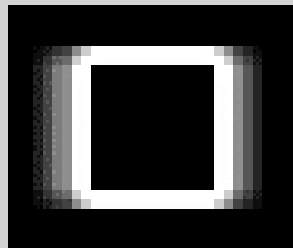
$$(I \otimes f)(v) = \iiint f(v_x - r \cos \theta, v_y - r \sin \theta, v_z - z) I(r, \theta, z) r dr d\theta dz$$

- Implementation
 - convolution with local masks that depend on the distance to the axis

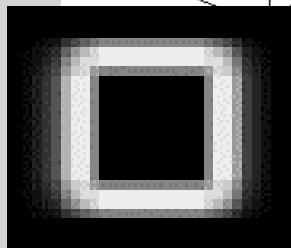
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Gradient Computation (3)

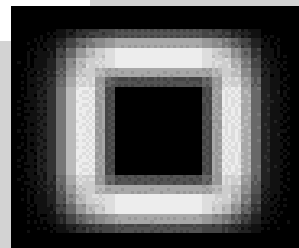
- Example



Window=3



Window=5



Window=7

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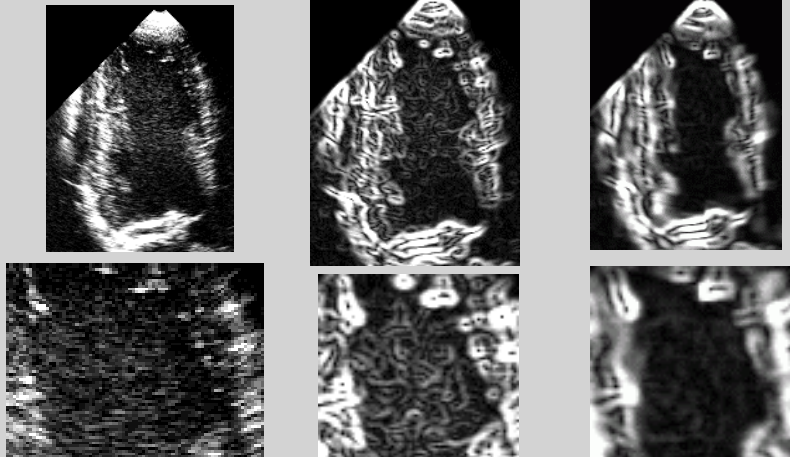
Gradient Computation (4)

Original Image

it ?

2D Cartesian

Cylindrical



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Image Enhancement

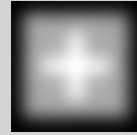
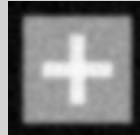
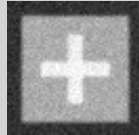
- Improve detection of boundary
- Previous Work:
 - Diffusion Tensor : (Cottet et al. 95)
 - AOS Scheme for diffusion (Weickert et al. 98)
 - 4D Anisotropic Diffusion (Jacob et al. 99)

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Anisotropic Diffusion

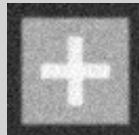
- Isotropic Diffusion

$$\frac{\partial I}{\partial t} = \Delta I = \text{div}(\vec{\nabla} I)$$



- Anisotropic Diffusion

$$\frac{\partial I}{\partial t} = \text{div}(g(\|\vec{\nabla} I\|) \vec{\nabla} I)$$



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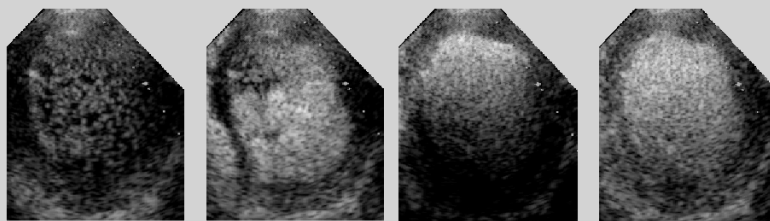
Time-dependent Anisotropic Diffusion

- Time information helps removing speckle/noise
- Two approaches :
 - Perform 2D+T diffusion
 - Perform 3D+T diffusion

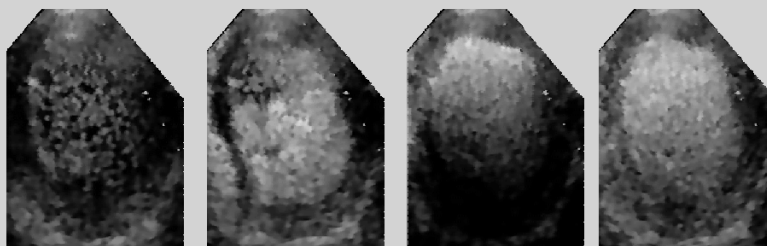
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2D Diffusion

Original
Images



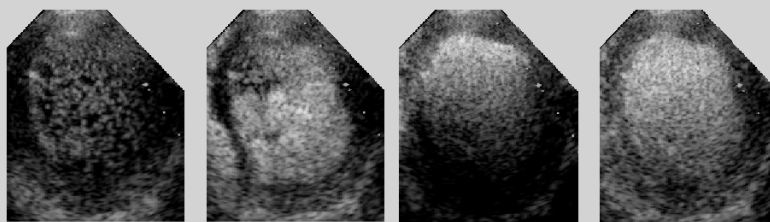
2D
Anisotropic
Diffusion



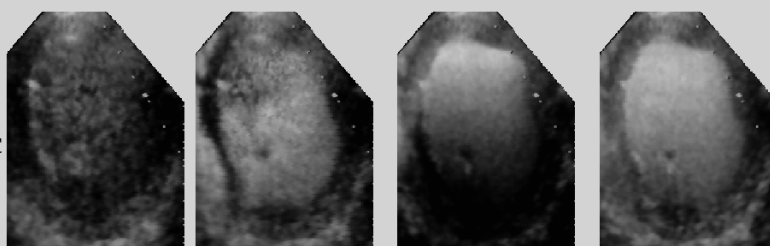
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2D+T Diffusion

Original
Images



2D+T
Anisotropic
Diffusion



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3D+T Diffusion

- Use Diffusion Tensor :

$$\frac{\partial I}{\partial t} = \text{div} \left(D(\| \vec{\nabla}^t I_\sigma \|) \vec{\nabla}^t I \right)$$

With :

$$\vec{\nabla}^t I = \begin{pmatrix} I_x \\ I_y \\ I_z \\ I_t \end{pmatrix}$$

$$D(\vec{\nabla}^t I) = \begin{pmatrix} \frac{1}{\sqrt{1 + \left(\frac{I_x}{\lambda_x}\right)^2}} & 0 & 0 & 0 \\ 0 & \frac{1}{\sqrt{1 + \left(\frac{I_y}{\lambda_y}\right)^2}} & 0 & 0 \\ 0 & 0 & \frac{1}{\sqrt{1 + \left(\frac{I_z}{\lambda_z}\right)^2}} & 0 \\ 0 & 0 & 0 & \frac{1}{\sqrt{1 + \left(\frac{I_t}{\lambda_t}\right)^2}} \end{pmatrix}$$

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3D+T Diffusion (2)

- Implementation Issues :
 - Iteratively estimate gradient thresholds

$$\lambda_x, \lambda_y, \lambda_z, \lambda_t$$

- Computationally expensive

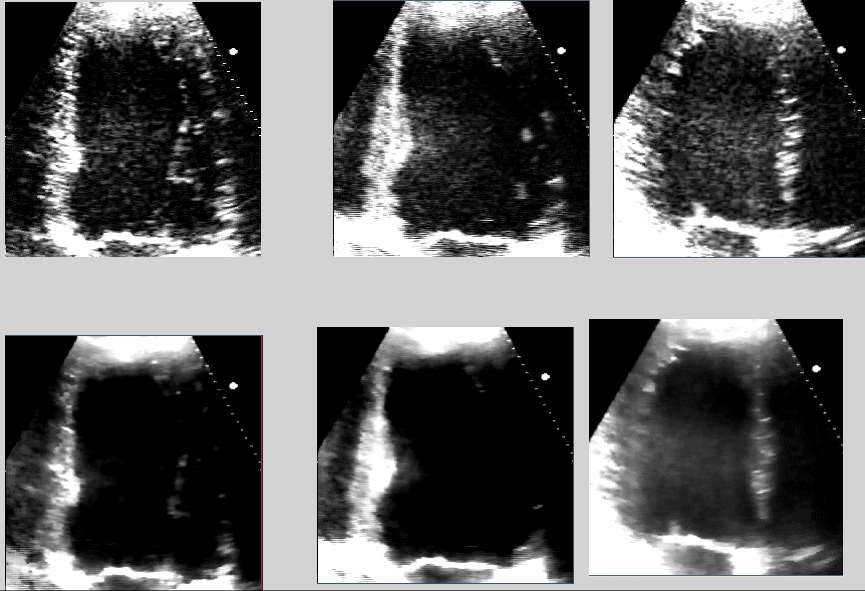


Use of AOS discretization scheme

- Can use large time steps

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3D+T Diffusion (3)



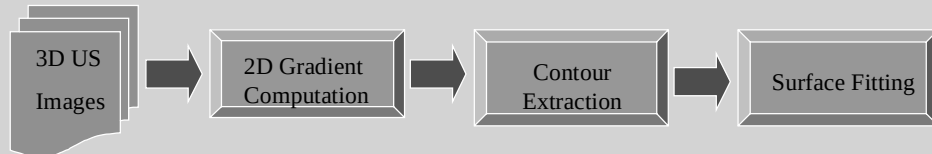
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3D Reconstruction

- 2 Key Ideas:
 - Find boundary points
 - Perform 3D Regularization
- 2 Different Strategies
 - Extract 2D contours and fit a 3D surface
 - Extract a 3D surface directly

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First Strategy



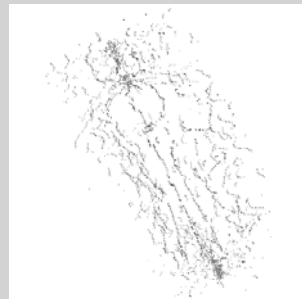
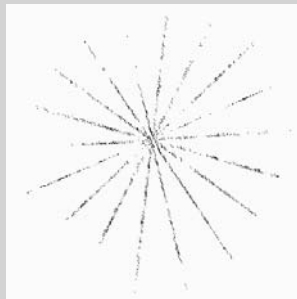
- Direct Contour extraction (Roux et al. 98)
- Use Deformable Contours (Noble et al. 98, Berger et al. 97)

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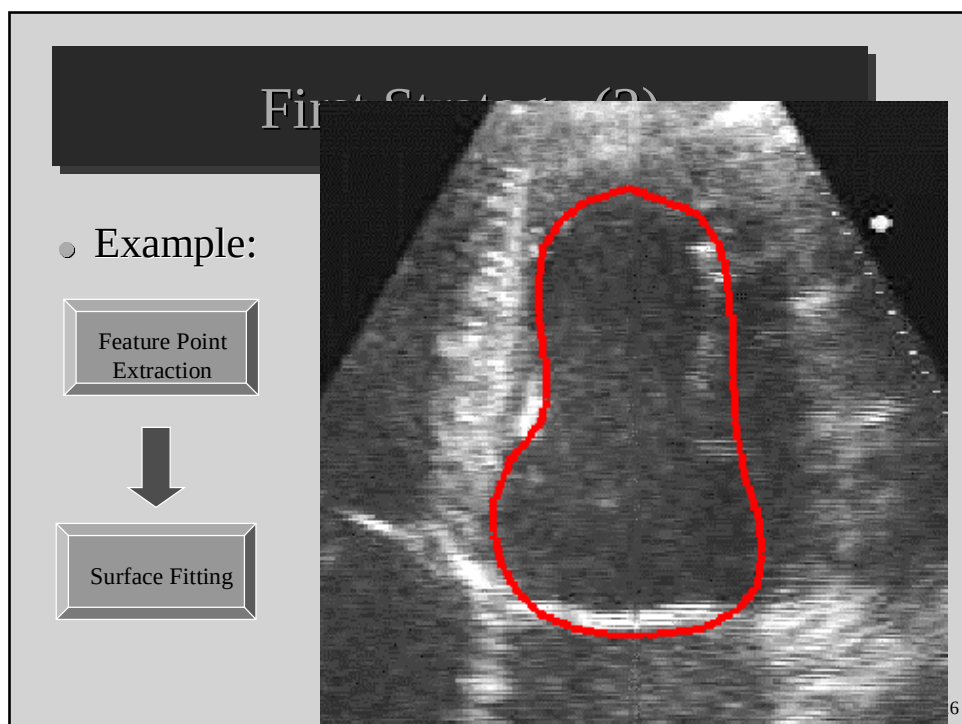
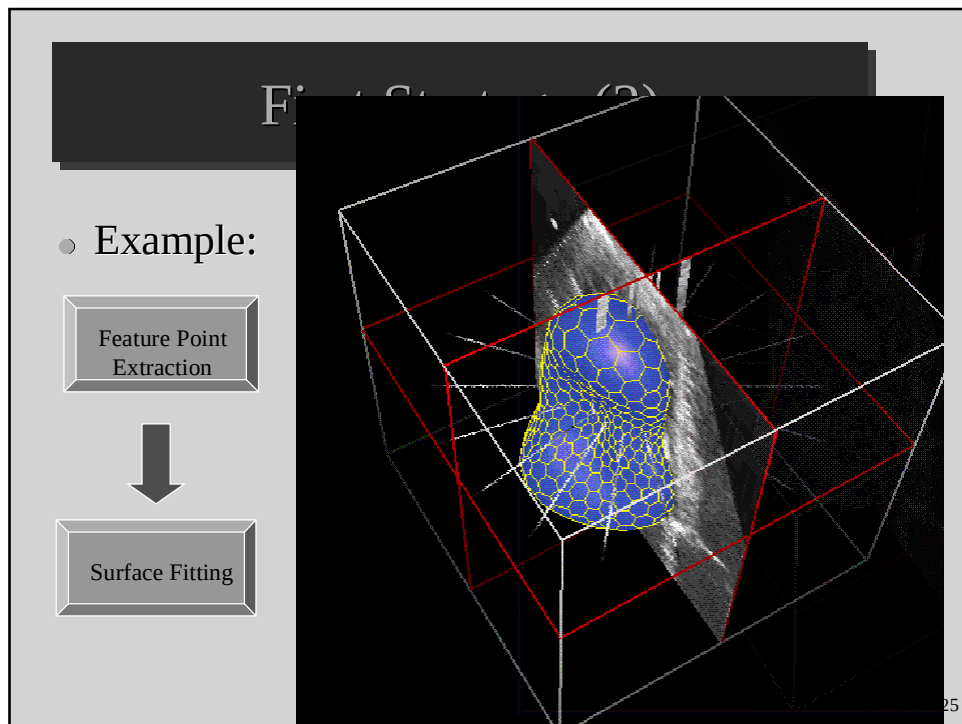
First Strategy (2)

- Example:

Feature Point
Extraction



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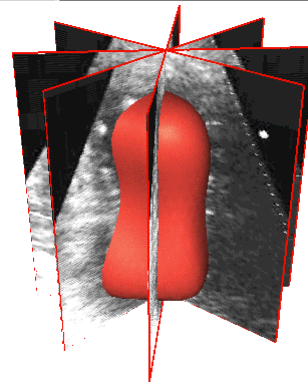
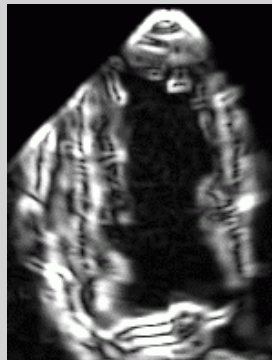


Second Strategy

3D US
Images

3D Gradient
Computation

Surface Fitting



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3D Surface Fitting

- Use simplex meshes as the surface representation
- Use scan-line algorithm for external force computation in cylindrical images
- Use “region” (intensity+gradient) to detect boundaries

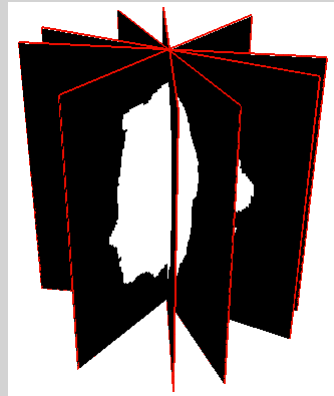
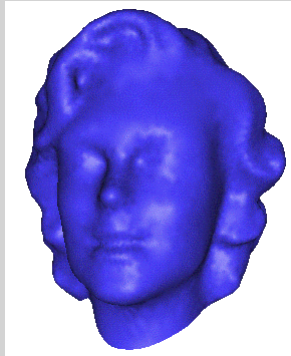


See J. Montagnat's poster

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3D Surface Fitting (2)

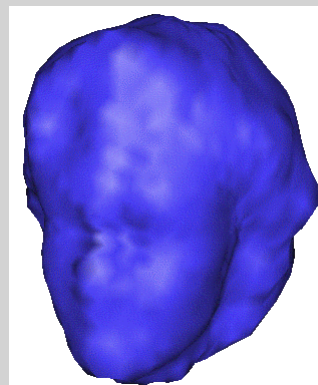
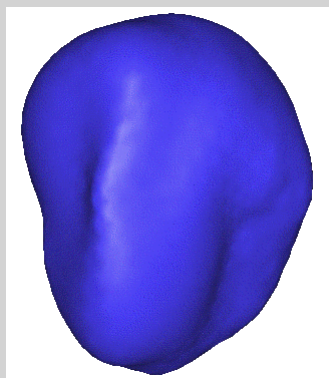
- Synthetic Example:



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3D Surface Fitting (2)

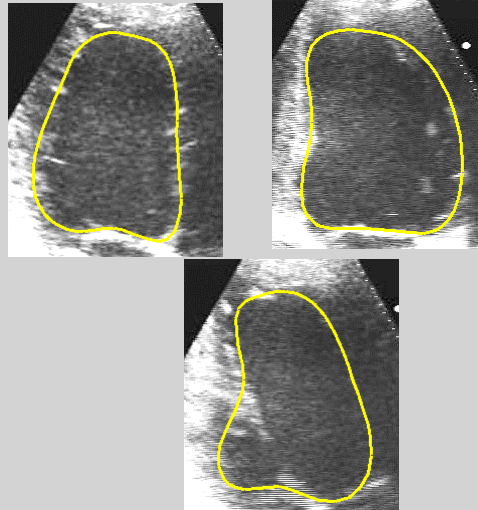
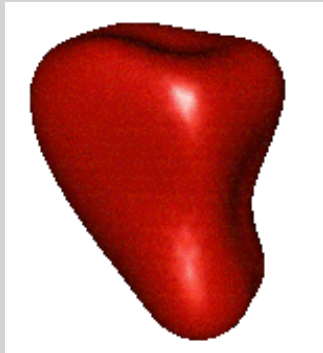
- Synthetic Example:



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3D Surface Fitting (3)

- Example:



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4D Image Reconstruction

- 1 key idea
 - Use temporal information for shape regularization
- 3 different approaches
 - Weak temporal constraint
 - Strong temporal constraint for 2D+T
 - Strong temporal constraint for 3D+T

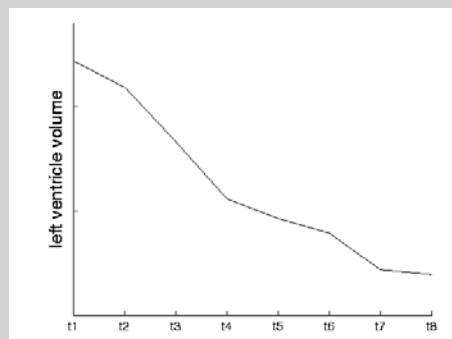
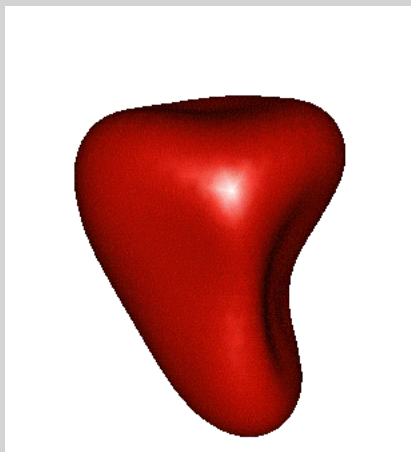
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Weak Temporal Constraint

- Use 3D model at time t as the initial model at time $t+1$
 - 😊 Straightforward generalization
 - 😞 Weak enforcement of time continuity
 - 😞 No periodicity of motion

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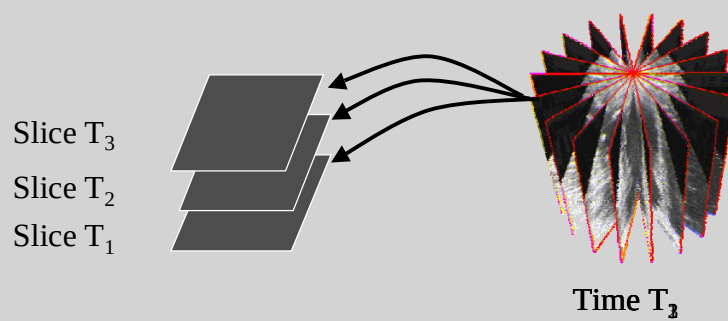
Weak Temporal Constraint (2)



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2D+T Reconstruction

2D+T Image
Formation



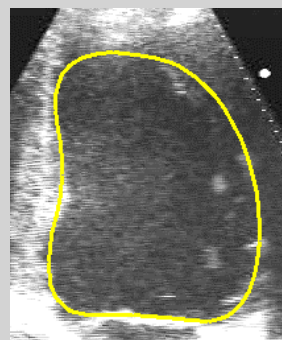
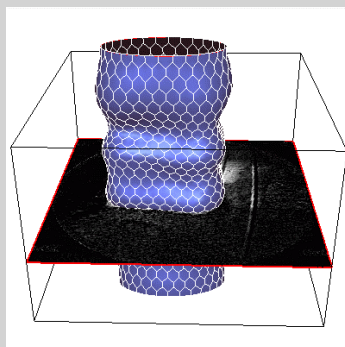
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2D+T Reconstruction

2D+T Image
Formation



2D+T Surface
Fitting



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2D+T Reconstruction

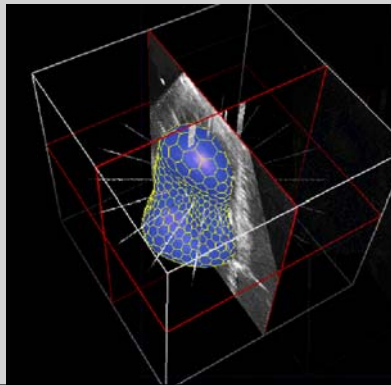
2D+T Image
Formation



2D+T Surface
Fitting



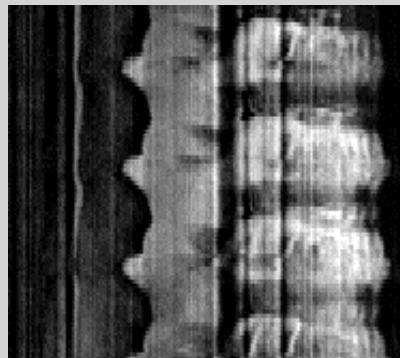
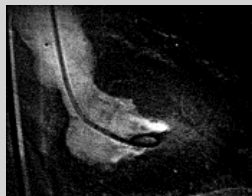
3D Surface
Fitting



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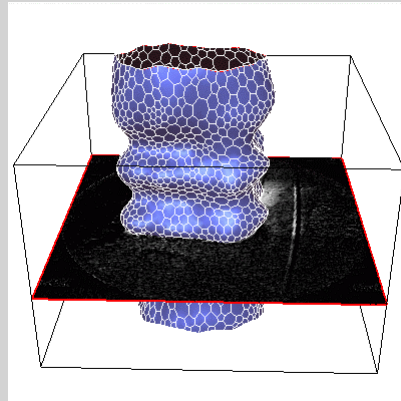
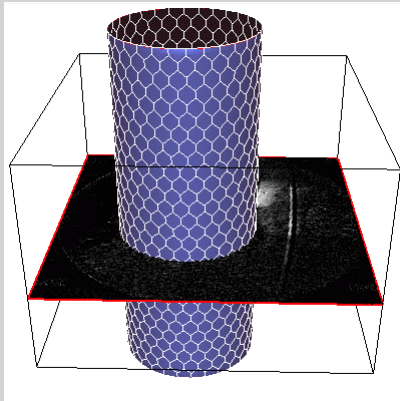
2D+T Reconstruction (2)

- Example : Ventriculography (courtesy of CCM)



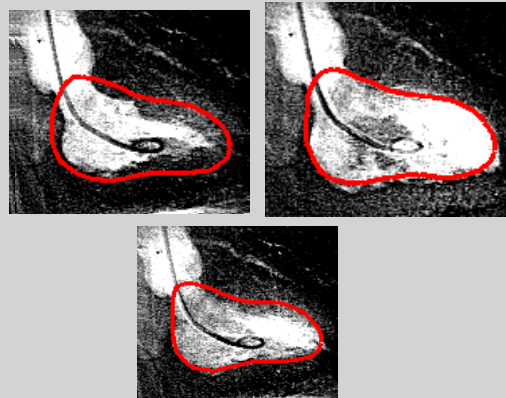
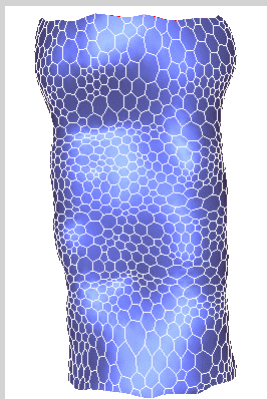
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2D+T Reconstruction (3)



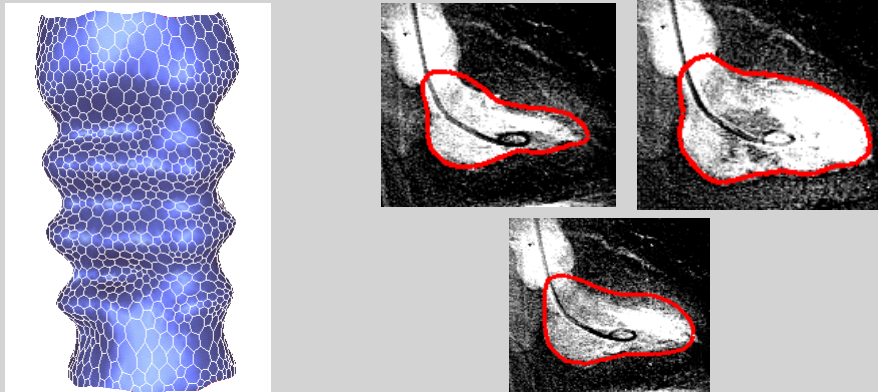
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2D+T Reconstruction (3)



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2D+T Reconstruction (3)



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3D+T Reconstruction

- Reconstruct simultaneously all 3D models with temporal constraints acting as regularizing forces
 - 😊 Enforce periodicity
 - 😊 Nicely differentiate between time/shape constraints
 - 😞 High memory+CPU requirements
- Previous work : (Declerck et al 98)

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Ultrasound image segmentation

- 4D image sequence
- 4D model deformation
- Resulting beating heart



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MR/US Registration

- updating pre-operative MR planning with intra-operative 3D US (Roboscope Project)



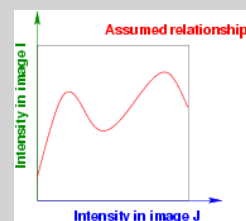
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MR/US Registration (2)

- Multi-modal image registration
- Related Work : (Hata et al. 94), (Erbe et al. 96), (Bucholz et al. 96) (Roche et al. 98)
- Iconic-based image registration

Hypothesis : Functional +
Gaussian Noise

Criterion : Correlation Ratio



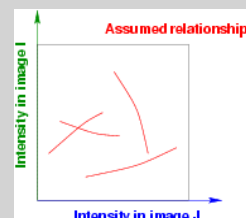
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MR/US Registration (2)

- Multi-modal image registration
- Related Work : (Hata et al. 94), (Erbe et al. 96), (Bucholz et al. 96) (Roche et al. 98)
- Iconic-based image registration

Hypothesis : Unconstrained
Transition Probabilities

Criterion : Mutual Information



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MR/US Registration (3)

- Results :



Satisfactory Accuracy : 2mm,
1Degree of rotation



Not robust : require close
initialization

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MR/US Registration (4)

Original
MR Image

Similarity measure	Failures
Correlation ratio	14%
Mutual information	51%

Anisotropic
Diffused
MR Image

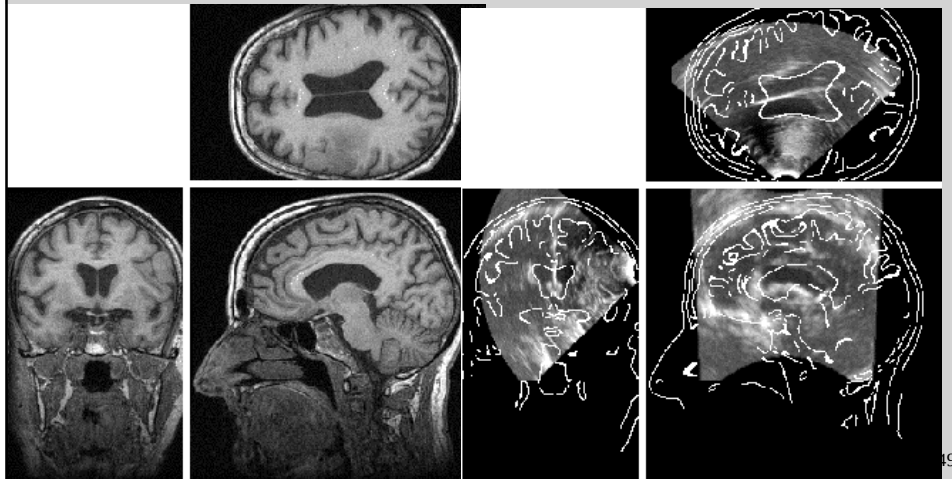
Similarity measure	Failures
Correlation ratio	12,5%
Mutual information	28%

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MR/US Registration (5)

MR image

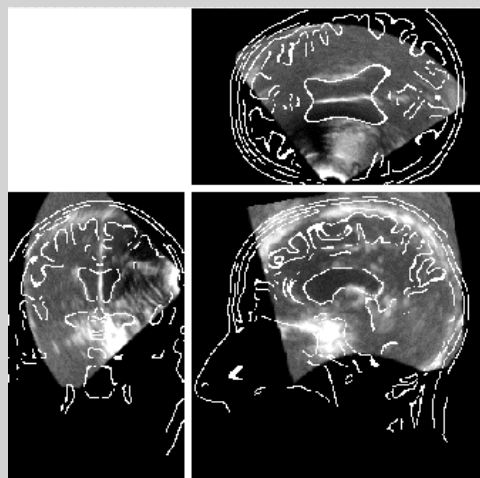
Original MR+US



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MR/US Registration (5)

US/MR Registration



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Conclusion

- Needs Validation
- Using geometry knowledge of 3D US images
 - Computation of 3D Gradient
 - 3D and 4D deformable models
- Perspectives:
 - add physical and anatomical knowledge