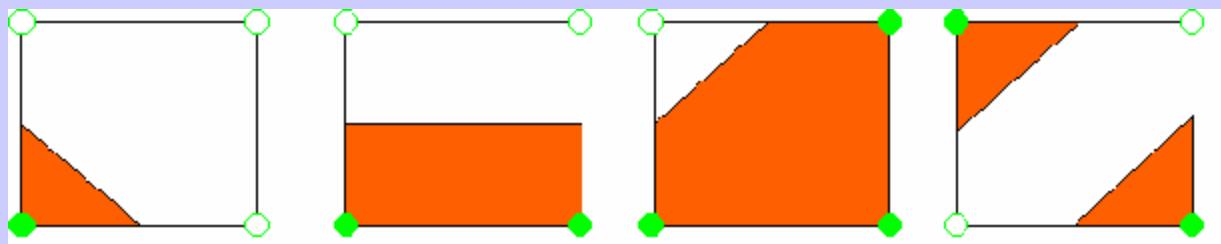


# Extraction d'Isocontour (2)

- Calcul de l'isocontour à l'intérieur de chaque pixel :

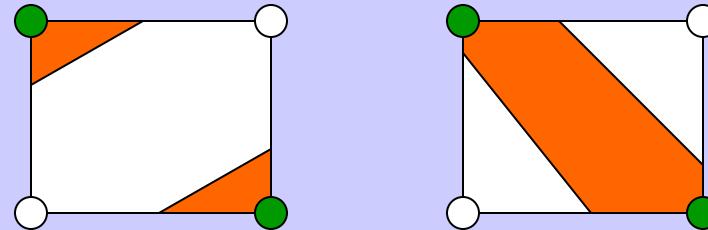


- Algorithme :

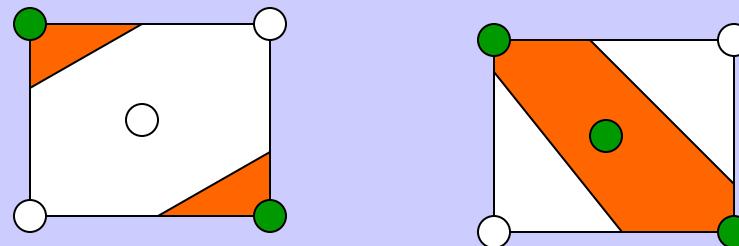


# Extraction d'Isocontour (3)

- Ambiguité : 2 choix sont possibles:



- On utilise l'un ou l'autre ou la moyenne des intensités au centre du pixel :



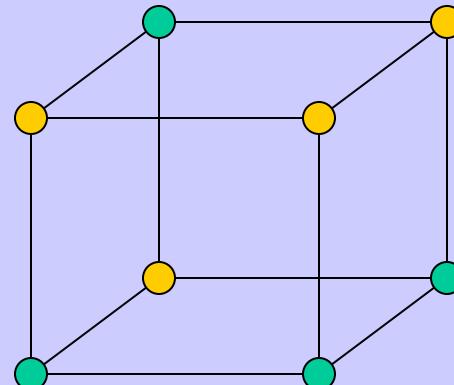
# Extraction d'Isosurface (1)

- On procède de même :
  - Dualité voxel/point
  - Calcul de l'intersection de l'isosurface avec chaque arête
  - Détermination des voxels qui intersecte l'isosurface
  - Calcul de l'intersection de l'isosurface avec chaque voxel



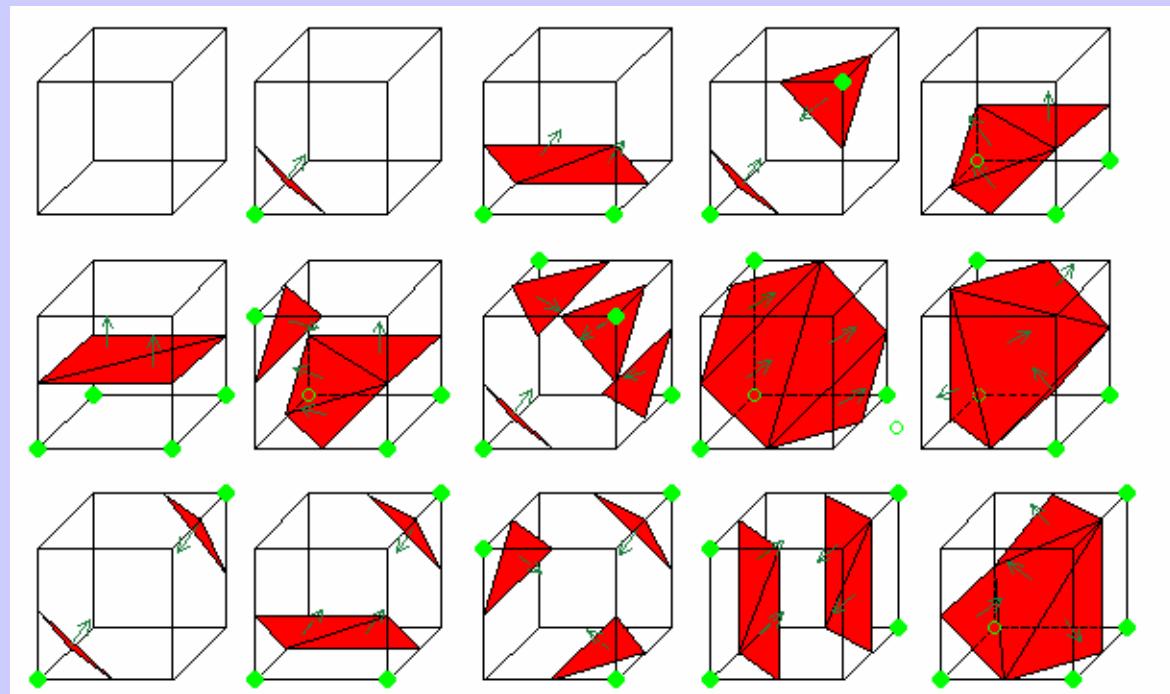
# Extraction d'Isosurface (2)

- Calcul de l'intersection de l'isosurface dans chaque voxel :
  - Intersection = ensemble de polygones 3D (non plan)
  - A priori  $8 \times 8 = 256$  possibilités



# Extraction d'Isosurface (3)

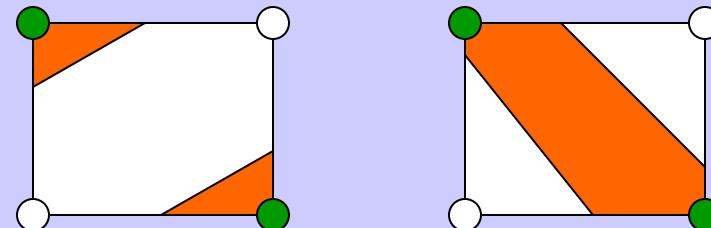
- Algorithme des « Marching Cubes » par Lorensen & Cline (1987)
- Par symétrie, on peut se ramener à 15 cas



# Extraction d'Isosurface (4)

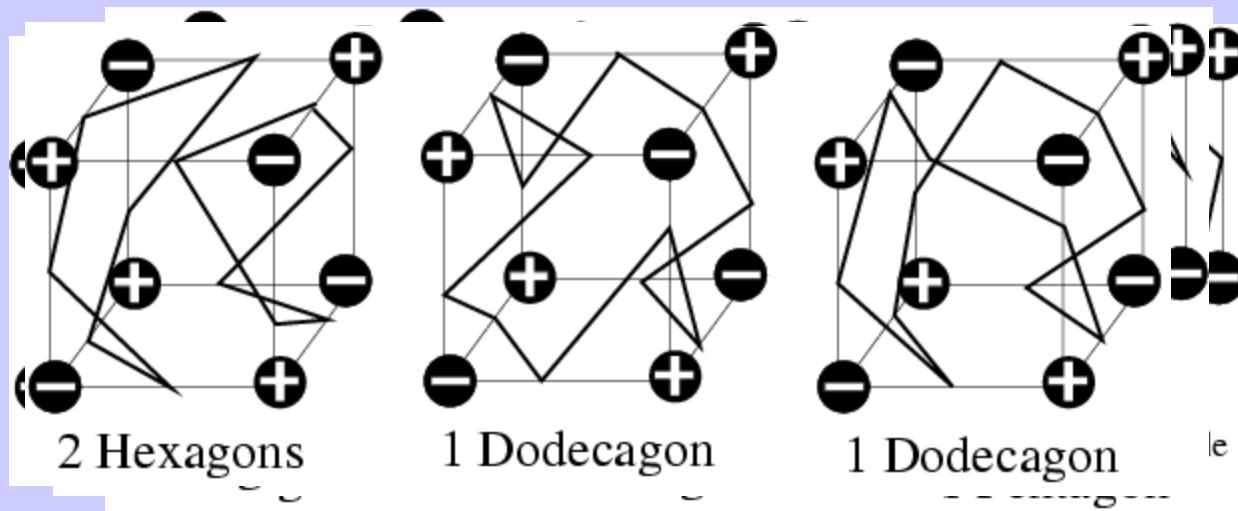
- Utilisation d'une table de hachage :
  - on code sur 1 octet la configuration
  - on associe la configuration avec un tableau ainsi que la symétrie à appliquer (un bit)
- Problème  $\Rightarrow$  on peut avoir des trous :

Une même face peut être discrétisée différemment suivant le voxel auquel elle appartient



# Extraction d'Isosurface (5)

- Plusieurs solutions :
  - prendre en compte le centre de chaque face (6 bit supplémentaires)



# Extraction d'Isosurface (5)

- Problèmes supplémentaires :
  - Nécessité de trianguler chaque polygone :
    - ajout d'arête entre sommets
    - ajout d'un sommet central
  - Grande quantité de triangles générés :
    - simplification des surfaces ultérieures
    - utilisation d'approches hiérarchiques
  - Possibilité d'utiliser des grilles simpliciales



# Segmentation

## *2. Modèles déformables*

# Modèles Déformables

- 2 idées principales:
  - Modèle Déformable est un récipient pour stocker de l'information a priori sur la géométrie et l'apparence de structures anatomiques
  - Définition des frontières fondée sur l'intensité et le gradient d'intensité

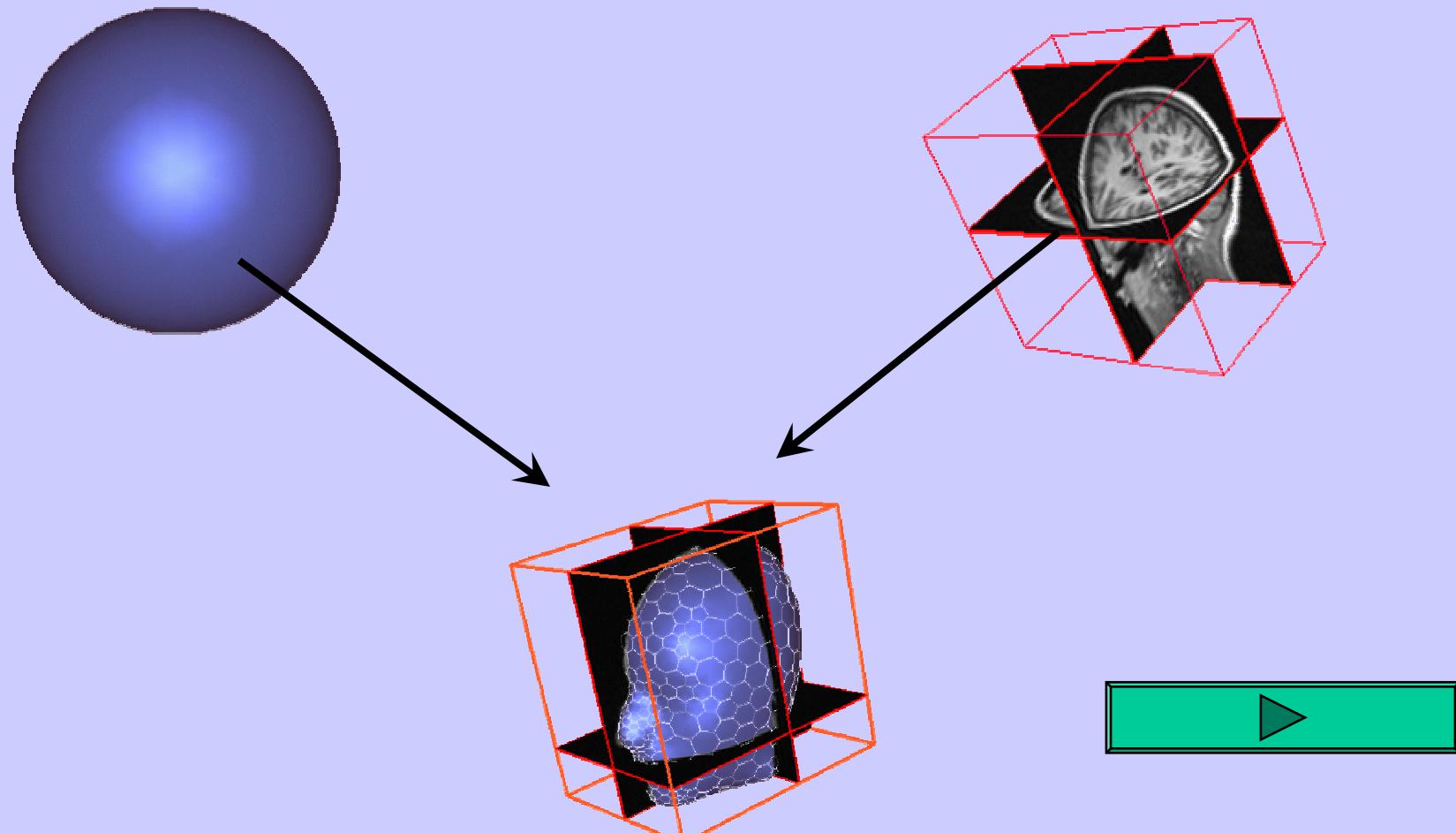
# Segmentation d'images à l'aide de modèles déformables

- Un modèle déformable est un récipient pour stocker de l'information a priori sur la **géométrie** et **l'apparence** de structures anatomiques
- Deux niveaux de connaissance a priori:

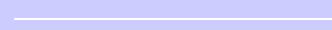
|           | Faible Connaissance a priori   | Grande Connaissance a priori                             |
|-----------|--|--|
| Forme     | Contrainte de continuité C1 ou C2<br>Initialisation avec formes génériques (sphère, ...) | Contrainte de Forme<br>Initialisation avec forme moyenne |
| Apparence | Utilise information de gradient et/ou intensité  | Utilise profils d'intensité ou appariement de blocs      |



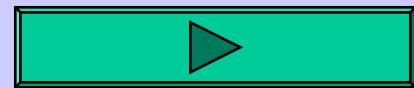
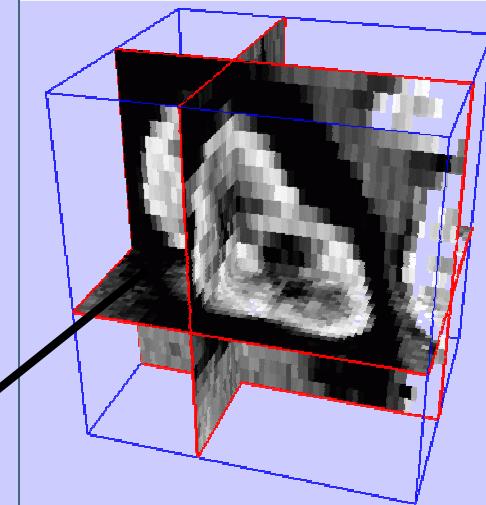
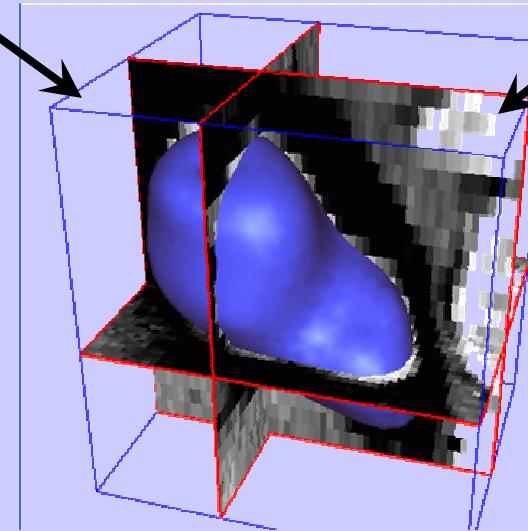
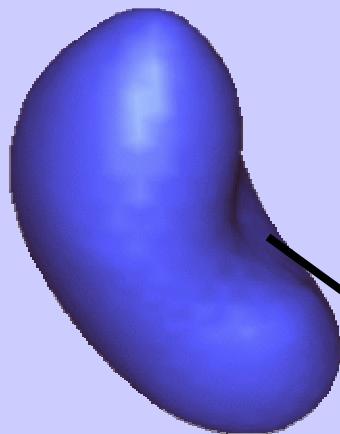
# Faible connaissance A Priori



- Valide pour des structures fortement contrastées
- Peut demander une intervention de l'utilisateur



# Forte connaissance A Priori



- Valide pour une structure donnée et une modalité donnée

08/02 • Plus robuste à l'exception des formes « anormales »

# Deformable model

- Snake / active contours
  - Minimisation of a two/three terms energy:

$$E(v(s)) = \int_0^1 \underbrace{E_{in}(v(s))}_{\text{internal energy}} + \underbrace{E_{im}(v(s))}_{\text{external energy}} + \underbrace{E_{con}(v(s))}_{\text{regularisation}} ds$$

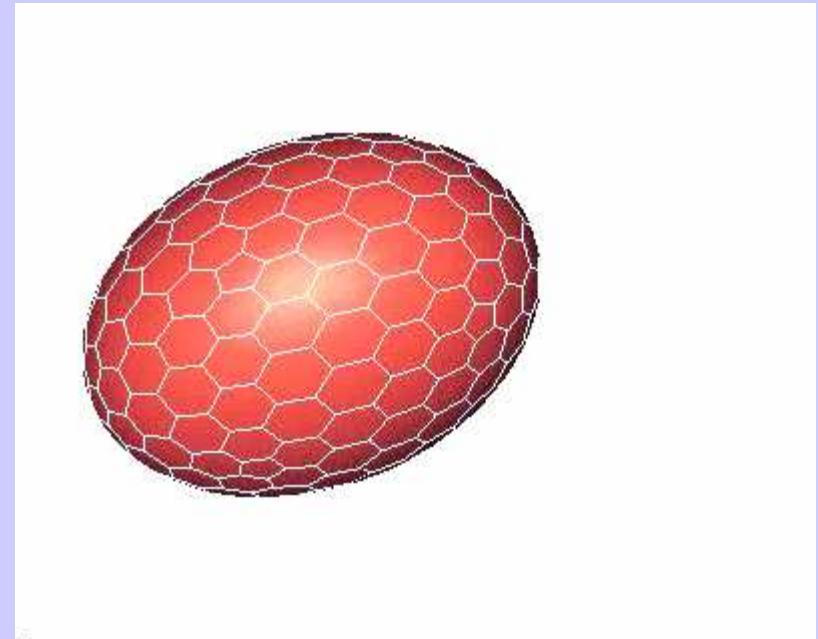
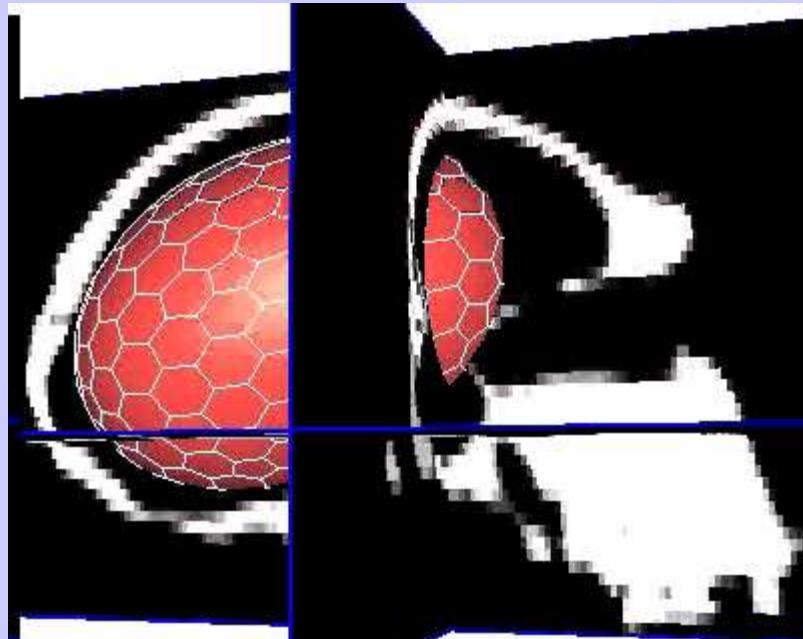
$E_{im}$ : internal energy (regularisation)

$$E_{in}(v(s)) \propto (\alpha) s \|v_s(\nabla v)(x, y)(s)\|_2^2$$



# Segmentation: endocranum

CT scan image, Bony structures



Time of convergence : 13,8 s

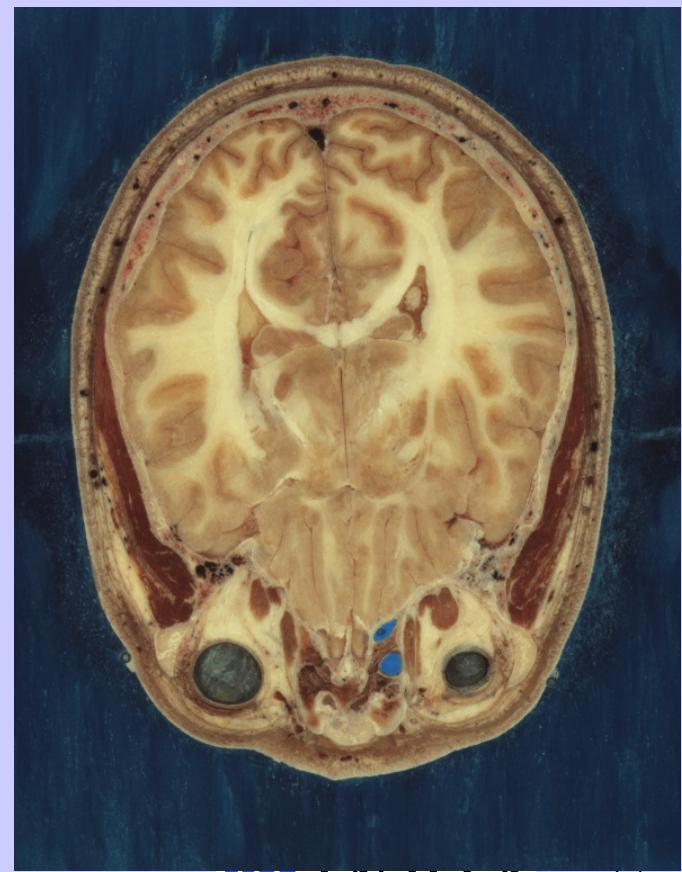
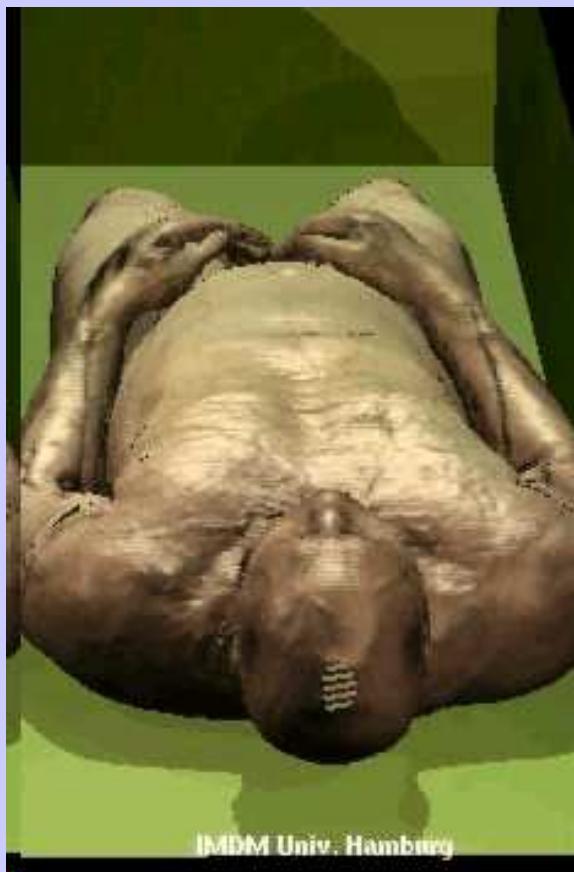
model:  $1169 \text{ cm}^3$   
mold:  $1150 \text{ cm}^3$

08/02/2006



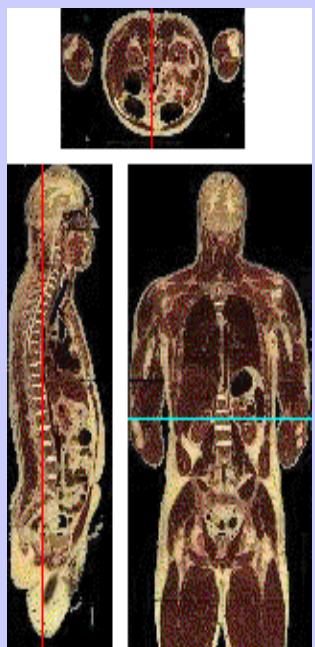
# Visible Human

Joseph Paul Jernigan (died August 5th 1993)

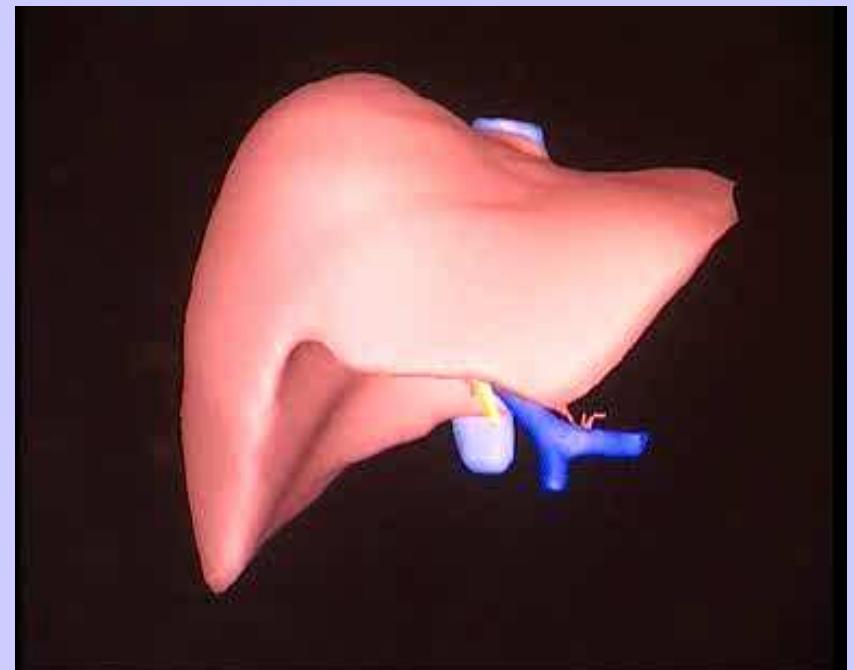
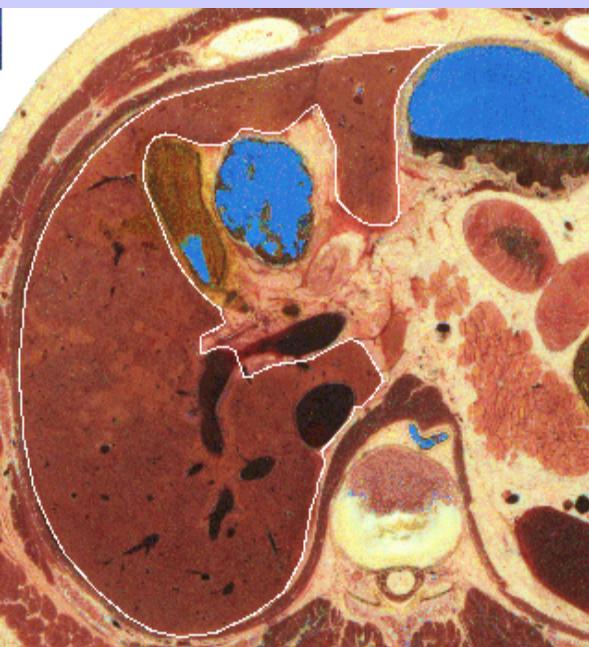


# Reconstruction du Foie

## Deformation à partir d 'un modèle de référence issu du « *Visible Human Project* »

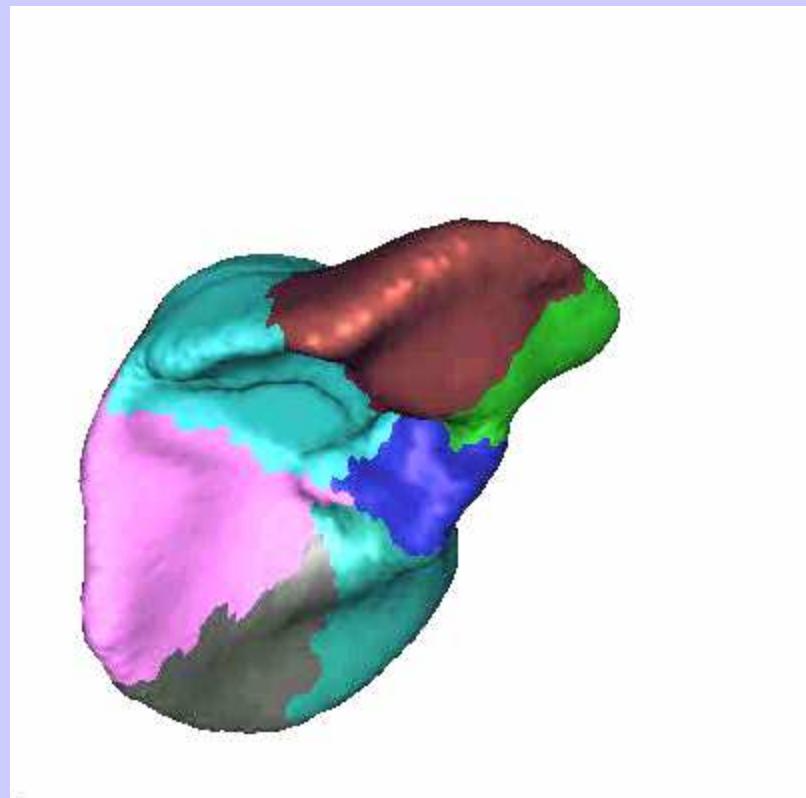
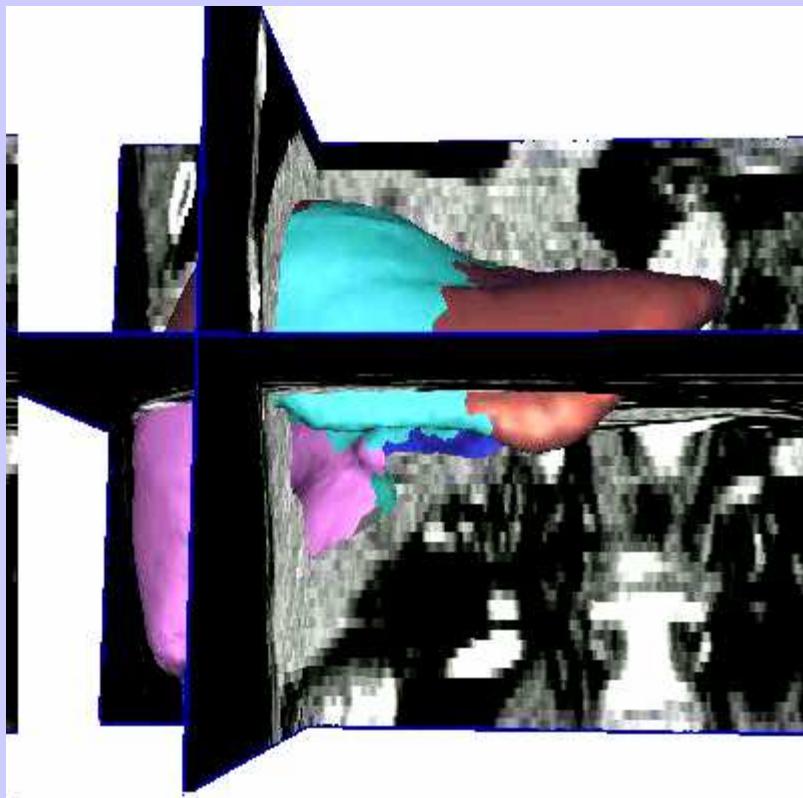


08/02/2006



# Segmentation: foie

Image scanner de l'IRCAD, extraction du foie



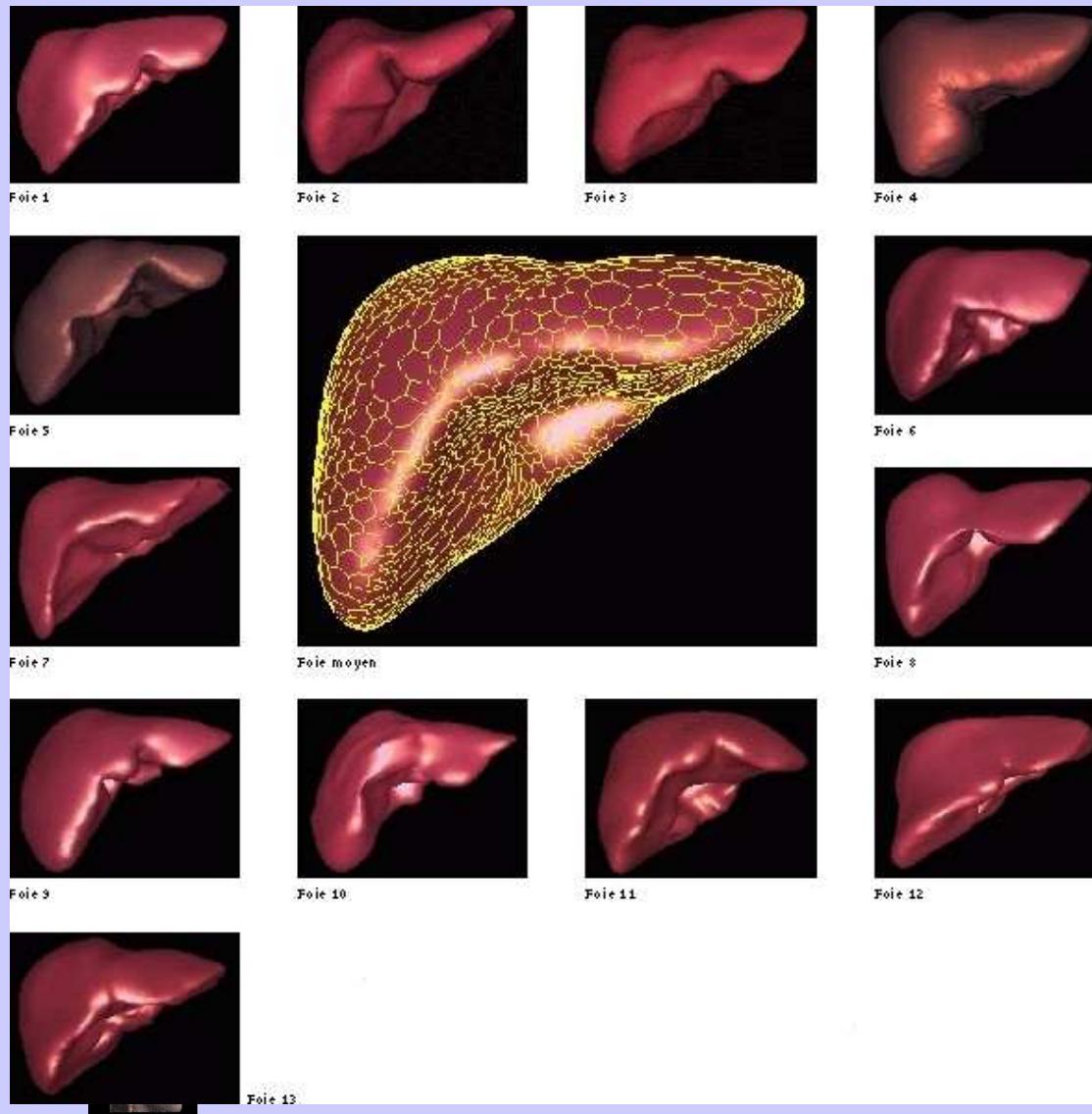
Temps de convergence: 2 mn 12 s

Extraction des segments de Couinaud

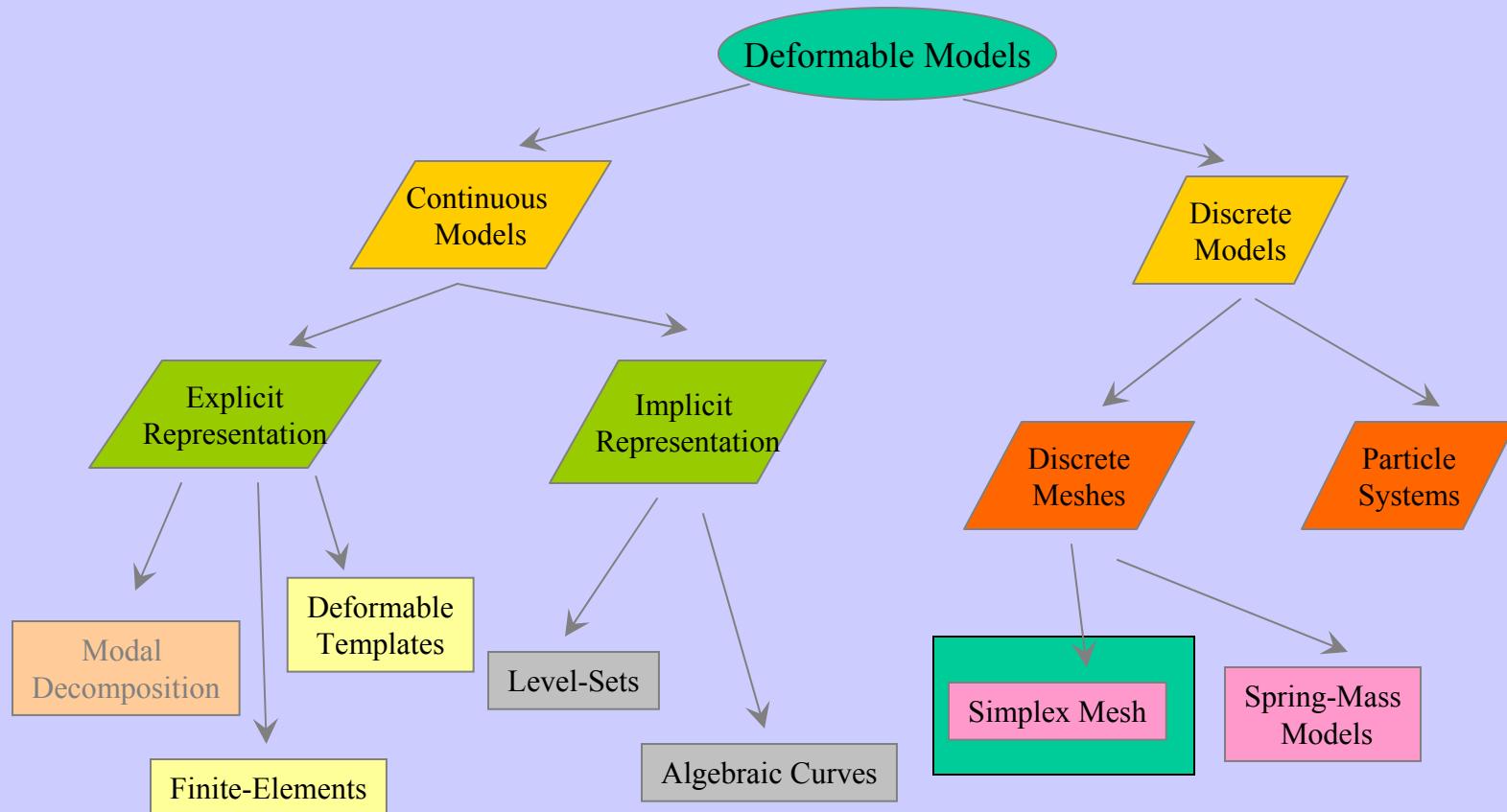
08/02/2006



# Variabilité anatomique du Foie



# Deformable Model Geometry (3)



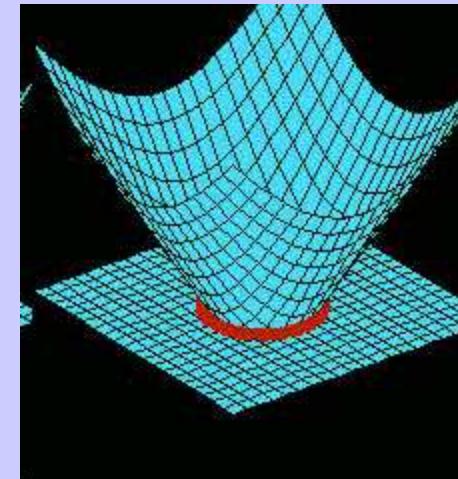
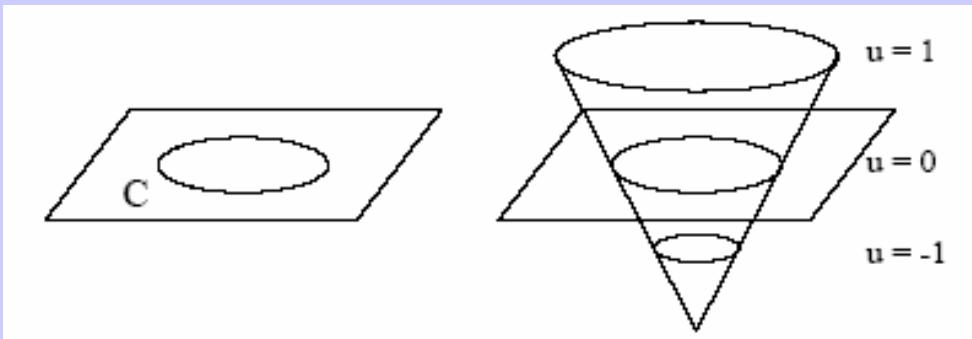
[Montagnat2001]



# Deformable models

- Level-sets
  - Curve/Surface  $C$  (in  $\Re^2/\Re^3$ ) that corresponds to an iso-level of a surface/hypersurface (in  $\Re^3/\Re^4$ )

$$C(t) = \{(x, y) \mid u(x, y, t) = 0\} \quad u_t + F |\nabla u| = 0$$



- Implicit representation

# Main difficulties in segmentation algorithms

- Ill-posed problem
  - Boundaries between structures may not be seen on images
  - Strong variability between experts for validation
- Most algorithms are dependent on the acquisition protocole and image modality
- Robustness required in the presence of pathologies



# Perspectives (2)

- Applications of segmentation :
  - Diagnosis
    - demand for very fast and automated algorithms with degree of confidence
  - Planning - Prediction -Prevention
    - demand for accurate but potentially not fully automated algorithms combined with high quality meshing
  - Clinical Research
    - demand for automated and accurate algorithm for use with large database (grid computing)



# Perspectives (3)

- Segmentation techniques is more and more split between :
  - Registration techniques :
    - registration with a anatomical/physical/physiological model
    - registration with a set of images (data fusion)
  - Low-level techniques :
    - anisotropic filtering, watershed, mathematical morphology

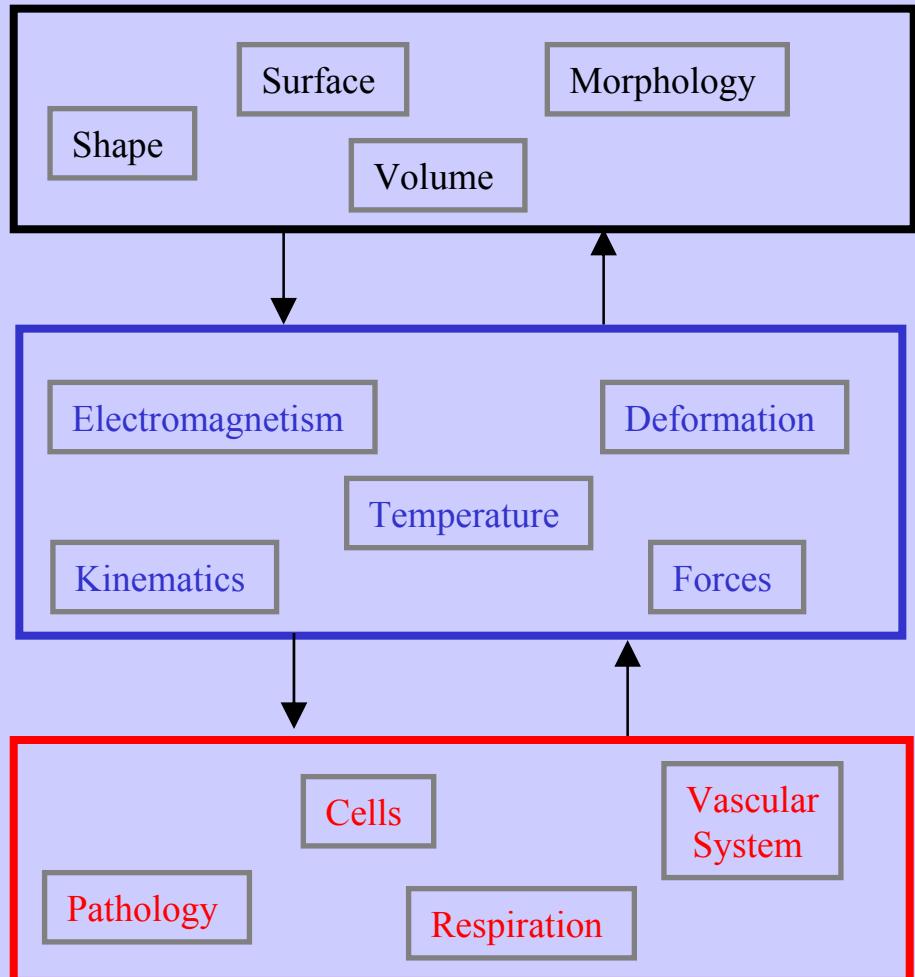
Need to define a unifying framework



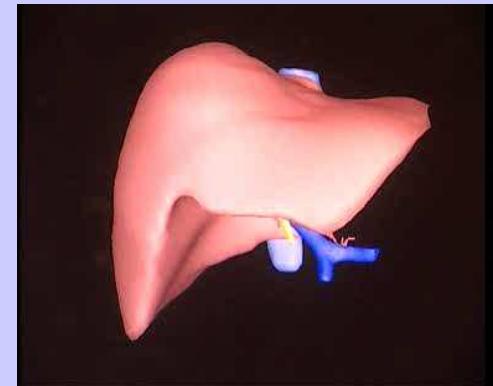
# Modélisation

*3. Computational Models of the  
Human Body*

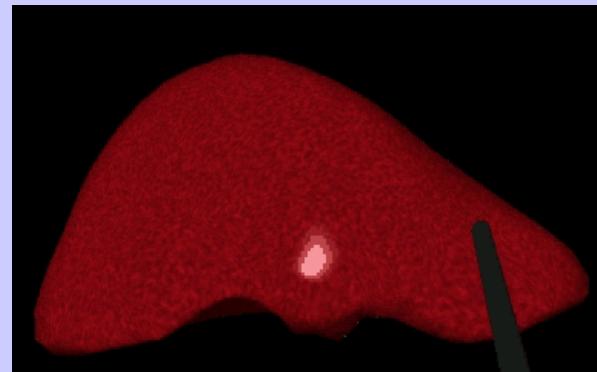
# Modeling Levels



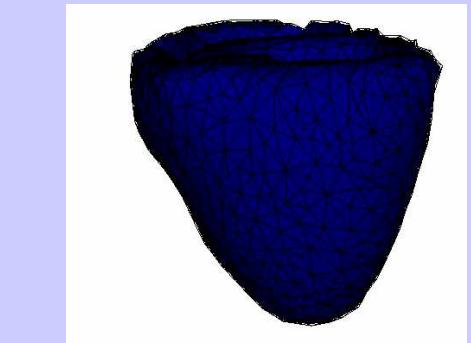
*Anatomy*



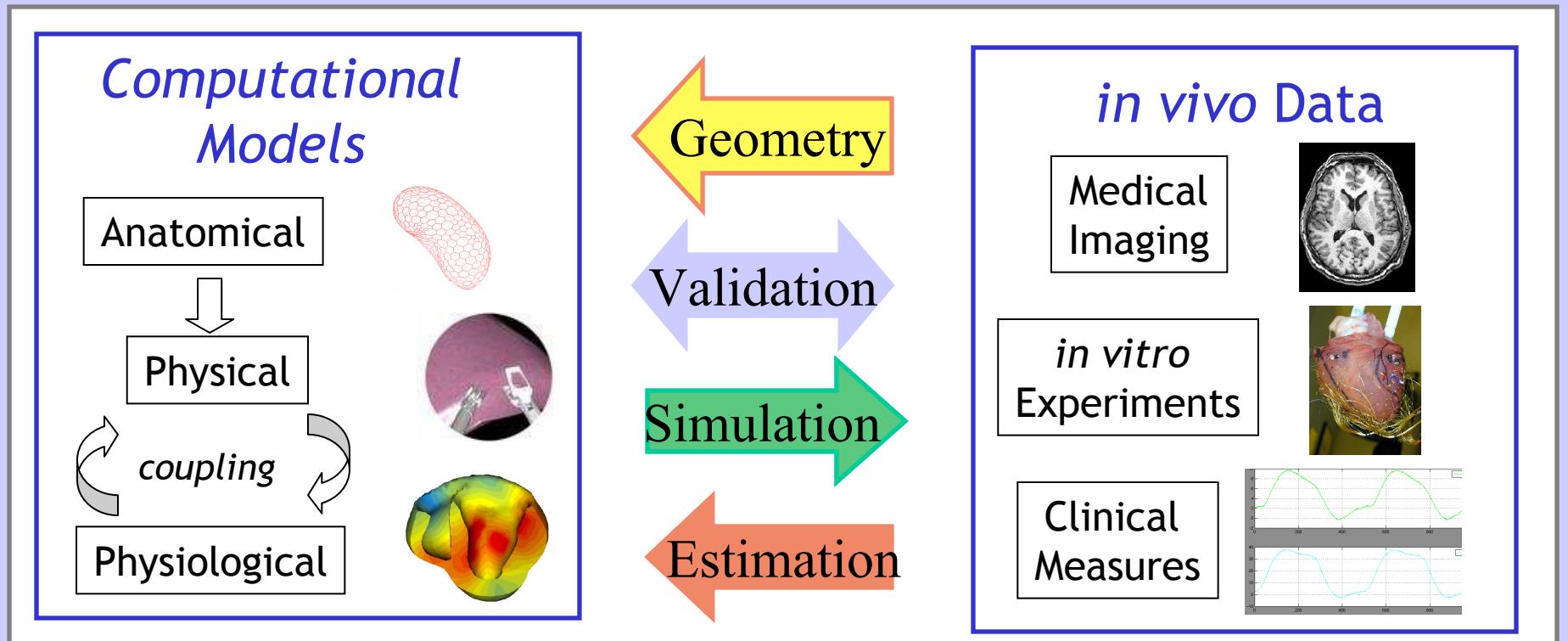
*Physics*



*Physiology*



# Modeling and Imaging



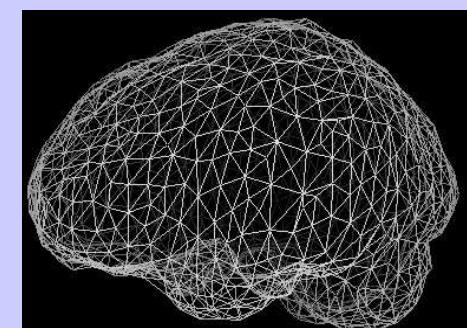
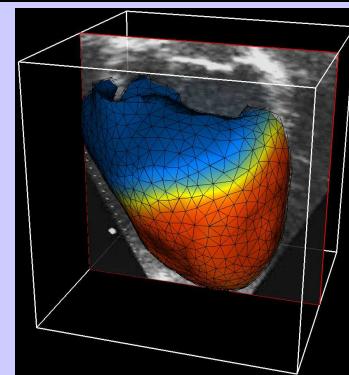
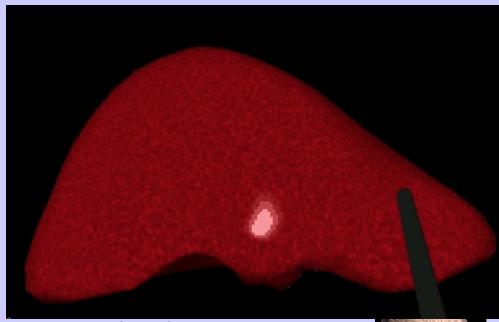
Mesh construction from medical images



# Example of Computational Models of the Human Body

- 3 applications of human modeling

| Application Type             | Organ | Real/Time Constraint | Image Interaction  | Physiological Modeling |
|------------------------------|-------|----------------------|--------------------|------------------------|
| Surgery Simulation           | Liver | Yes                  | Validation         | No                     |
| Diagnosis & Therapy Planning | Heart | No                   | Image Segmentation | Yes                    |
| Prediction of outcome        | Brain | No                   | Validation         | No                     |

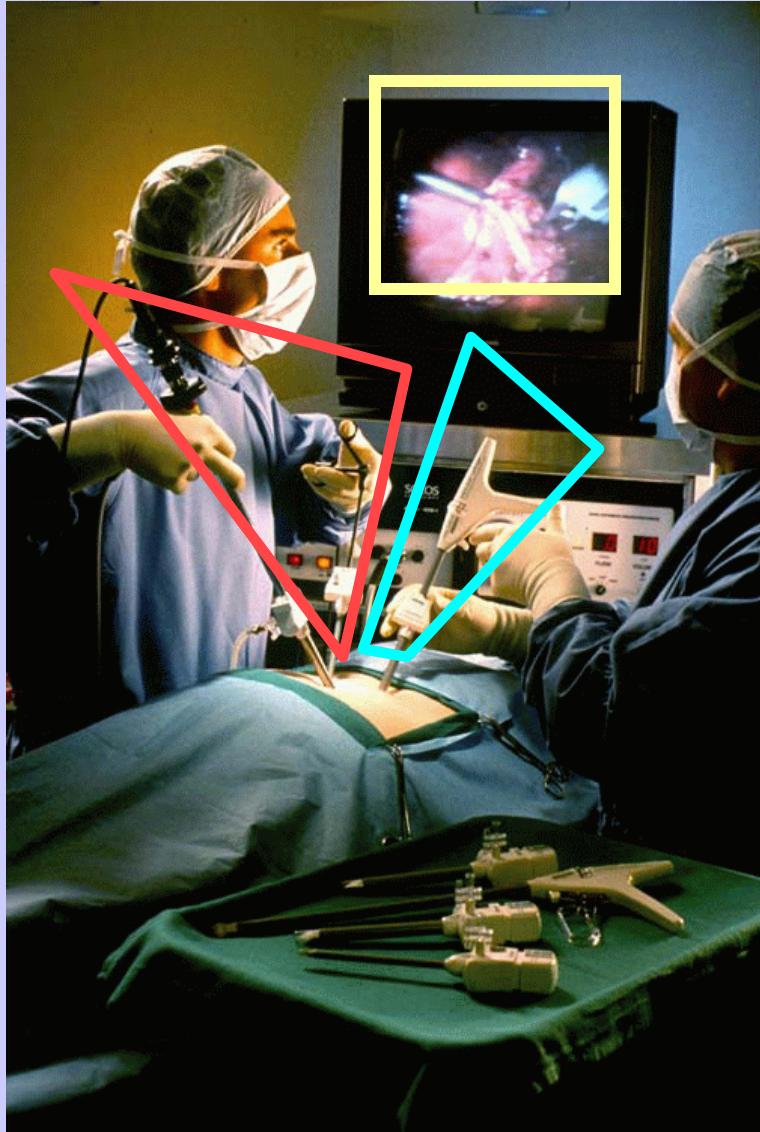


# Surgery Simulation

## Acknowledgments:

- Clément Forest, Guillaume Picinbono, Stéphane Cotin, Jean-Christophe Lombardo, Nicholas Ayache
- INRIA projects member of the AISIM collaborative action (Imagis,
- Sharp,Macs)
- IRCAD

# Need for Training



Hand-eye  
Synchronisation

Camera being  
manipulated by an  
assistant

Long instruments  
going through a fixed  
point in the abdomen

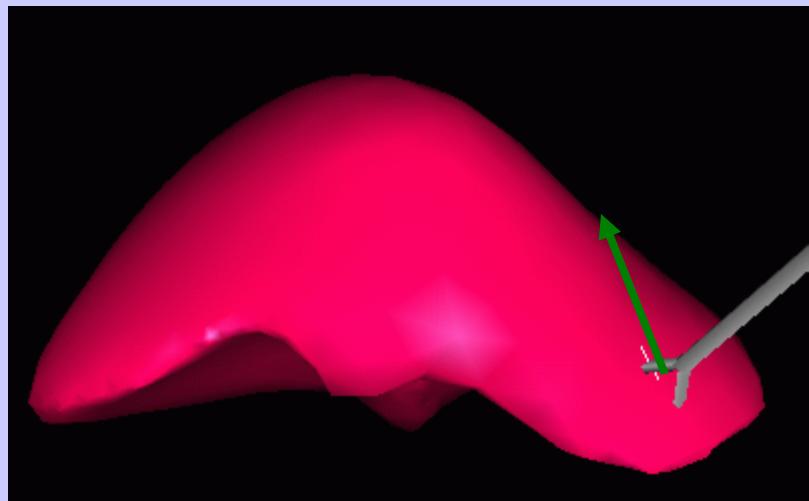
# EPIDAURE SIMULATION

[Cotin, 1997] [Picinbono, 2001] [Forest 2003]

- Hepatectomy Simulation by laparoscopy
- Includ



# Simulator Workflow



Position



Collision

Contact

Deformation

Force

Force

# Different Technical Issues

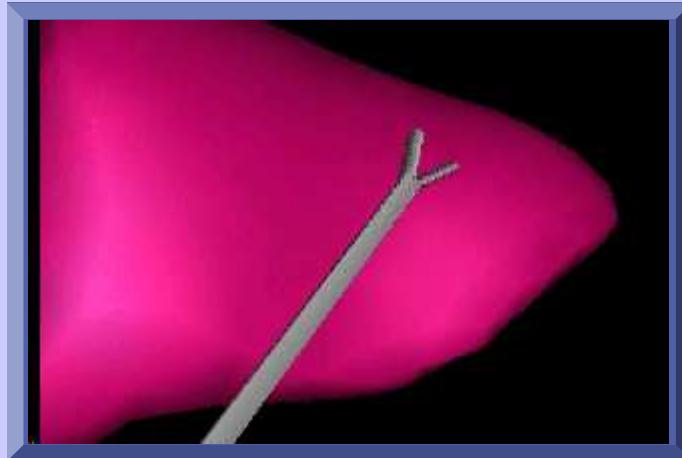
- Mesh Reconstruction from Images
- Soft Tissue Modeling
- Tissue Cutting
- Collision Detection
- Contact Modeling
- Surface Rendering
- Haptic Feedback



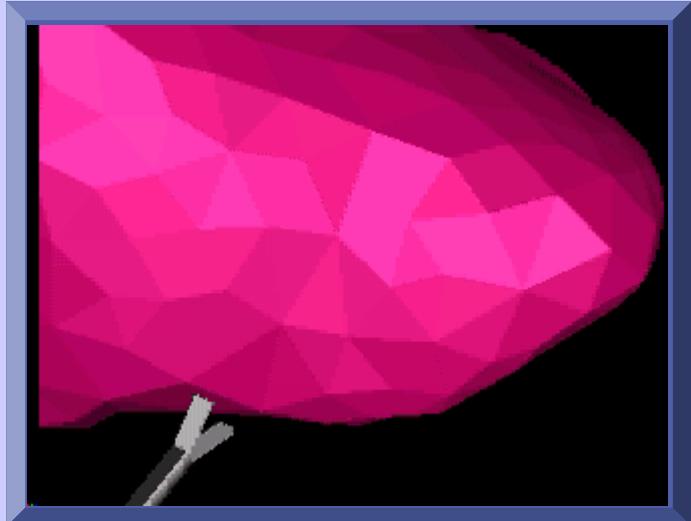
# Modeling basic surgical gesture



Gliding



Gripping



08/02/2006  
Cutting (pliers)



Cutting (NRSJA)  
SOPHIA ANTIPOLIS

# A Family of Models (1/3)

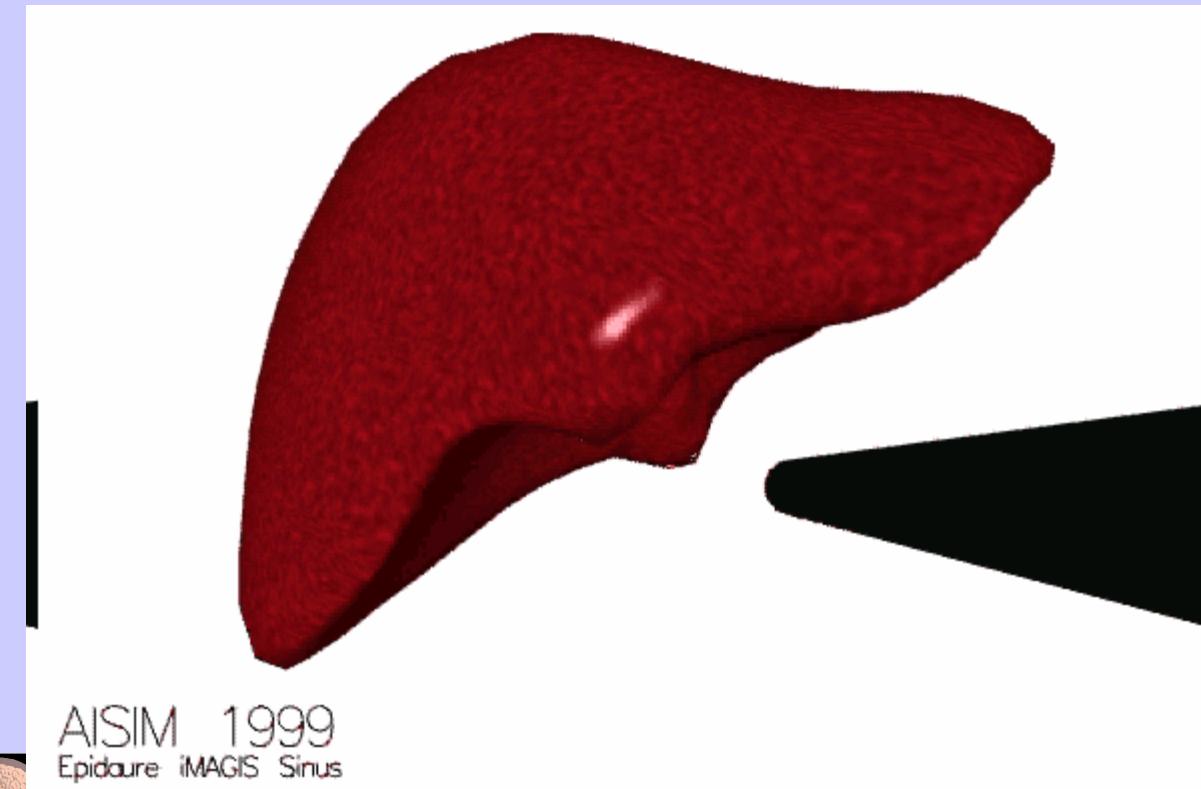
Pre-computed Linear  
Elastic Model



Very Fast



No topology changes



# A Family of Models (2/3)

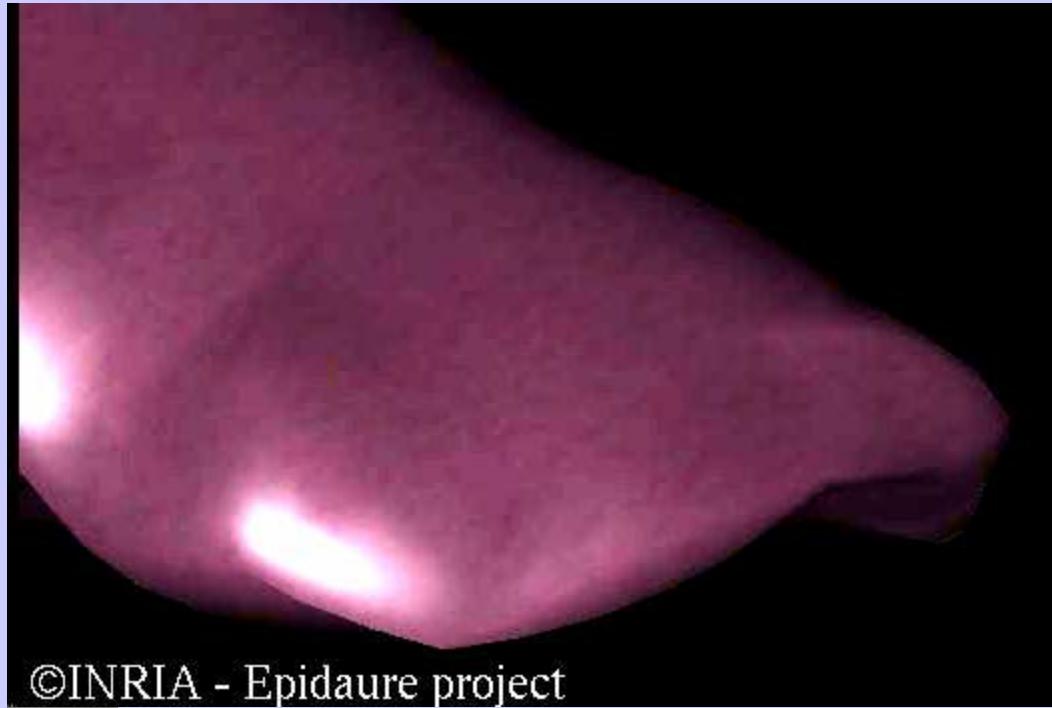
Elastic Model  
« Tensor-Mass »



Topology Changes



Limited to small displacements



©INRIA - Epidaure project



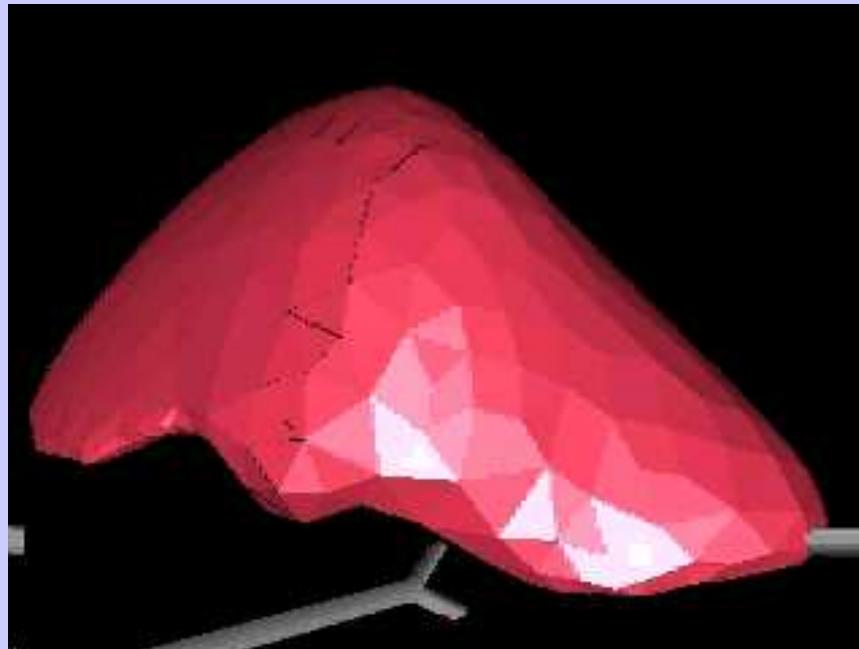
# A Family of Models (3/3)

Non-Linear Elastic  
Model

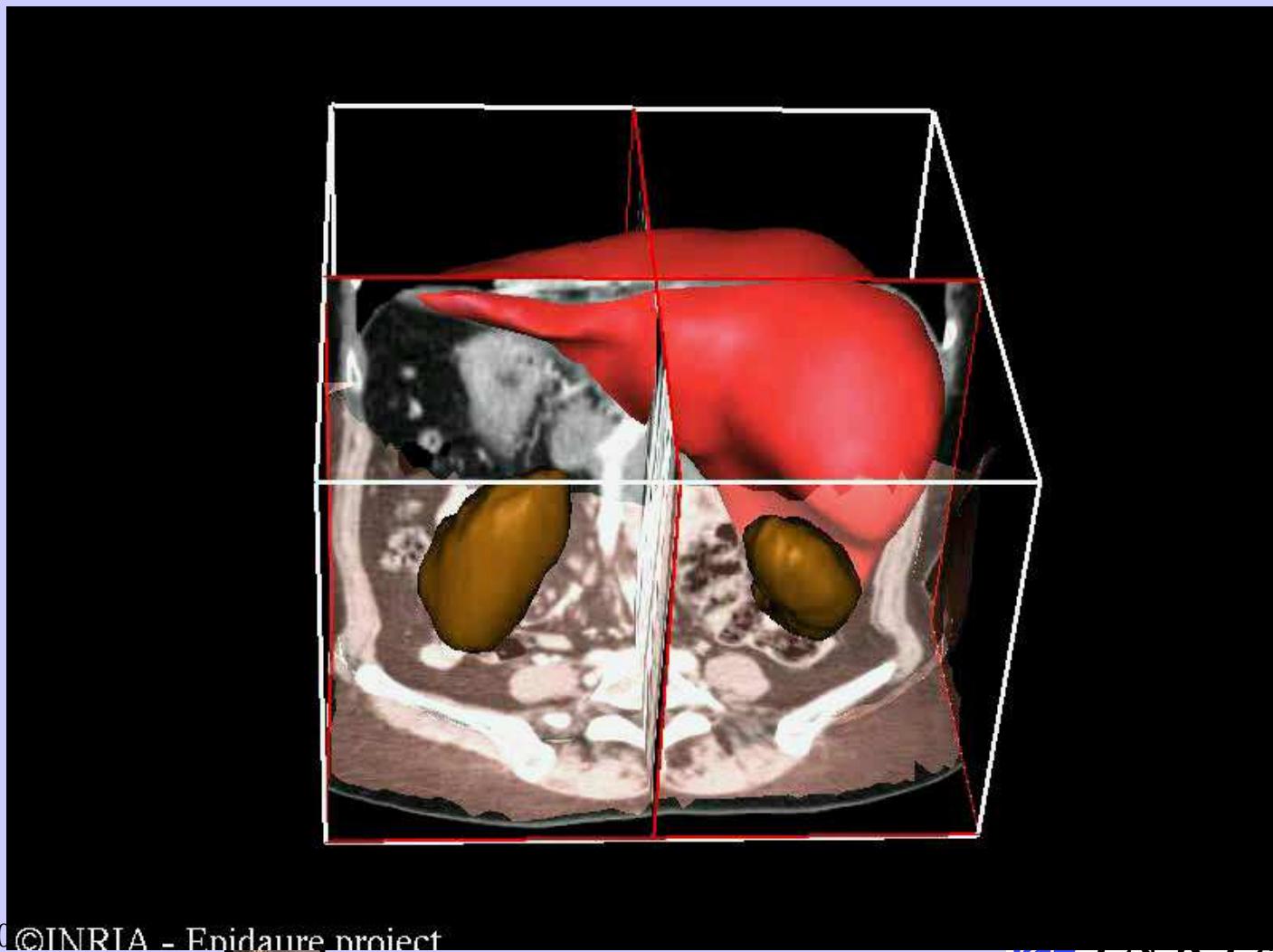


Large Displacements

Small Deformations



# Complete Simulation



# Cardiac Modeling

CARDIOSENSE3D

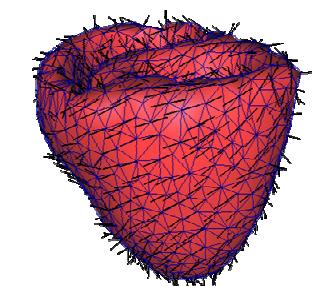
<http://www.inria.fr/CardioSense3D>

## Acknowledgments:

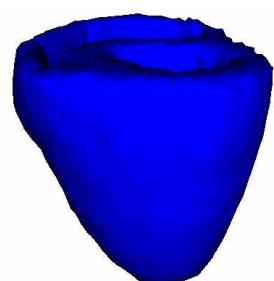
- Maxime Sermesant, Valérie Moreau, Nicholas Ayache
- INRIA projects member of the ICEMA collaborative action (Sosso, Macs, Caiman, University of Nantes),
- NIH (Elliott Mc Veigh), Guy's Hospital (D. Hill)
- Philips Research France

# Electromechanical Model of the Heart

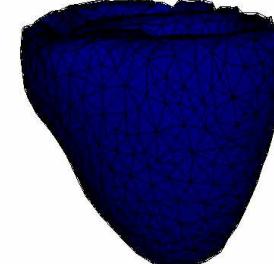
Anatomical Model



Electrical Model



Electro mechanical Coupling



08/02/2006



*pathology simulation  
intervention planification*

## Parameters

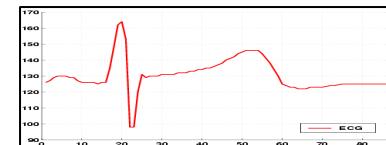
*cardiac function :*

- *ejection fraction*
- *wall thickness*
- *strain, stress*

## Medical Simulator

## Patient Data

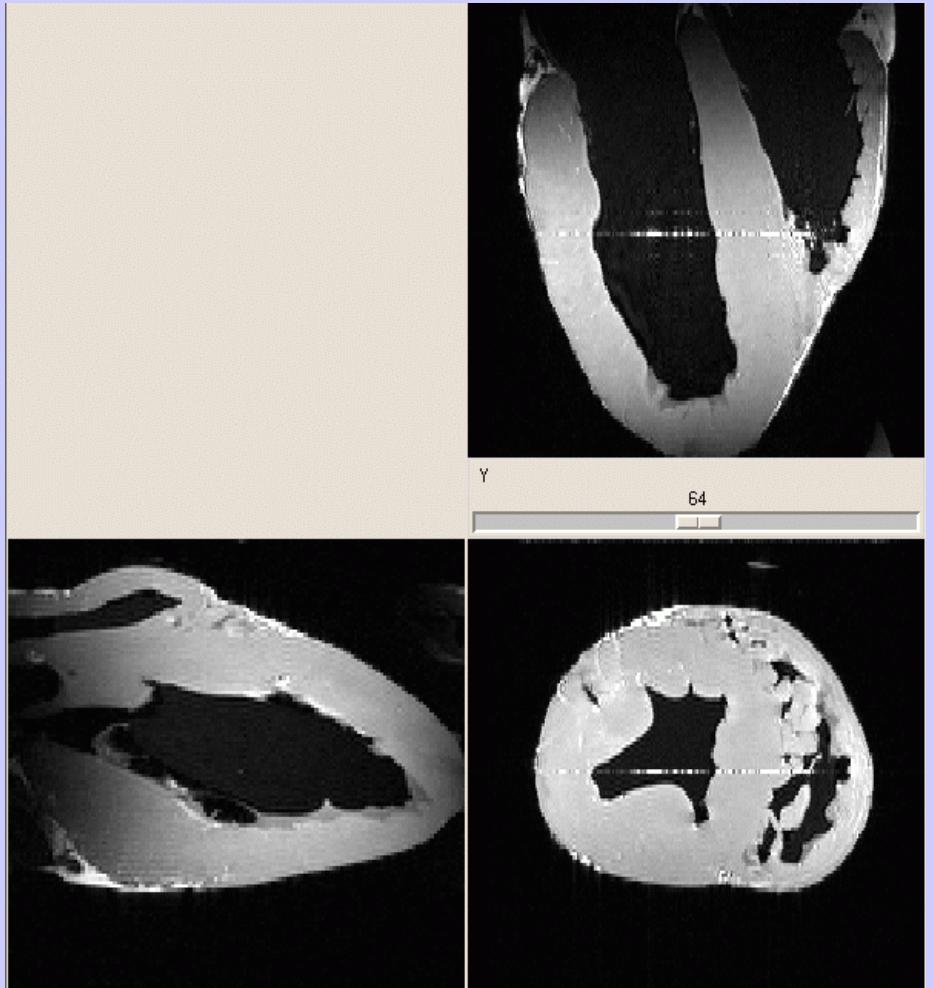
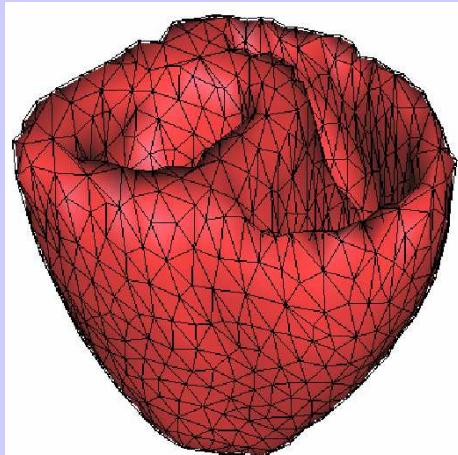
ElectroCardioGram



# Myocardium Geometry

- Obtained from High Resolution Post-Mortem MRI of canine heart

Courtesy of Hsu, Duke University

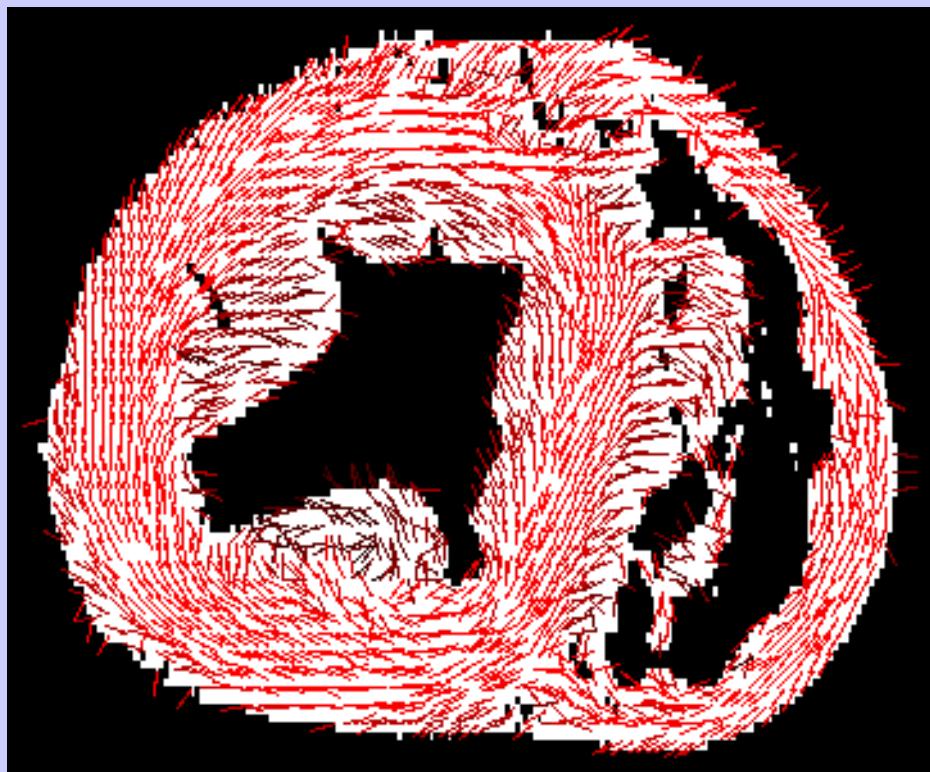


*Other Data available, Courtesy of P. Hunter, Auckland University*



# Fiber Directions (canine Data)

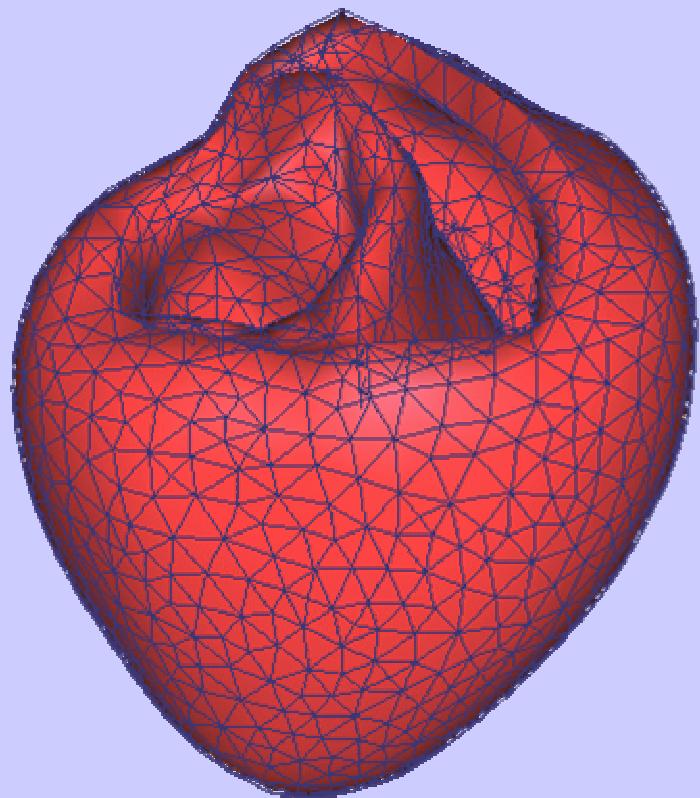
- From high resolution Diffusion Tensor MRI



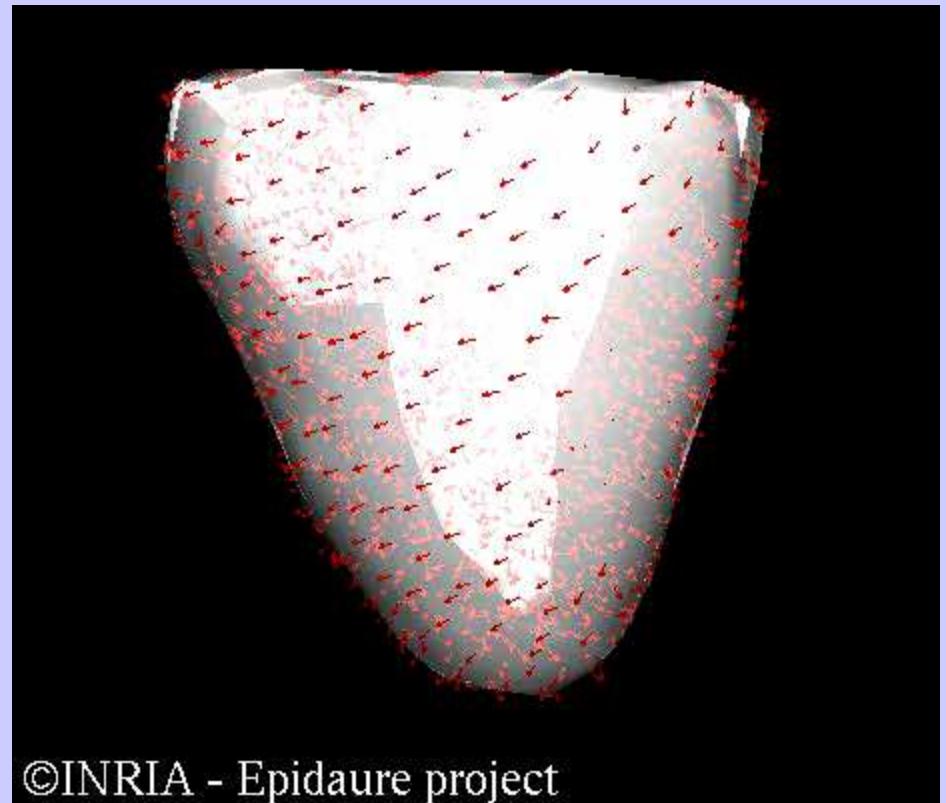
E.W. Hsu and C.S. Henriquez, *Myocardial fiber orientation mapping using reduced encoding diffusion tensor imaging*, Journal of Cardiovascular Magnetic Resonance, 2001.



# Geometrical Model of Human Heart



Finite Element Mesh



©INRIA - Epidaure project

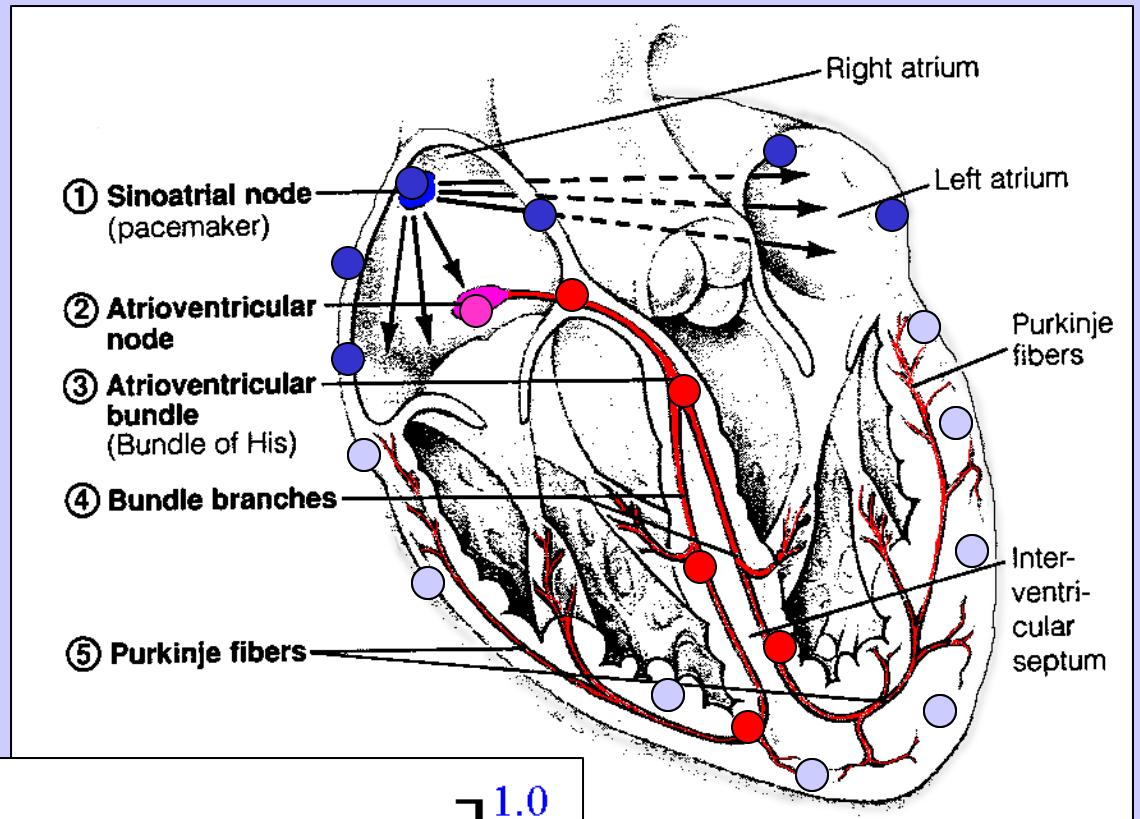
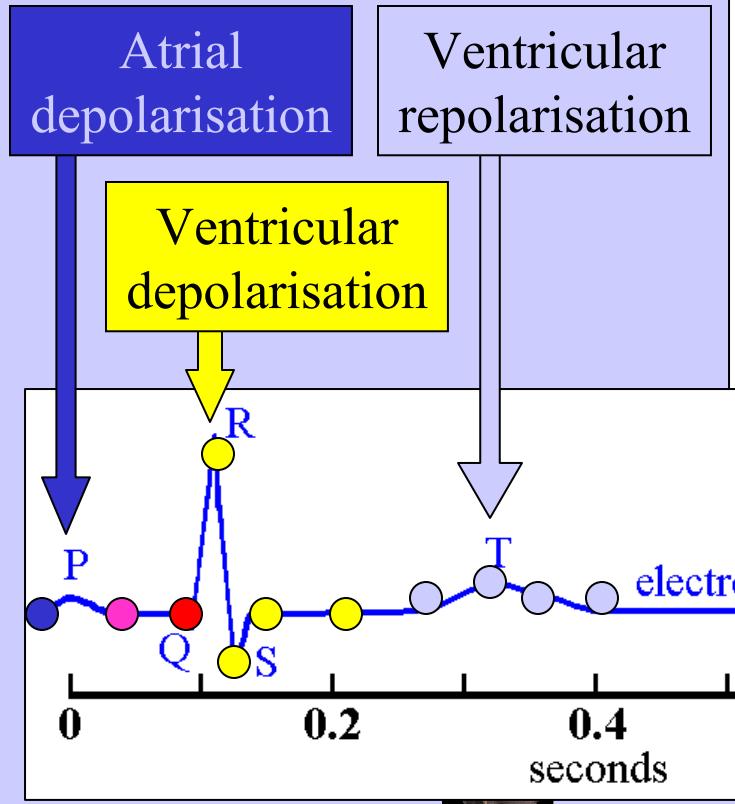
Fiber Directions

# Different Levels of Modeling

- Geometrical Modeling
- Electrical Propagation
- Mechanical Coupling
- Parameter Identification



# Heart Electrical Activity



# Electrical Model

- Action potential  $u$  computation: 2 variables  
FitzHugh-Nagumo *Reaction-Diffusion* system

$$\begin{cases} \frac{\partial u}{\partial t} = \operatorname{div}(D \nabla u) + f(u) - z \\ \frac{\partial z}{\partial t} = b(u - cz) \end{cases}$$

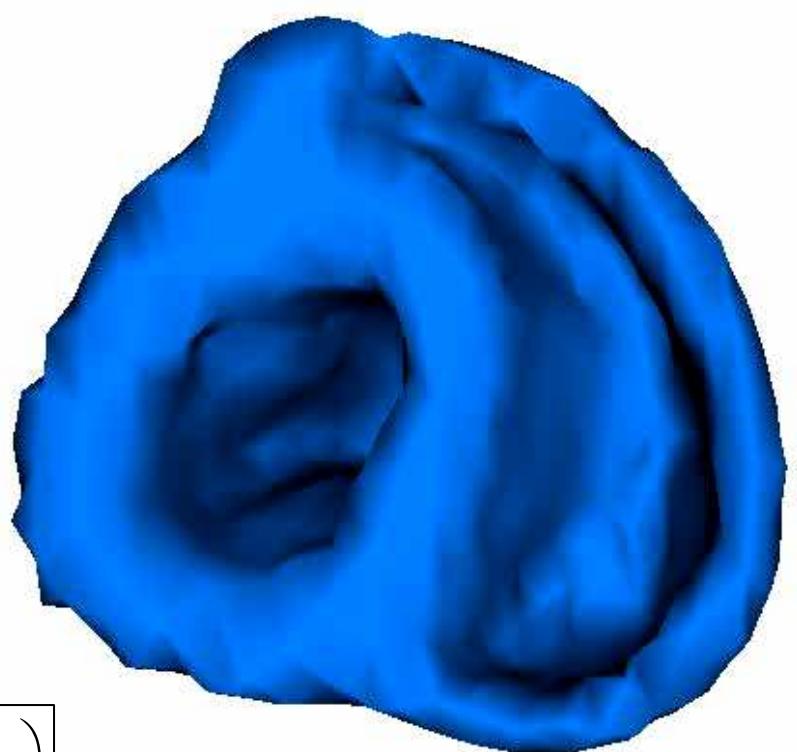
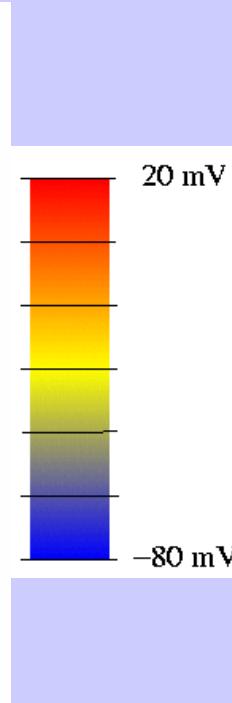
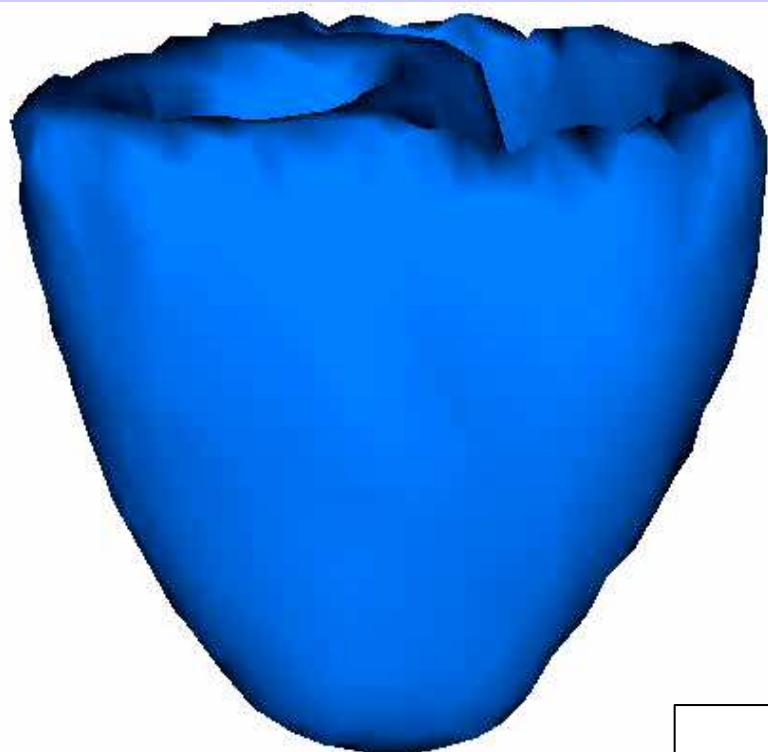
$u$  action potential  
 $D$  diffusion tensor  
 $f$  ionic current  
 $z$  repolarization variable  
 $b$  repolarisation rate  
 $c$  repolarisation decay

Or R. Aliev and A. Panfilov : A Simple Two-variable Model of Cardiac Excitation, *Chaos, Solitons & Fractals*, Vol 7, No 3, pp. 293-301, 1996



# Electrical Simulation

Anisotropic model (fiber geometry + Purkinje network)

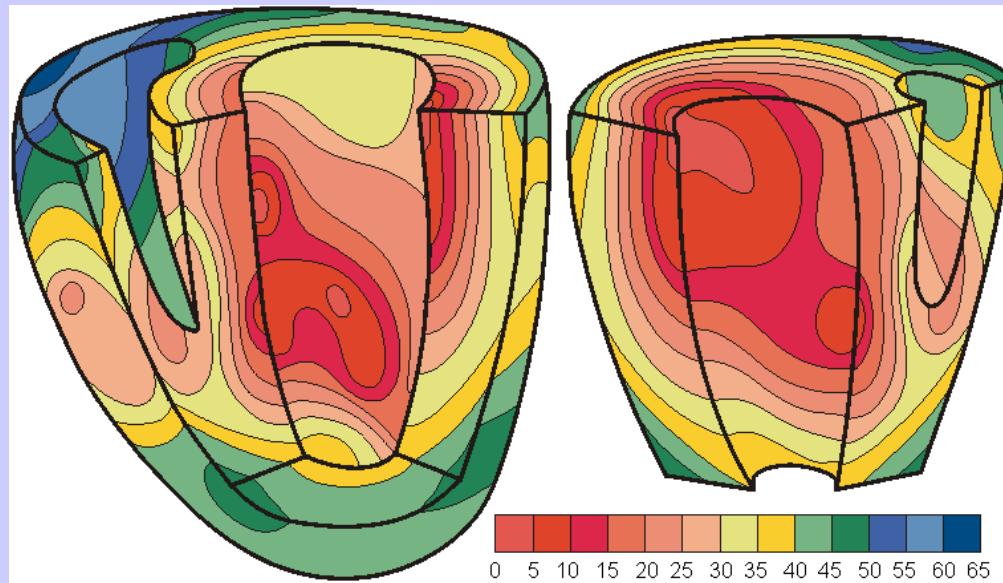


$$D = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0.25 & 0 \\ 0 & 0 & 0.25 \end{pmatrix}$$

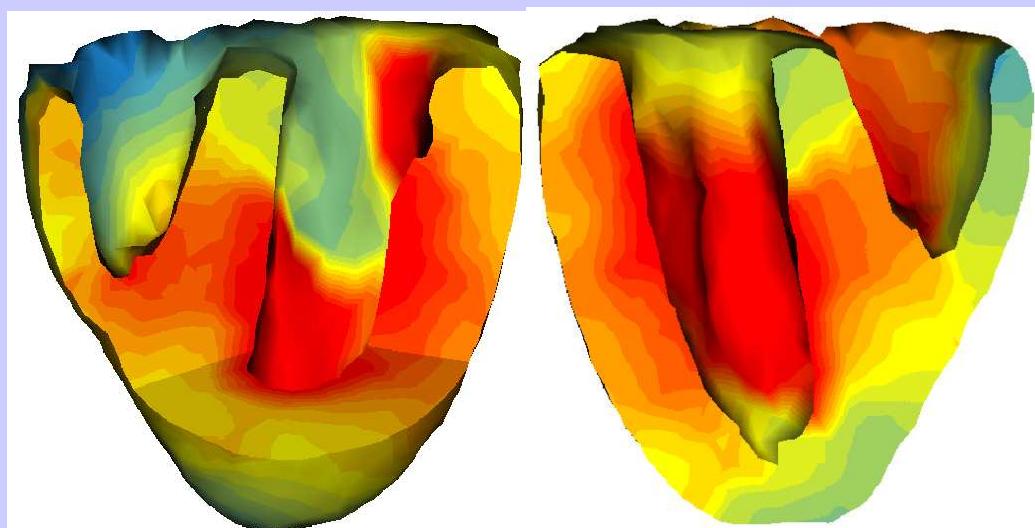


# Comparison of Isochrones

Durrer et al.



ICEMA at INRIA



107

08/02/2006



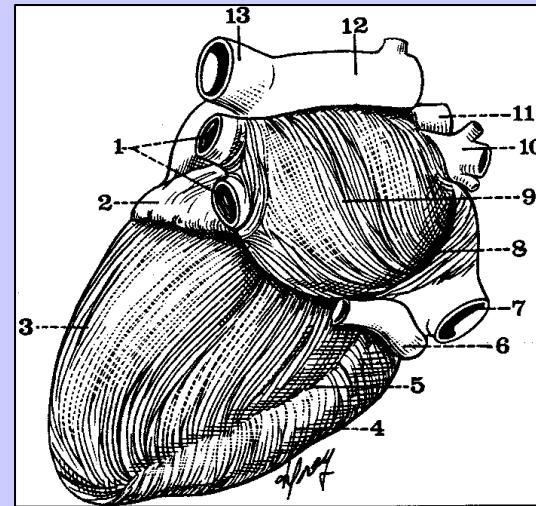
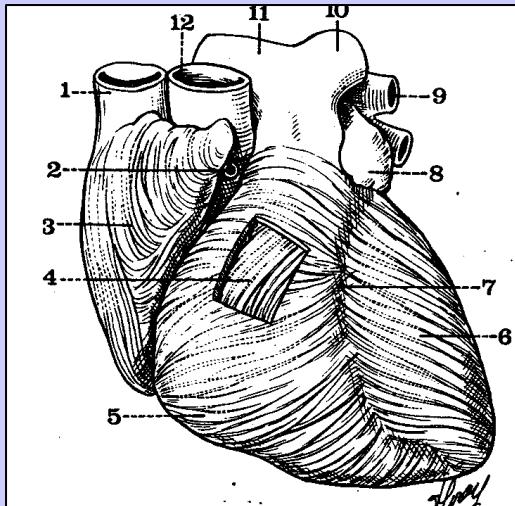
# Different Levels of Modeling

- Geometrical Modeling
- Electrical Propagation
- Mechanical Coupling
- Parameter Identification



# Biomechanical Properties

The myocardium is composed of muscle fibre bundles:



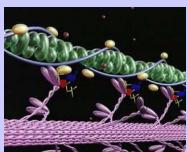
It is an active **non-linear viscoelastic**  
**anisotropic incompressible** material.

# Excitation-Contraction Coupling

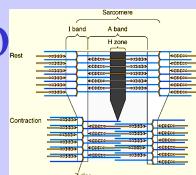
*From Bestel-Clément-Sorine, MICCAI'01*

Scale:

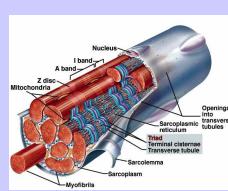
Nano



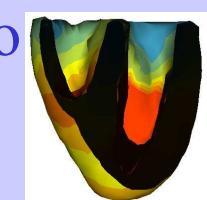
Micro



Meso



Macro



System:  
molecular motors

*Langevin equations*

(SDE) Ratchet or Power-stroke models

sarcomeres

*Huxley-like models*

(PDE)

myocytes

*BCS model*

(ODE)

myocardium

*dynamics equations*

(PDE with BCS Constitutive Law)

Control:

Calcium ions

*still to be designed...*

ionic currents

*Luo-Rudy-like models*

(ODE)

action potential

*FHN-like models*

(ODE)

action potential

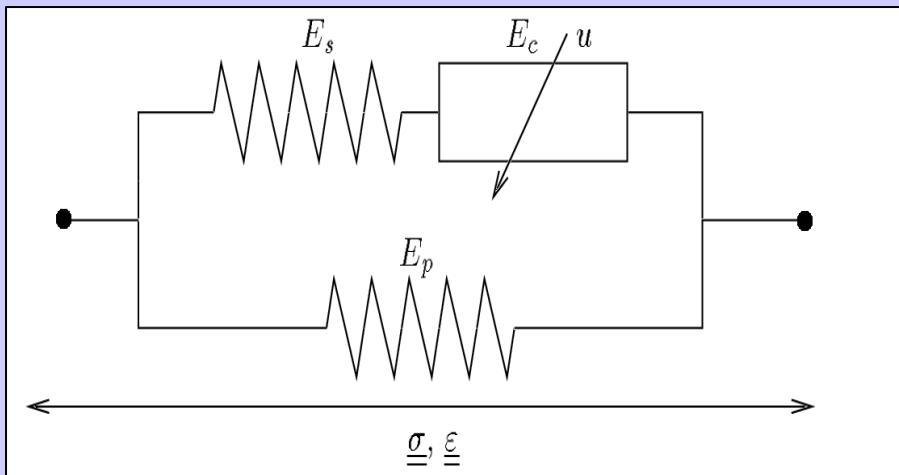
*FHN-like models*

(PDE)



# Electro-Mechanical Coupling

- Derived from nano to macroscopic scale
- Bestel-Clément-Sorine constitutive law in Hill-Maxwell type rheological model



$E_s$  series element  
 $E_p$  parallel element  
 $E_c$  contractile element  
 $u$  action potential  
 $\sigma$  stress  
 $\varepsilon$  strain

- $E_s$  and  $E_p$ : elastic material laws,
- $E_c$  contractile electrically-activated element.

J. Bestel, F. Clément, and M. Sorine. A Biomechanical Model of Muscle Contraction. In *Medical Image Computing and Computer-Assisted Intervention* (MICCAI'01), 2001.



# Bestel-Clément-Sorine Myofiber Model

Electromechanical coupling system derived from  
*nanoscopic to mesoscopic scale*

$$\begin{cases} \frac{dk_c}{dt} = -\left(|u| + \left|\frac{d\epsilon_c}{dt}\right|\right)k_c + k_0|u|_+ \\ \frac{d\sigma_c}{dt} = -\left(|u| + \left|\frac{d\epsilon_c}{dt}\right|\right)\sigma_c + k_c \frac{d\epsilon_c}{dt} + \sigma_0|u|_+ \end{cases}$$

$k_c$  contractile stiffness  
 $u$  electrical action potential

$\epsilon_c$  contractile strain  
 $\sigma_c$  contractile stress

J. Bestel, F. Clément, and M. Sorine. A Biomechanical Model of Muscle Contraction. In *Medical Image Computing and Computer-Assisted Intervention (MICCAI'01)*, 2001.

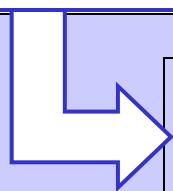


# $F_c$ : Simplified electromechanical model for image segmentation

$k$  piecewise constant

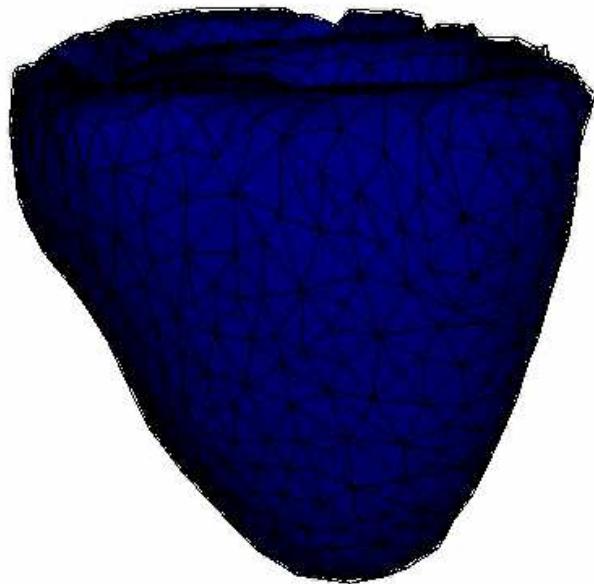
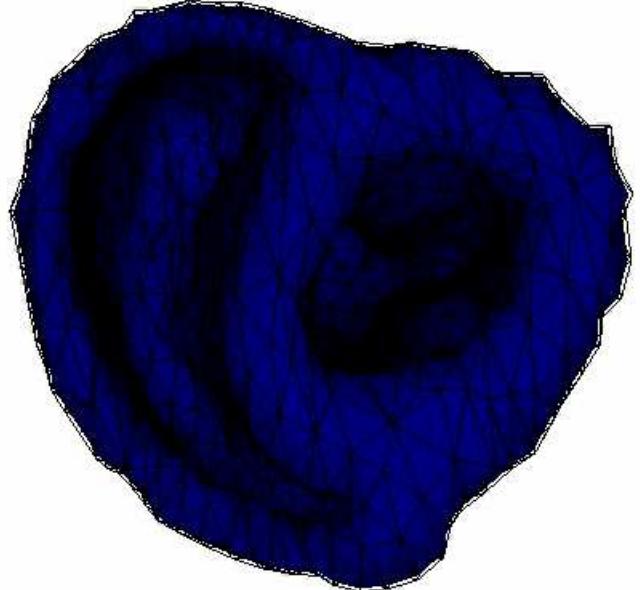
$$\frac{d\sigma_c}{dt} = -|u| \sigma_c + \sigma_0 |u|_+$$

Piecewise  
linear  
viscoelastic  
anisotropic  
material

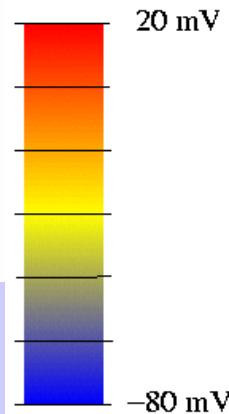


Only electrical command on  
contraction stress  $\sigma_c$





08/02/2006



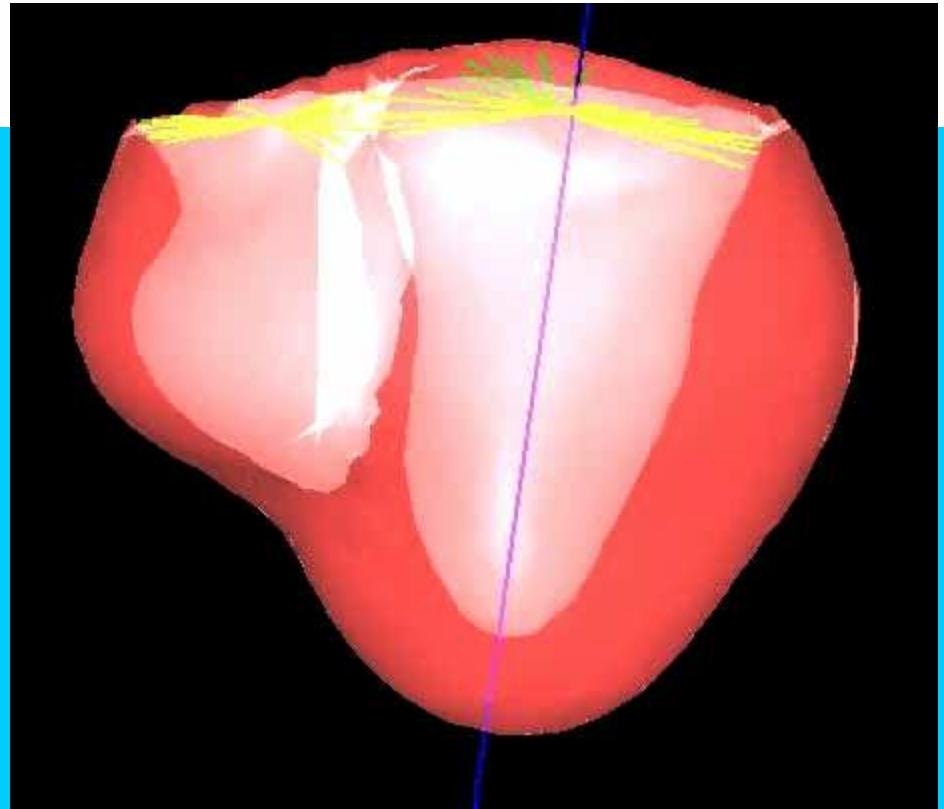
# Electro-Mechanical coupling

- the “Action potential”  $u$  controls contractile element:
  - $u > 0$  : Contraction
  - $u \leq 0$  : Relaxation
- $u$  also modifies stiffness  $k$  of the material.

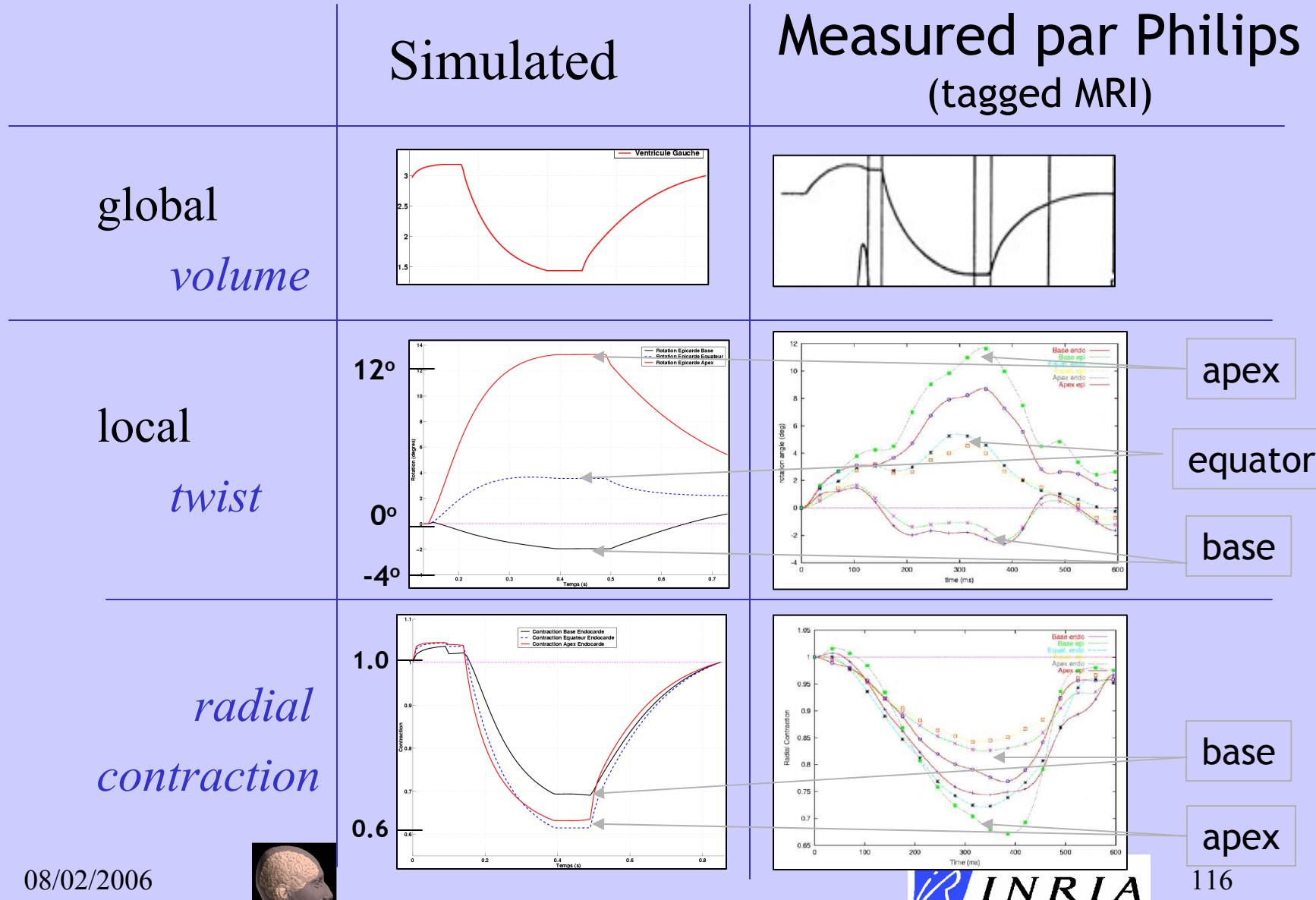
- Ayache-Chapelle-Clément-Coudière-Delingette-Sermesant-Sorine-FIMH'01
- Sermesant-Coudière-Delingette- et al., MICCAI'02

# Cardiac Cycle Simulation

- 4 phases :
  - filling
  - isovolumetric contraction
  - ejection
  - isovolumetric relaxation
- 2 Boundary Conditions :
  - Pressure constraint on the endocardium
  - Isovolumetric constraint on the endocardium

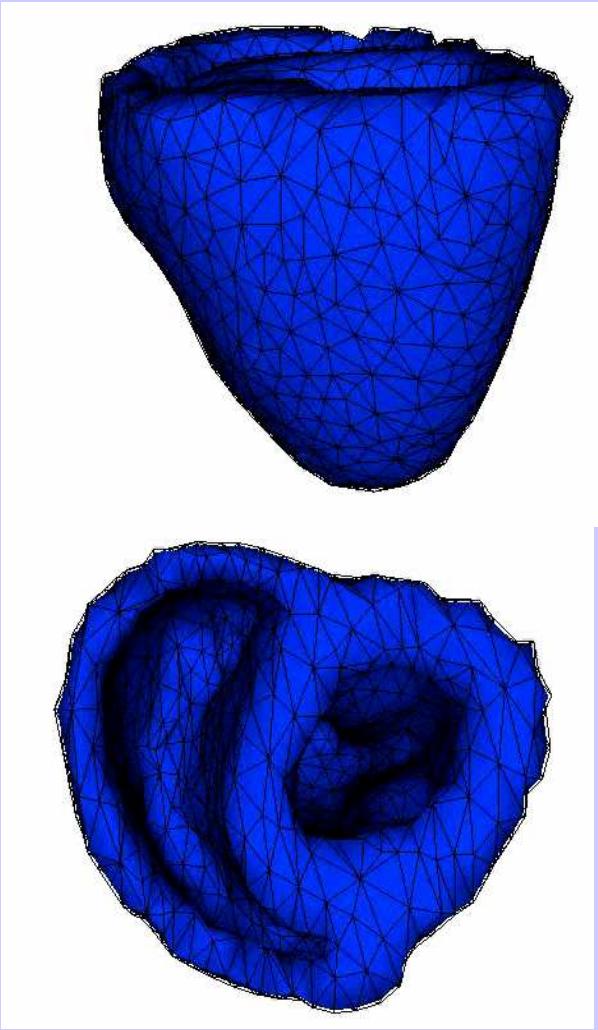


# Cardiac Cycle Parameters



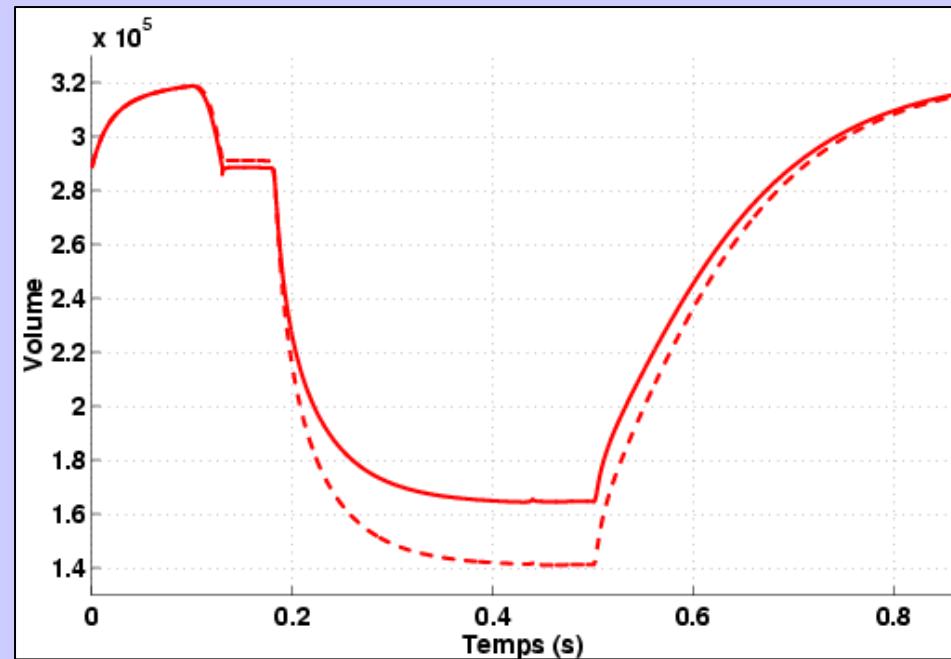
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*Infarcted zone  
simulation*

# Simulating an Infarct

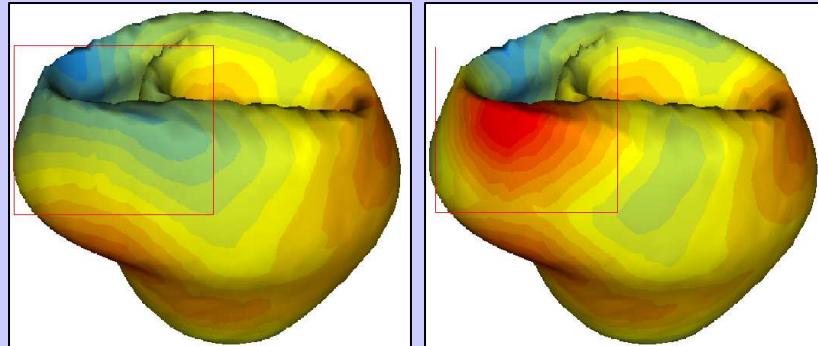


ejection fraction:  
**56 % → 48 %**

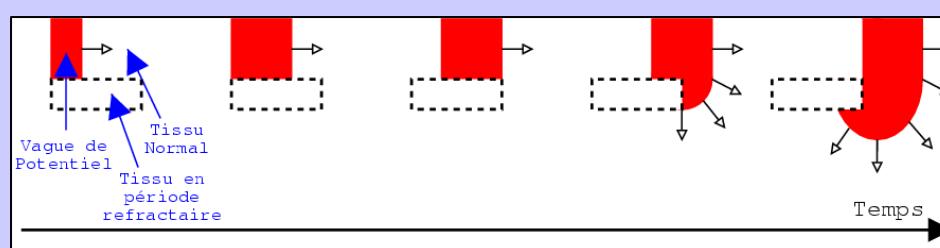
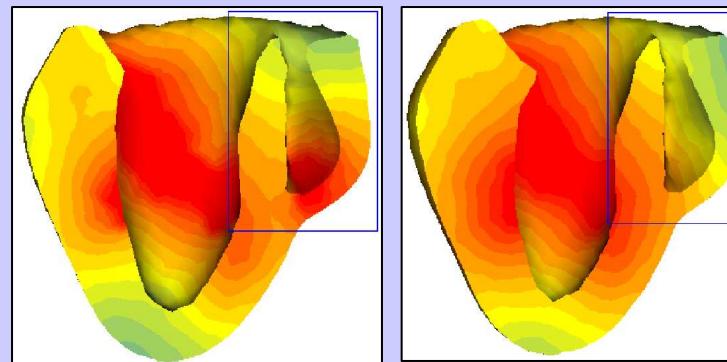


# Simulating Electrical Pathologies

- Ectopic Focus in RV
  - Wolff-Parkinson-White

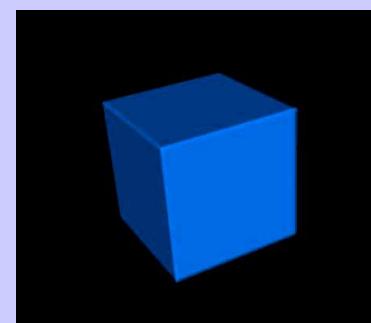


- Bundle of His defect in RV
  - Right Branch Block
- Fibrillation



*Wave-break*

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# Brain Soft Tissue Modeling

## Acknowledgments:

- Olivier Clatz, Nicholas Ayache
- Hopital La Pitié Salpétrière (D. Dormont)
- Centre Antoine Lacassagne (P.-Y. Bondiau)
- Brigham and Women's Hospital (S. Warfield)

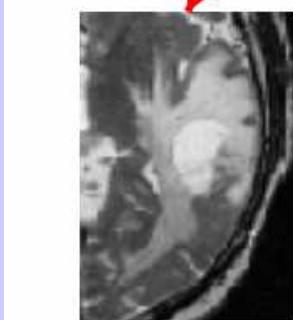
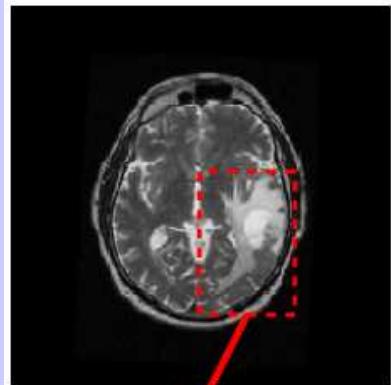
# Applications

- Glioblastoma growth modeling
  - Objectives :
    - Understanding tumor growth
    - Improve radiotherapy planning
- Brain-shift modeling
- Image registration based on biomechanical modeling



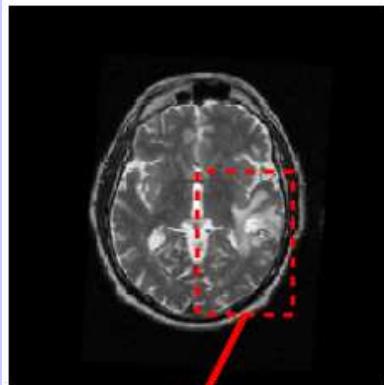
# Input Data (patient)

- 2x3 images acquired 6 months apart

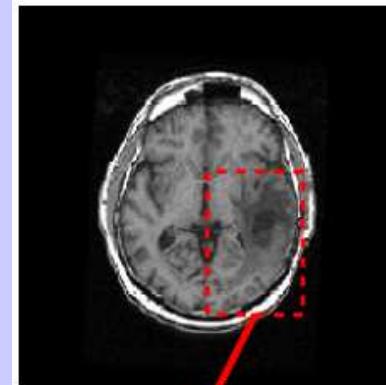


T2  
september

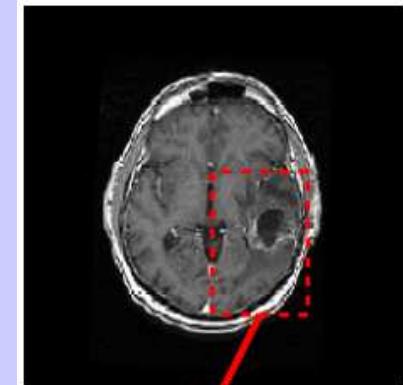
08/02/2006



T2  
march



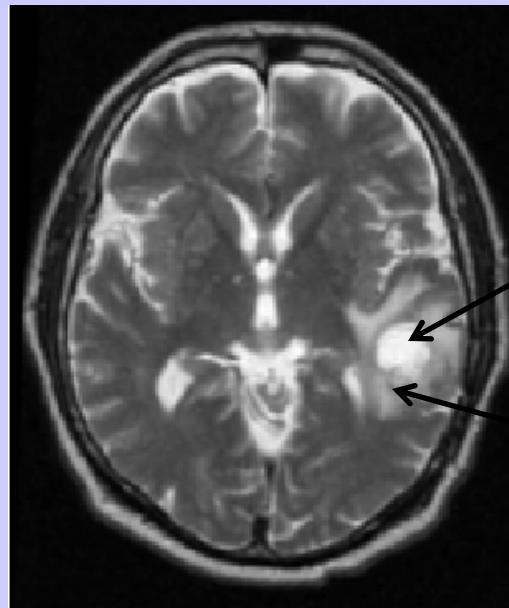
T1  
march



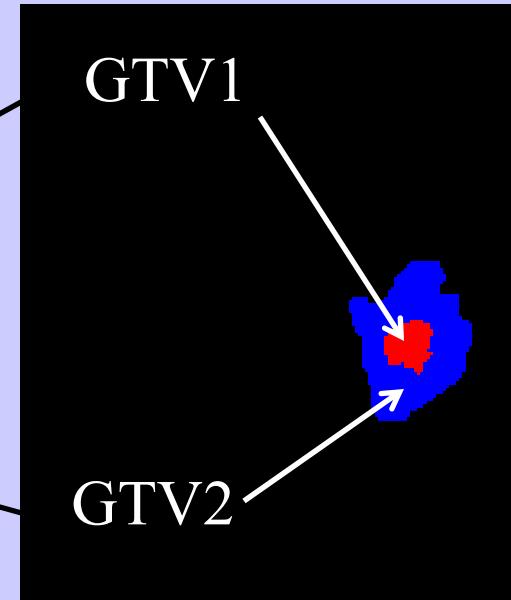
T1 + gad  
march

# Input Data (patient)

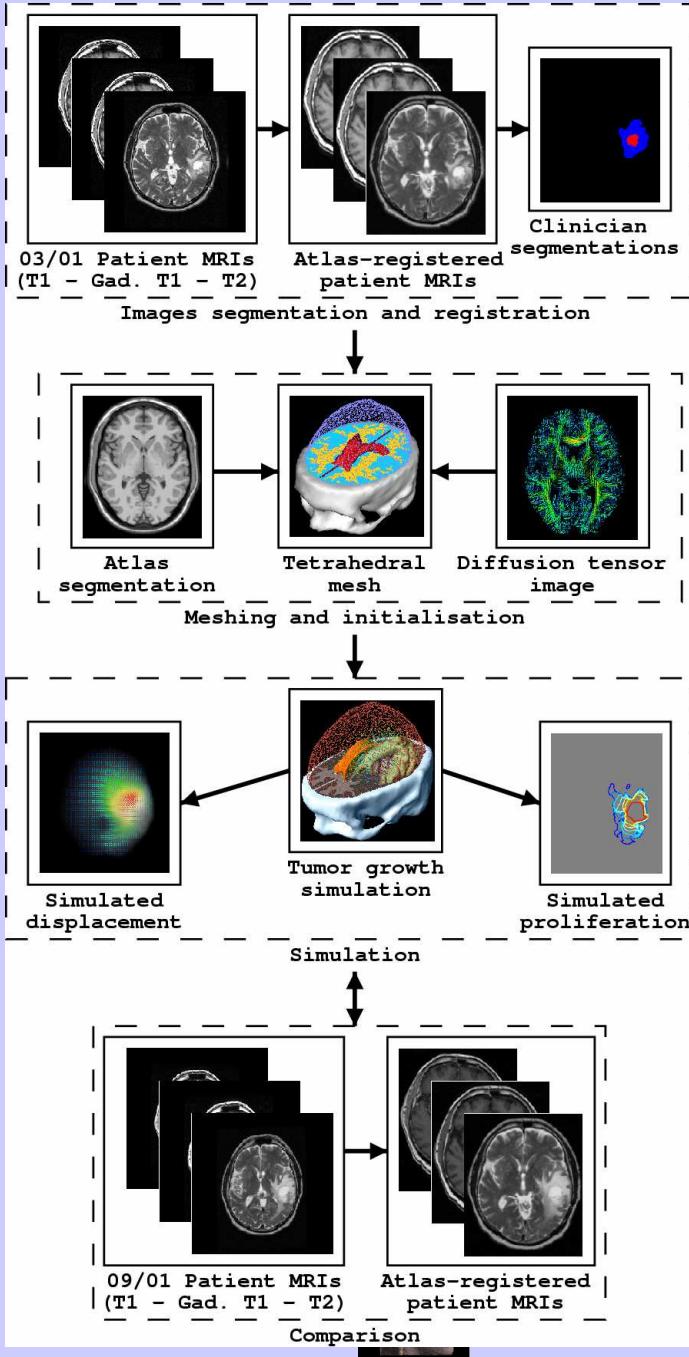
- Segmentation of target tissues



T2 MRI



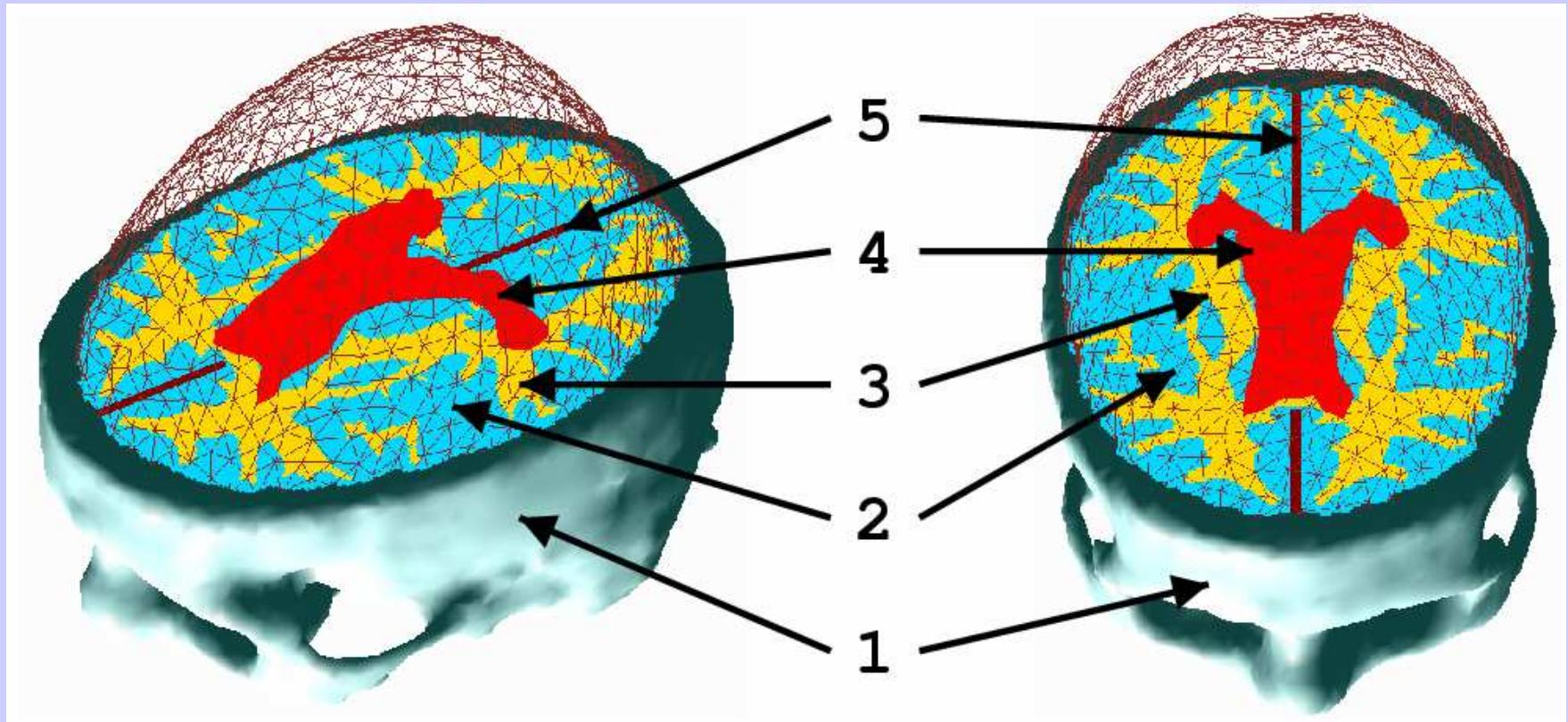
Segmentation GTVs



# Methods

- Images + segmentation
- Initialization with atlas
- FE Method
  - Diffusion
  - Mechanical
- Comparaison with patient

# Mesh Construction



1 Skull. 2 Grey Matter. 3 White Matter  
4 Ventricles. 5 Falx

# Model Equations

## Diffusion + source terms

$$\frac{\partial u}{\partial t} = \operatorname{div}(D \nabla u) + \rho u$$

u = density of tumor cells

D = Diffusion Tensor

$\rho$  = Source Term

## Mechanical Constitutive Law

Linear Elasticity :  $\sigma = k \varepsilon$

$\sigma$  = stress

$\varepsilon$  = strain :  $\varepsilon = \frac{1}{2}(\nabla x + \nabla x^t)$

k = stiffness

$F_{ext}$  = External force

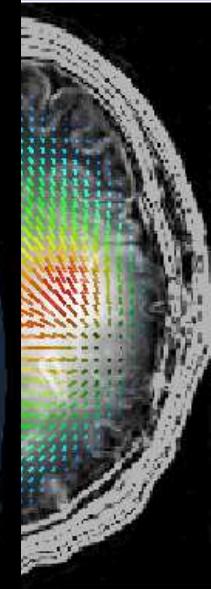
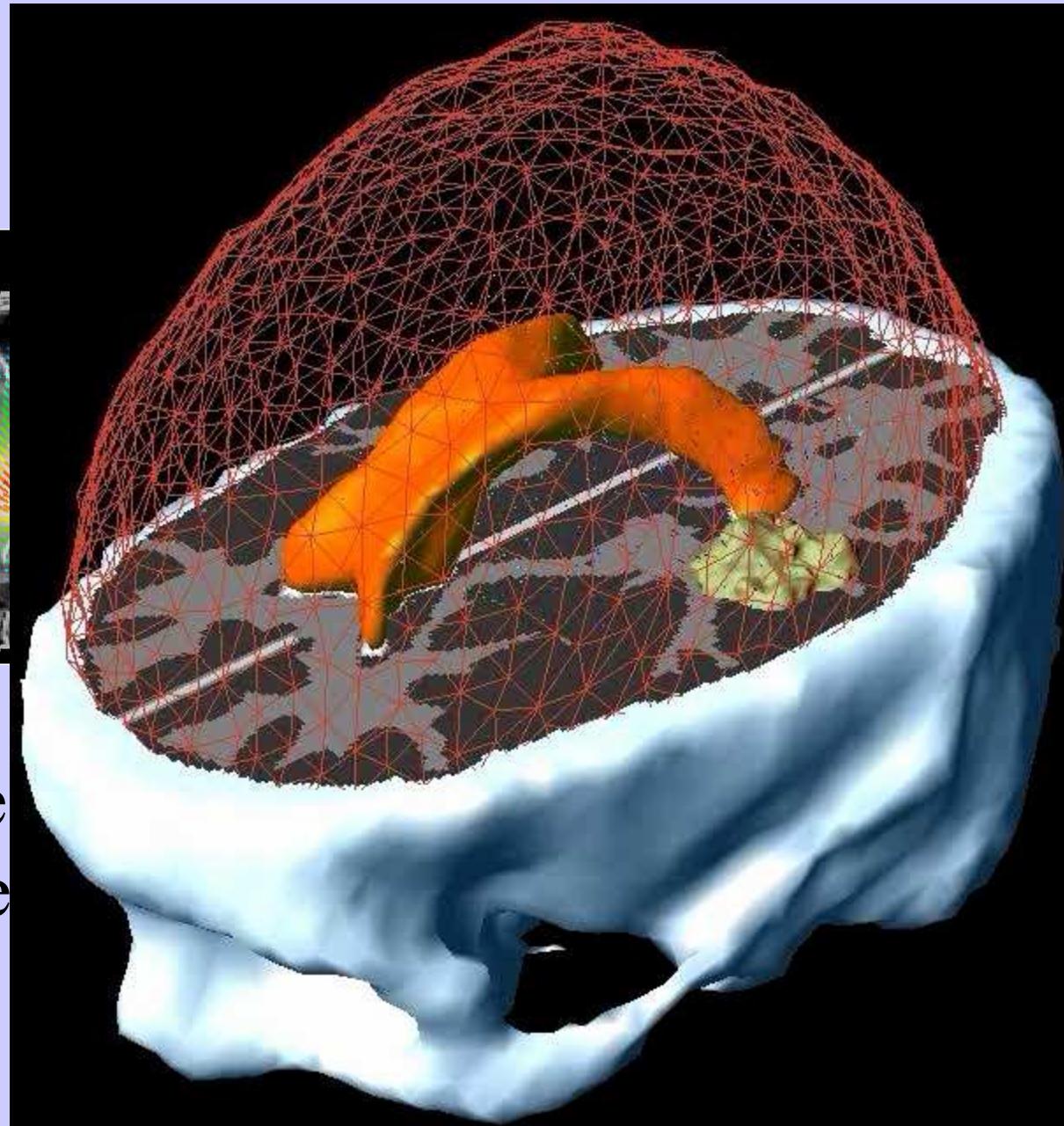
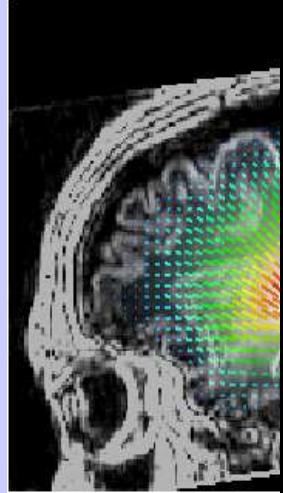
Équilibre :  $\operatorname{div} \sigma + F_{ext} = 0$

## Coupling

$$F_{ext} = \lambda \nabla u$$

$\lambda$  = coupling factor

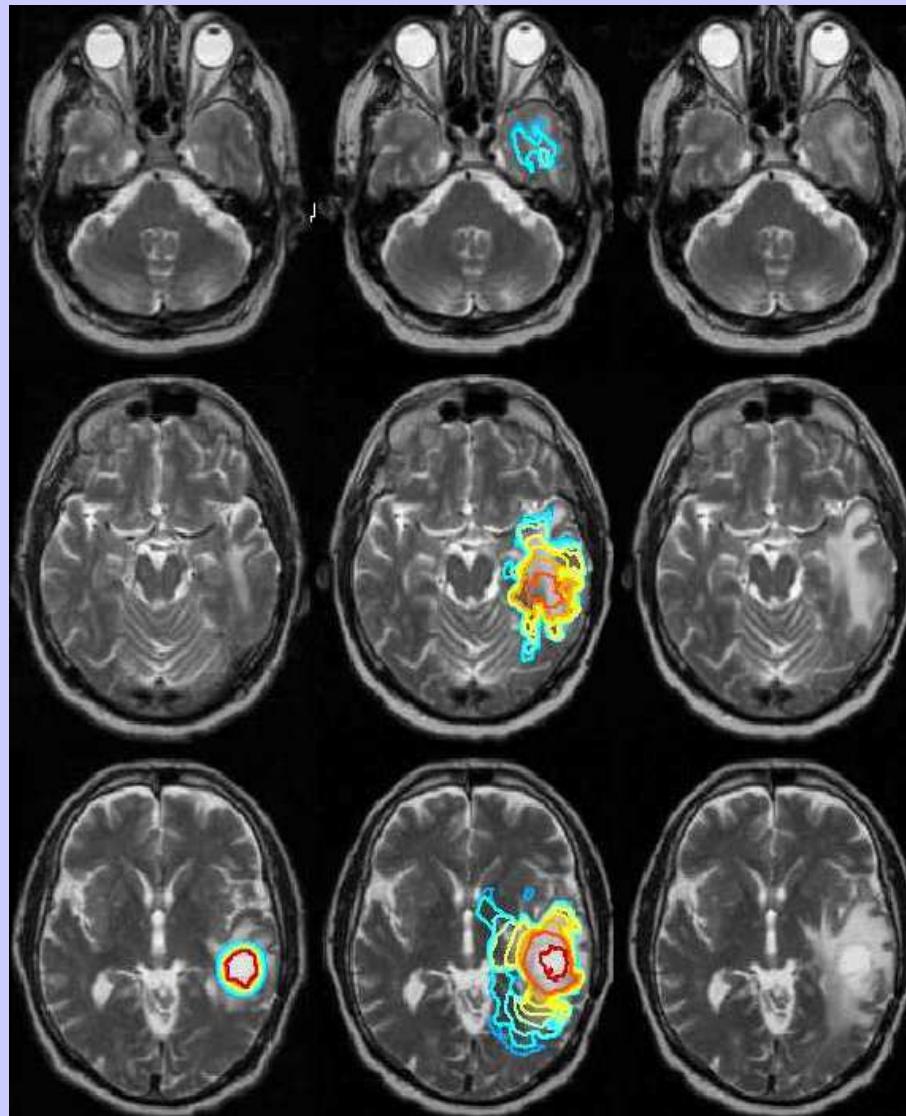




- Me ave

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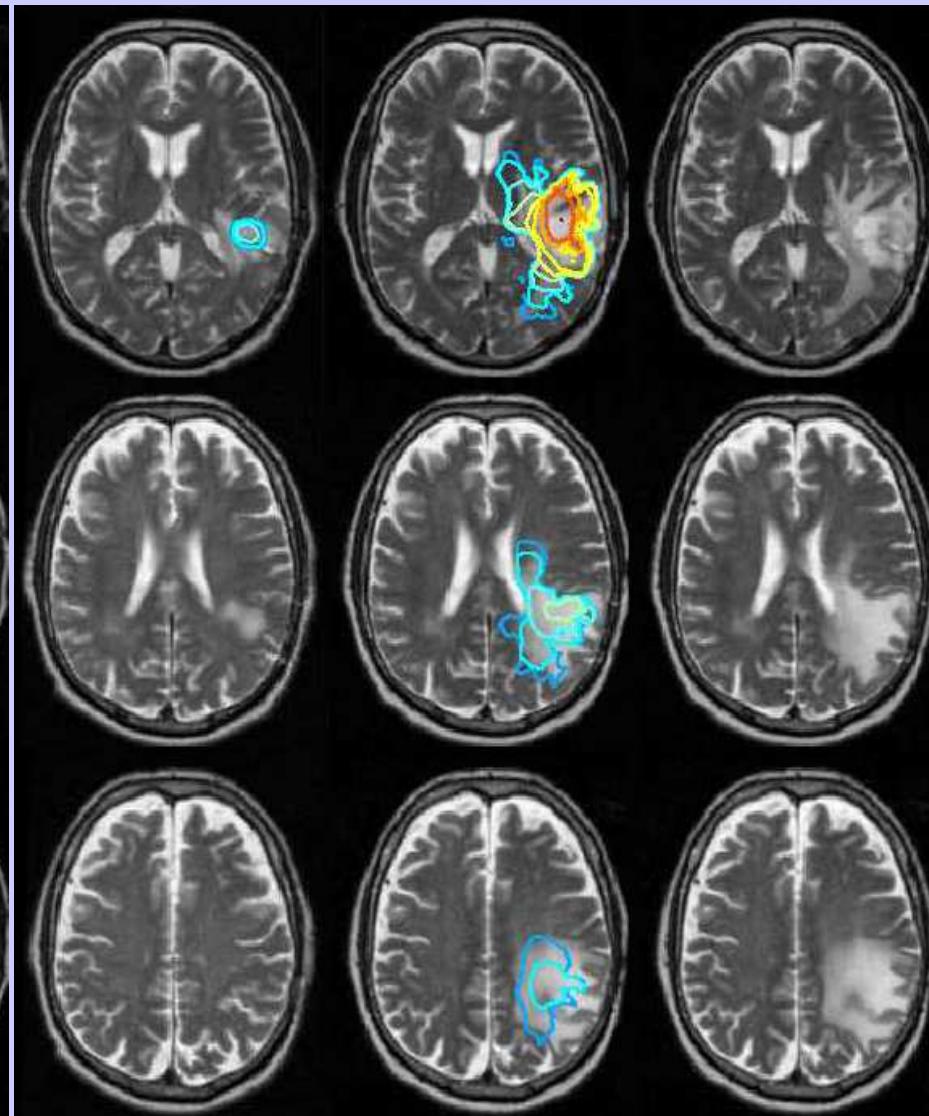
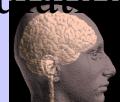




March

08/02/2006

September  
simulation



March

September  
simulation