

Online Blind Calibration of Non-Uniform Photodetectors: Application to Endomicroscopy

Nicolas Savoire¹, Barbara André¹ and Tom Vercauteren¹

¹Mauna Kea Technologies, Paris

Abstract. We present an original method for the online blind calibration of non-uniform photodetectors. The disparity of the detectors may arise from both irregular spatial arrangement and distinct slowly time-varying photometric transfer functions. As natural images are mostly continuous, the signal *collected* by neighboring detectors is strongly correlated over time. The core idea of our method is to translate the calibration problem into relative pairwise calibrations between neighboring detectors followed by the regularized inversion of a system akin to gradient-based surface recovery. From our blind calibration procedure, we design an *online* blind calibration pipeline compatible with clinical practice. *Online blind* calibration is proved to be statistically better than standard *offline* calibration for reconstructing endomicroscopy sequences.

1 The need for online blind calibration in endomicroscopy

In vivo endomicroscopy consists of imaging the tissue at microscopic level, by inserting, through a standard endoscope, a probe made of tens of thousands of optical fibers. A laser scanning unit sends along each fiber an excitation light that is locally absorbed by fluorophores in the tissue and emitted back at a longer wavelength along the same fiber to a photodetector. Raw images are produced at a rate of 9 to 18 frames per second. The standard endomicroscopy image reconstruction scheme proposed by Le Goualher et al. [1] is composed of three steps: estimation of the signal collected by each fiber, compensation of calibration coefficients, and interpolation. Alternative less physically motivated methods [2, 3] use image filtering to remove the fiber honeycomb pattern at the cost of introducing some blur. As described in [1], each fiber i of the endomicroscopy probe acts as a mono-pixel photodetector with an affine transfer function:

$$v_i(t) = \alpha_i u_i(t) + \beta_i \quad (1)$$

where α_i and β_i are respectively the gain and offset of fiber i , $u_i(t)$ is the concentration of fluorophore *seen* at time t by fiber i , and $v_i(t)$ is the signal collected at time t by fiber detector i .

For the estimation of the calibration coefficients, Le Goualher et al. [1] proposed a *offline* non-blind calibration method, assuming constant gain and offset for each fiber. This method compensates for affine fiber transfer functions by

previously acquiring two reference images, one in the air and one in a fluorophore solution, and then deducing from these two images a static offset and a static gain for each fiber. However, fiber coefficients are both slowly time-varying and medium-dependent. Indeed, due to photo-bleaching, autofluorescence signal slowly decreases with illumination time during the course of the procedure unless a long pre-illumination has been performed. In addition, fiber gains also depend on refractive indices and dispersive properties of the observed medium. For these reasons, image quality after the *offline* calibration may be affected by the presence of a *veil* on the image, i.e. a static noise pattern, which can be seen in all three images on the top of Fig. 3. Blindly recovering the parameters of non-uniform photodetectors is an ill-posed problem that has been scarcely addressed in the literature. In the field of astronomy, Kuhn et al. [4] proposed a blind calibration method that requires shifted images of the exact same scene, which can typically not be acquired on *in vivo* samples. The closest work is found in the field of computer vision. Weiss [5] presented an algorithm for blindly recovering intrinsic images from a sequence of natural scenes with different illumination, but only considered detectors on regular grids and with a single gain coefficient. To the best of our knowledge, this paper proposes the first online blind calibration of non-uniform mono-pixel photodetectors.

Our first objective is to design a blind method for the calibration of photodetectors having both irregular spatial arrangement and distinct photometric transfer functions. We then show how our blind calibration can be applied in an online manner to handle slowly time-varying transfer functions.

2 Solving an inverse problem on temporal windows

Let us first focus on static blind calibration. The core observation behind our method is that, when looking at physical objects, neighbor fibers nearly *see* the same *object* signal over time, so the *collected* signal from two neighbor fibers is strongly temporally correlated. This property arises from the mostly continuous nature of natural images, where edges form a set of zero measure and where the noise can be measured for example using total variation as introduced by Rudin et al. [6]. To translate this into mathematical terms, we capture the spatial relationship of the irregularly arranged photodetectors with a Delaunay triangulation applied to fiber locations, and express (1) in terms of a global function $U_t(\mathbf{p})$ which represents the concentration of fluorophore in the observed medium at position \mathbf{p} and time t . Let $G = (V, E)$ the undirected graph associated with the triangulation. In our endomicroscopy probes the fiber pattern is pseudo hexagonal leading to $|E| \simeq 3|V|$. In (1), we substitute for $u_i(t)$ the expression $U_t(\phi(t) + \mathbf{p}_i)$, where \mathbf{p}_i is the spatial position of fiber i relative to the center of probe distal end, and $\phi(t)$ is the spatial position of the probe center at time t . We then have:

$$v_j(t) = \frac{\alpha_j}{\alpha_i}(v_i(t) - \beta_i) + \beta_j + \epsilon_{ij}(t) \quad (2)$$

where $\epsilon_{ij}(t) = (\mathbf{p}_j - \mathbf{p}_i) \cdot \nabla U_t(\mathbf{p}_i + \phi(t)) + o(\|\mathbf{p}_j - \mathbf{p}_i\|)$ is a noise term whose distribution is sparse, with the natural assumption, similar to [6], that spatial

variations of the concentration $U_t(\cdot)$ are almost always smooth. The signals collected by two neighboring fibers can thus be related by the affine relationship $v_j(t) \simeq a_{ij}v_i(t) + b_{ij}$, from which we derive two systems:

$$\{a_{ij} = \frac{\alpha_j}{\alpha_i}\}_{(i,j) \in E} \quad (3)$$

$$\{b_{ij} = \beta_j - \frac{\alpha_j}{\alpha_i}\beta_i\}_{(i,j) \in E} \quad (4)$$

Interestingly, the affine coefficients a_{ij} and b_{ij} may conceptually be seen as the *gradients* of the fiber gain map and of the fiber offset map, respectively, except that the fibers are distributed on a non regular grid. Thus, the problem of recovering the calibration coefficients from the relative pairwise calibrations is akin to recovering a surface from a gradient field [7, 8].

Our blind calibration method is designed in two steps. The first step performs linear regressions on a buffer of collected images to estimate the relative calibration coefficients (a_{ij}, b_{ij}) for all $(i, j) \in E$. Once all regressions have been computed, the second step consists of solving the gain system (3) and the offset system (4), in order to recover the gain α_i and the offset β_i of each fiber i .

2.1 Pairwise relative calibrations of photodetectors

The first step of our blind calibration method consists of estimating relative calibration coefficients a_{ij} and b_{ij} between two observed signals $v_i(t)$ and $v_j(t)$ that are collected by neighboring fibers (i, j) and sampled at times $t \in \{1, \dots, m\}$ without loss of generality. From equation (2), we have: $v_j(t) = a_{ij}v_i(t) + b_{ij} + \epsilon_{ij}(t)$. Noticing that there is measurement error in both variables, an orthogonal linear regression [9] is more appropriate than ordinary least squares regression to estimate a_{ij} and b_{ij} . In order to account for outliers resulting from the non-normality of $\epsilon_{ij}(t)$, the most common example being when an edge occurs between two neighbor fibers, we perform a robust orthogonal regression. For this purpose, we use M-estimators because they are deterministic and computationally competitive compared to other methods. We choose to perform an iteratively reweighted least squares fitting algorithm, which is at iteration p :

$$\hat{\boldsymbol{\theta}}_{ij}^{(p)} = \arg \min_{\{\boldsymbol{\theta}_{ij} | \theta_{1ij}^2 + \theta_{2ij}^2 = 1\}} \sum_{t=1}^m z(r_{ij,t}^{(p-1)}) (\theta_{1ij}v_i(t) + \theta_{2ij}v_j(t) + \theta_{3ij})^2 \quad (5)$$

where $\boldsymbol{\theta}$ represents the regression coefficients, $z(x) = \rho'(x)/x$ is the weight function and $r_{ij,t}^{(p)} = \theta_{1ij}^{(p)}v_i(t) + \theta_{2ij}^{(p)}v_j(t) + \theta_{3ij}^{(p)}$ is the orthogonal residual at iteration p associated with a sample at time t . By choosing the Tukey's biweight function for $\rho(\cdot)$, we ensure that the residuals larger than a cutoff value c are eliminated. We set $c = 4.6851\hat{\sigma}$, where $\hat{\sigma}$ is the median absolute deviation of residuals. Our robust algorithm initialization sets initial slope to s_j/s_i and initial intercept to $\mu_j - s_j\mu_i/s_i$, where μ_i and s_i respectively denote the median and interquartile range of $\{v_i(t)\}_{1 \leq t \leq m}$.

As the probe may contain *dead* fibers that do not transmit any light, any regression between these fibers and their neighbors is sterile. To overcome this issue, we decide to detect and reject regressions which are bad fits, based on a robust goodness-of-fit measure g_{ij} for $(i, j) \in E$. We define g_{ij} as the *weighted* squared Pearson correlation coefficient between v_i and v_j : $g_{ij} = (\sum_{t=1}^m z_{ij,t}(v_i(t) - \bar{v}_i)(v_j(t) - \bar{v}_j))^2 / (\sum_{t=1}^m z_{ij,t}(v_i(t) - \bar{v}_i)^2 \sum_{t=1}^m z_{ij,t}(v_j(t) - \bar{v}_j)^2)$, where $\{z_{ij,t}\}_{1 \leq t \leq m}$ are the final weights of (5) after convergence, and $\bar{v}_i = (\sum_{t=1}^m z_{ij,t}v_i(t)) / (\sum_{t=1}^m z_{ij,t})$. These $\{g_{ij}\}_{(i,j) \in E}$ will be used in the second step of our blind calibration method, focusing on system inversion.

2.2 From relative calibrations to global calibration

Gain estimation The gain system (3) uses the results of an linear orthogonal regression. The symmetry of orthogonal regression implies that noise on the estimates \hat{a}_{ij} is better modeled as multiplicative. Therefore, (3) can be advantageously transposed to the log domain: $\{\alpha_j^* - \alpha_i^* = \hat{a}_{ij}^*\}_{(i,j) \in E}$ with $\alpha_i^* = \log \alpha_i$ and $\hat{a}_{ij}^* = \log \hat{a}_{ij}$. This can be rewritten as $M\alpha^* = \hat{\mathbf{a}}^*$, where M is the $|E| \times |V|$ matrix such as $M_{lp} = \delta_{p,j_l} - \delta_{p,i_l}$, with $E = \{(i_l, j_l), 1 \leq l \leq |E|\}$. In order to cope with noise and *dead* fibers, we introduce the weight function $w(x) = (1 + e^{-(x-g_0)})^{-1} \delta(x \geq g_0)$, where δ is the Kronecker operator. This function puts more weight on the relations of (3) associated with higher goodness-of-fit values, and ignores those associated with values below an arbitrary cutoff value $g_0 = 0.6$. To cope with the non-uniqueness of the solution and regularize the system, we add the a priori that the gains are close to 1. We use the $|E| \times |E|$ diagonal matrix W defined by $W_{ll} = w(g_{i_l j_l})$ to obtain the weighted system:

$$\hat{\alpha}^* = \arg \min_{\alpha^*} \|W(M\alpha^* - \hat{\mathbf{a}}^*)\|^2 + \lambda \|\alpha^*\|^2 \quad (6)$$

The overdetermined system (6) is solved using a conjugate gradient method (LSQR) which has a good numerical stability for ill-conditioned systems. Finally, we deduce the estimated gains $\hat{\alpha} = \exp \hat{\alpha}^*$.

Offset estimation In order to uncouple offset estimation from gain estimation, we approximate α_j/α_i by \hat{a}_{ij} in the offset system (4). As (4) uses the estimates \hat{b}_{ij} resulting from the symmetric orthogonal regression, we symmetrize the offset system by introducing a normalization factor $\gamma_{ij} = (1 + \hat{a}_{ij}^2)^{0.5}$: $\beta_j/\gamma_{ij} - (\hat{a}_{ij}/\gamma_{ij})\beta_i = \hat{b}_{ij}/\gamma_{ij}$. In order to regularize the system, we make the assumption \mathcal{A} that fiber background $\beta(t)$ at time $t > t_0$ can be approximated by $q\beta_0$ where β_0 is an initial offline background estimation and q is an unknown global factor only depending on t [10]. Injecting $\beta_i = q\beta_{0i}$ in (4) gives: $q\beta_{0j} - \hat{a}_{ij}q\beta_{0i} \simeq b_{ij}$. A robust estimate of q is then: $\hat{q} = \text{median}_{(i,j) \in E} \{\hat{b}_{ij}/(\beta_{0j} - \hat{a}_{ij}\beta_{0i})\}$. From this estimate \hat{q} , we obtain an approximation $\hat{q}\beta_0$ of β and use this value to regularize the system (4). Weighting the system as described in 2.2, offset estimation is rewritten as:

$$\hat{\beta} = \arg \min_{\beta} \|W(A\beta - \frac{1}{\gamma}\hat{\mathbf{b}})\|^2 + \lambda \|\beta - \hat{q}\beta_0\|^2 \quad (7)$$

where A is the $|E| \times |V|$ matrix such as $A_{lp} = (\delta_{p,j_l} - \delta_{p,i_l} \hat{a}_{i_l j_l}) / \gamma_{i_l j_l}$. Being similar to system (6), the system (7) is solved using LSQR.

2.3 Online blind calibration pipeline

Our second objective is to integrate the blind calibration method described in Section 2.2 into an online calibration pipeline, illustrated in Fig. 2. For this purpose, we leverage the fact that the temporal variation of fiber transfer functions are quite slow compared to the temporal variation of fluorescence signal which is due to either motion within the tissue, or motion of the probe along the tissue during endomicroscopy procedure. We thus decide to apply our blind calibration method on temporal windows where transfer functions do not significantly change, and to perform successive calibration updates as soon as possible. At startup of the imaging system, the probe is in the air and laser illumination allows to record the non-fluorescent background signal β_0 . Standard *offline* calibration can be used as initial calibration. When the physician starts the acquisition at time T_0 , successive frames are accumulated in a buffer until there is sufficient data to make system inversion possible. Our intuition is that the more moving fluorescent signal there is, the better linear regression results are, and so the more chance there is to solve the system. We consider that there is sufficient data if the following criterion \mathcal{C} is satisfied: $|\{(i, j) \in E, g_{ij} \geq g_0\}| \geq 0.9|E|$. Regressions are performed until time T_1 when \mathcal{C} is satisfied, then we perform system inversion and proceed to the first calibration update. At k^{th} calibration update, buffer is flushed at $t = T_k + 1$ and new frames are accumulated in the buffer from $t = T_k + 1$ to $t = T_{k+1}$ when $(k + 1)^{\text{th}}$ calibration is possible. From the gains $\hat{\alpha}^{T_k}$ and the offsets $\hat{\beta}^{T_k}$ estimated at time T_k , we construct the new calibrated signal as follows: $\forall t \in]T_k, T_{k+1}]$, $\hat{u}_i(t) = (v_i(t) - \hat{\beta}_i^{T_k}) / \hat{\alpha}_i^{T_k}$. This provides an estimate of the fluorophore concentration $u_i(t)$ seen by fiber i at time t . Finally, interpolation of \hat{u} is performed.

3 Evaluation and results

Before method evaluation, we aim at validating the assumption $\mathcal{A} : \beta = q\beta_0$. For this purpose, we tested 4 probes having different numbers of fibers and different optical properties. Each probe was used to acquire every minute a 10-frame average image in the air. Laser illumination was continuously on during the first 14 minutes in order to measure autofluorescence decrease. After 14 minutes, to highlight the phenomenon of autofluorescence recovery, illumination was off except during acquisition of the images. We then calculated the Pearson correlation between the background signal of all fibers at time t and those at time $t_0 = 0$. The results presented in Fig. 1 on the right, reveal that, for all 4 probe models the Pearson correlation coefficient is quite high, being superior to 0.98, therefore validating \mathcal{A} .

Our database used for method evaluation is composed of 89 endomicroscopy sequences acquired during clinical procedures in 6 different medical centers. Each

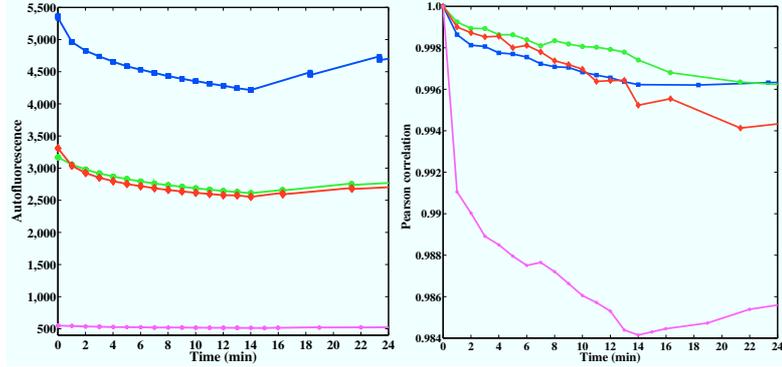


Fig. 1: Left: Autofluorescence decrease ($t \leq 14min$) and recovery ($t > 14min$), measured for 4 different probe models. Right: Corresponding Pearson correlation values between fiber signal at time t and at time t_0 .

of these 89 sequences is complete in the sense that every single image from startup to shutdown was recorded. We propose to evaluate first the ability of our calibration method to recover the model parameters, then the impact of the calibration on image reconstruction. Since it is impossible to get an uniform medium with the same physical properties as a given observed living tissue, validation cannot rely on flat-field images.

Our online pipeline implies that calibration applied on *current* data is only computed from *past* data. This ensures unbiased performance evaluation on reconstructed data. Given a temporal window $[T_k, T_{k+1}]$ where the calibration is static, we define a static calibration quality CQ_k which measures the ability to align the calibrated gains of two neighboring fibers from the model parameters estimated on $[T_{k-1}, T_k]$: $CQ_k = |\{(i, j) \in E, 1 - \eta < \hat{a}_{ij}^{T_{k+1}} \cdot \hat{\alpha}_i^{T_k} / \hat{\alpha}_j^{T_k} < (1 + \eta)^{-1}\}| / |E|$, where $\hat{a}_{ij}^{T_{k+1}}$ is the relative calibration estimated between fiber i and fiber j on the temporal window $[T_k, T_{k+1}]$, and η is an arbitrary threshold set to 0.1. The expression $\hat{a}_{ij}^{T_{k+1}} \cdot \hat{\alpha}_i^{T_k} / \hat{\alpha}_j^{T_k}$ is basically an unbiased estimation of the residuals of (6). CQ_k therefore provides an unbiased measure of how good we would be at reconstructing a flat image from a flat signal with the same physical properties as the observed medium. We then define the global calibration quality CQ of the whole video sequence as the average of static calibration quality values. According to the results presented in Fig. 2 on the left, *online* blind calibration yields statistically higher calibration quality than *offline* calibration (95% confidence interval of $[0.13, 0.19]$ using paired difference *t*-test). Visual inspection of worst cases revealed that the sequences for which *offline* calibration performs similarly or slightly better contains either mostly noise, static fluorescence signal, non-sufficient moving fluorescent signal or only thin fluorescent structures. For all 89 sequences, the first *online* calibration succeeded after less than 30 seconds of moving fluorescent signal, a delay which is clearly compatible with

clinical practice. Regarding the sequences acquired with a probe of $n = 10,000$ fibers for example, computation time was less than 4 ms per frame in the buffer for performing all regressions, and less than 300 ms for system inversion.

We then propose to evaluate the impact of the calibration on image reconstruction by measuring the noise (static and dynamic) in a calibrated sequence. For this purpose, we compute the average of the (Delaunay-based) total variation [6] on all T frames of the sequence: $\sum_{t=1}^T \sum_{(i,j) \in E} |\hat{u}_i(t) - \hat{u}_j(t)| / (|E|T)$. Results show that the measured noise is statistically lower after *online* blind calibration than after *offline* calibration (95% confidence interval of $[-55, -33]$ using paired difference t -test). The improvement of image quality, from *offline* to *online* calibration, can be qualitatively appreciated on still images presented in Fig. 3, and on two video sequences acquired on the bile duct and on the colon, available as Supplemental Material (<http://youtu.be/1WYEQysDBqQ>).

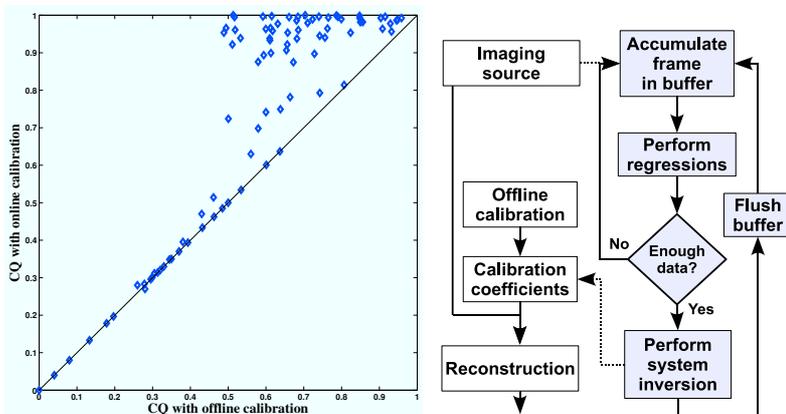


Fig. 2: Left: Calibration Quality (CQ) of 89 sequences processed by *online* versus *offline* calibration. Right: Pipeline of *online* blind calibration, highlighted in gray boxes. Dotted arrows show source input (top) and calibration update (bottom).

4 Conclusion

We have presented an original method for *online blind* calibration of non-uniform photodetectors, where only past signal is used to calibrate current signal in a transparent way to the user. By performing robust linear regressions and regularizing an ill-posed inverse problem, our method is able to handle photodetectors having both irregular spatial arrangement and individual slowly time-varying photometric transfer functions. Using a relatively large database of complete sequences acquired during clinical endomicroscopy procedures, we have demonstrated that *online* blind calibration statistically outperforms standard *offline*

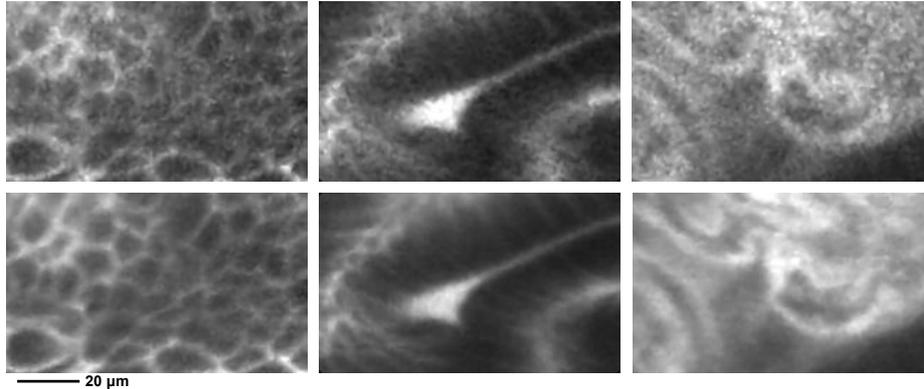


Fig. 3: Endomicroscopy image portions of Barrett's Esophagus, from 3 sequences processed by *offline* calibration (top) or *online* calibration (bottom). Bottom images appear much less noisy although no spatial smoothing is performed by *online* calibration.

calibration. For future work, we plan to evaluate whether *online* blind calibration leads to higher perceived image quality and better diagnostic performance for the physicians.

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