# Lecture 8 Generative Adversarial Networks

Deep Learning for Computer Vision Valeriya Strizhkova 9 November 2021

# About myself

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1st year PhD student @ Inria, STARS team

https://scholar.google.ru/citations?user=6n5PrUAAAAAJ&hl

https://github.com/valerystrizh



# Lecture Structure

- GANs: Valeriya Strizhkova
- DeepFake Detection: Dr. Antitza Dantcheva

# Outline

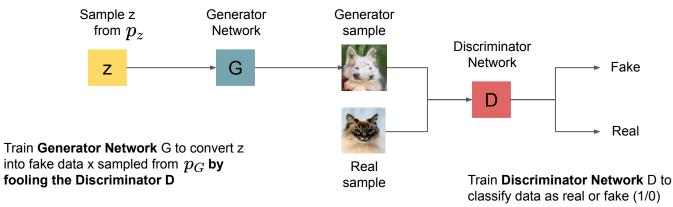
- Basic idea of GAN
- Image generation
  - Conditional GAN
  - Image-to-image translation (Pix2Pix, CycleGAN)
  - StyleGAN
- Video Generation

# **Generative Adversarial Networks**

- Setup: Assume we have data  $x_i$  drawn from distribution  $p_{data}(x)$ . Want to sample from  $p_{data}$ .
- Idea: Introduce a latent variable z with simple prior p(z).
- Sample  $z \sim p(z)$  and pass to a Generator Network x = G(z)
- Then x is a sample from the Generator distribution  $p_G$ . Want  $p_G = p_{data}$

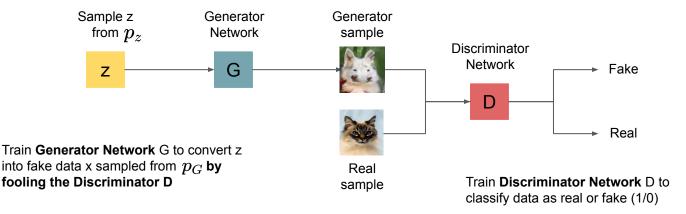
# **Generative Adversarial Networks**

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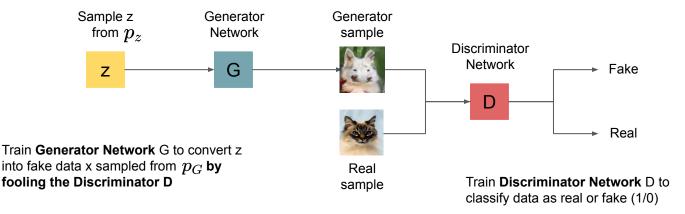
Jointly train generator G and discriminator D with a minimax game

$$\min\max(E_{x\sim p_{data}}[\log D(x)]+E_{z\sim p(z)}[\log(1-D(G(z)))])$$

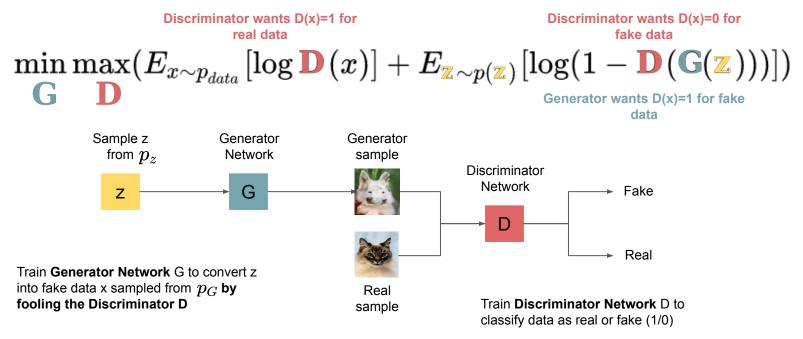


Jointly train generator G and discriminator D with a minimax game

$$\min_{\mathbf{G}} \max_{\mathbf{D}} (E_{x \sim p_{data}}[\log D(x)] + E_{z \sim p(z)}[\log(1 - D(G(z)))])$$



Jointly train generator G and discriminator D with a minimax game



Jointly train generator G and discriminator D with a minimax game

$$\begin{split} \min \max & (E_{x \sim p_{data}} \left[ \log \mathbf{D}(x) \right] + E_{\mathbf{Z} \sim p(\mathbf{Z})} \left[ \log(1 - \mathbf{D}(\mathbf{G}(\mathbf{Z}))) \right] ) \\ & = \min \max \mathbf{V}(\mathbf{G}, \mathbf{D}) \\ & \mathbf{G} \quad \mathbf{D} \end{split}$$

Train G and D using alternating gradient updates:

1. Update 
$$\mathbf{D} = \mathbf{D} + \alpha_{\mathbf{D}} \frac{\delta \mathbf{V}}{\delta \mathbf{D}}$$
  
2. Update  $\mathbf{G} = \mathbf{G} + \alpha_{\mathbf{G}} \frac{\delta \mathbf{V}}{\delta \mathbf{G}}$ 

#### Generative Adversarial Networks: vanishing gradient

$$\min \max_{G} V(G,D) = \min_{G} \max_{D} (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + rac{E_{z \sim p(z)} \left[ \log (1 - D(G(z))) 
ight])}{G D}$$

$$\begin{aligned} \nabla_{\Theta_G} V(G,D) &= \nabla_{\Theta_G} E_{z \sim q(z)} \left[ log(1 - D(G(z))) \right] \\ \nabla_a \log(1 - \sigma(a)) &= \frac{-\nabla_a \sigma(a)}{1 - \sigma(a)} = \frac{-\sigma(a)(1 - \sigma(a))}{1 - \sigma(a)} = -\sigma(a) = -D(G(z)) \\ D(G(z)) \rightarrow 0 \\ & D(G(z)) \rightarrow 0 \end{aligned}$$

$$\\ \bullet \quad \text{Minimize } \left[ -E_{z \sim p(z)} \left[ \log(D(G(z))) \right] \right] \text{ for Generator instead} \end{aligned}$$

$$\\ \text{(keep Discriminator as it is)} \end{aligned}$$

$$egin{aligned} &\min\max_G (E_{x\sim p_{data}}\left[\log D(x)
ight]+E_{z\sim p(z)}\left[\log(1-D(G(z)))
ight])\ &=\min\max_G (E_{x\sim p_{data}}\left[\log D(x)
ight]+E_{x\sim p_G}\left[\log(1-D(x))
ight])\ &G\ D\ &=\min\max_G \int_X (p_{data}(x)\log D(x)+p_G(x)\log(1-D(x)))dx\ &=\min_G \int_X \max_D (p_{data}(x)\log D(x)+p_G(x)\log(1-D(x)))dx \end{aligned}$$

$$egin{aligned} f(y) &= a\log y + b\log(1-y) \ f'(y) &= rac{a}{y} - rac{b}{1-y} \ f'(y) &= 0 \Leftrightarrow y = rac{a}{a+b} \end{aligned}$$

#### **Optimal Discriminator:**

$$D^*_G(x) = rac{p_{data}(x)}{p_{data}(x) + p_G(x)}$$

$$egin{aligned} &\min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log (1 - D(G(z))) 
ight] ) \ &= \min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{x \sim p_G} \left[ \log (1 - D(x)) 
ight] ) \ &= \min_G \int_X (p_{data}(x) \log D^*_G(x) + p_G(x) \log (1 - D^*_G(x))) dx \ & G \end{aligned}$$

Optimal Discriminator: 
$$\ D^*_G(x) = rac{p_{data}(x)}{p_{data}(x) + p_G(x)}$$

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ight] + E_{z \sim p(z)} \left[ \log(1 - D(G(z))) 
ight] ) \ &= \min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{x \sim p_G} \left[ \log(1 - D(x)) 
ight] ) \ &= \min_G \int_X (p_{data}(x) \log D^*_G(x) + p_G(x) \log(1 - D^*_G(x))) dx \ &= \min_G \int_X (p_{data}(x) \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} + p_G(x) \log rac{p_G(x)}{p_{data}(x) + p_G(x)} ) dx \end{aligned}$$

Optimal Discriminator: 
$$D_G^*(x) = rac{p_{data}(x)}{p_{data}(x) + p_G(x)}$$

$$egin{aligned} &\min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log(1 - D(G(z))) 
ight] ) \ &= \min \int_X (p_{data}(x) \log D^*_G(x) + p_G(x) \log(1 - D^*_G(x))) dx \ &G \ &= \min_G \int_X (p_{data}(x) \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} + p_G(x) \log rac{p_G(x)}{p_{data}(x) + p_G(x)} ) dx \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight] ) \end{aligned}$$

$$egin{aligned} &\min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log(1 - D(G(z))) 
ight]) \ &= \min_G \int_X (p_{data}(x) \log D^*_G(x) + p_G(x) \log(1 - D^*_G(x))) dx \ &= \min_G \int_X (p_{data}(x) \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} + p_G(x) \log rac{p_G(x)}{p_{data}(x) + p_G(x)}) dx \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight]) \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight]) \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight] - \log 4) \end{aligned}$$

$$\min_G \max_D (E_{x \sim p_{data}}[\log D(x)] + E_{z \sim p(z)}[\log(1 - D(G(z)))]) \ = \min_G (E_{x \sim p_{data}}[\log rac{p_{data}(x)}{p_{data}(x) + p_G(x)}] + E_{x \sim p_G}[\log rac{p_G(x)}{p_{data}(x) + p_G(x)}] - \log 4)$$

Kullback-Leibler Divergence: 
$$\,KL(p,q)=E_{x\sim p}[lograc{p(x)}{q(x)}]$$

$$egin{aligned} &\min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log (1 - D(G(z))) 
ight] ) \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight] - \log 4 ) \ &= \min_G (KL(p_{data}, rac{p_{data} + p_G}{2}) + KL(p_G, rac{p_{data} + p_G}{2}) - \log 4) \end{aligned}$$

Kullback-Leibler Divergence: 
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ight]+E_{x \sim p_{G}}\left[\lograc{p_{G}(x)}{p_{data}(x)+p_{G}(x)}
ight]-\log4)\ &=\min_{G}(KL(p_{data},rac{p_{data}+p_{G}}{2})+KL(p_{G},rac{p_{data}+p_{G}}{2})-\log4) \end{aligned}$$

#### Jensen-Shannon Divergence: $JSD(p,q) = \frac{1}{2}KL(p,\frac{p+q}{2}) + \frac{1}{2}KL(q,\frac{p+q}{2})$

$$egin{aligned} &\min \max_G (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log (1 - D(G(z))) 
ight] ) \ &= \min_G (E_{x \sim p_{data}} \left[ \log rac{p_{data}(x)}{p_{data}(x) + p_G(x)} 
ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
ight] - \log 4 ) \ &= \min_G (KL(p_{data}, rac{p_{data} + p_G}{2}) + KL(p_G, rac{p_{data} + p_G}{2}) - \log 4) \ &= \min_G (2 imes JSD(p_{data}, p_G) - \log 4) \end{aligned}$$

#### Jensen-Shannon Divergence: $JSD(p,q) = \frac{1}{2}KL(p,\frac{p+q}{2}) + \frac{1}{2}KL(q,\frac{p+q}{2})$

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ight] + E_{x \sim p_G} \left[ \log rac{p_G(x)}{p_{data}(x) + p_G(x)} 
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JSD is always nonnegative and zero when the two distributions are equal

=> the global minimum is 
$$p_{data} = p_G$$

Jensen-Shannon Divergence:  $JSD(p,q) = \frac{1}{2}KL(p,\frac{p+q}{2}) + \frac{1}{2}KL(q,\frac{p+q}{2})$ 

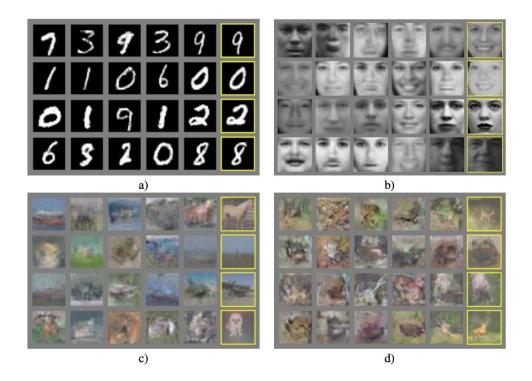
$$\min_{G} \max_{D} (E_{x \sim p_{data}} \left[ \log D(x) 
ight] + E_{z \sim p(z)} \left[ \log(1 - D(G(z))) 
ight])$$

$$= \min_G (2*JSD(p_{data},p_G) - \log 4)$$

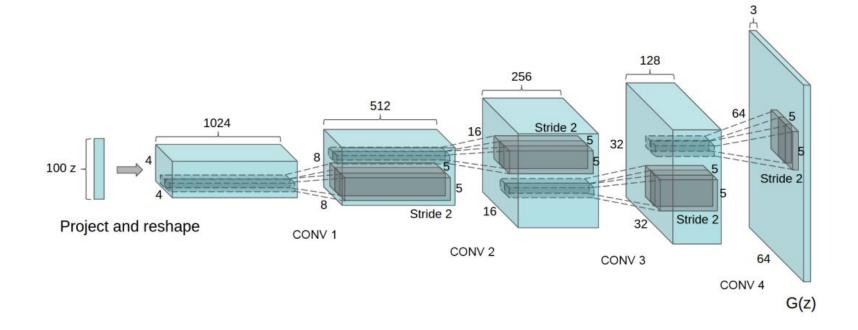
Summary: The global minimum of the minimax game happens when:

1. 
$$D_G^*(x) = rac{p_{data}(x)}{p_{data}(x) + p_G(x)}$$
 (Optimal discriminator for any G)  
2.  $p_G(x) = p_{data}(x)$  (Optimal generator for optimal D)

# Generative Adversarial Networks: results



### Generative Adversarial Networks: DC-GAN

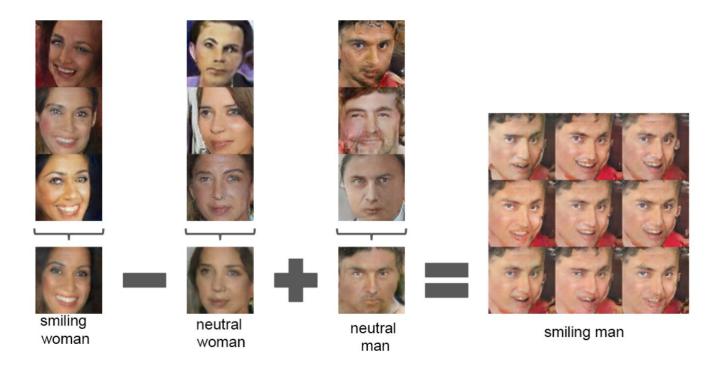


### **Generative Adversarial Networks: Interpolation**



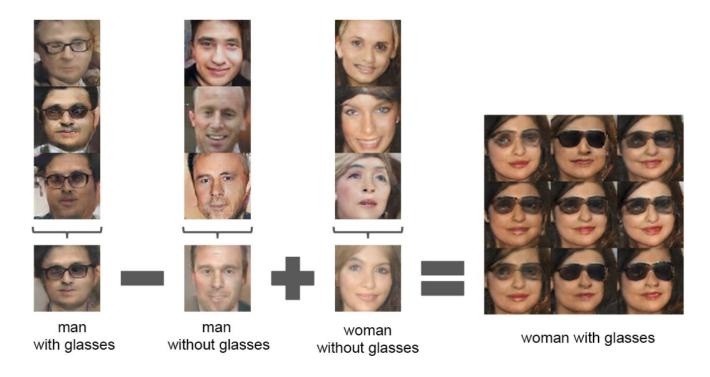
Alec Radford, Luke Metz, Soumith Chintala. Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks. ICLR 2016

### Generative Adversarial Networks: Vector Math



Alec Radford, Luke Metz, Soumith Chintala. Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks. ICLR 2016

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Alec Radford, Luke Metz, Soumith Chintala. Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks. ICLR 2016

# **GAN: Improved Loss Functions**

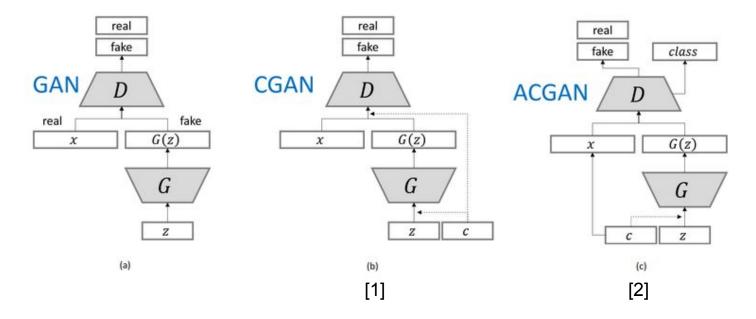




[1] Martin Arjovsky, Soumith Chintala, Léon Bottou. Wasserstein GAN. 2017

[2] Ishaan Gulrajani, Faruk Ahmed, Martin Arjovsky, Vincent Dumoulin, Aaron Courville. Improved Training of Wasserstein GANs. NeurIPS, 2017.

# **Conditional GANs**

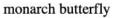


[1] Mehdi Mirza, Simon Osindero. Conditional Generative Adversarial Nets. 2014

[2] Augustus Odena, Christopher Olah, Jonathon Shlens. Conditional Image Synthesis With Auxiliary Classifier GANs. ICML 2016

# **Conditional GANs**







goldfinch



daisy



redshank



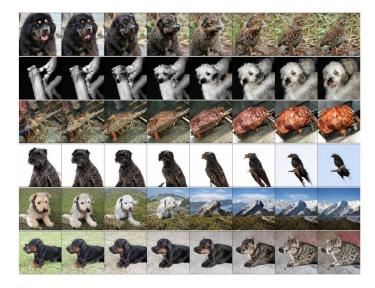
grey whale

Augustus Odena, Christopher Olah, Jonathon Shlens. Conditional Image Synthesis With Auxiliary Classifier GANs. ICML 2016

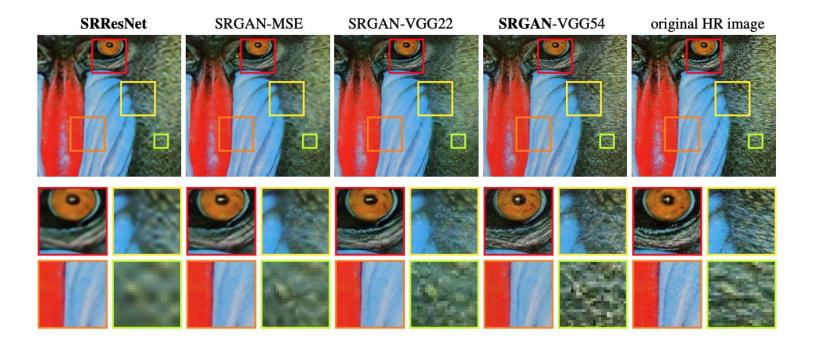
# Conditional GANs: BigGAN



Figure 6: Samples generated by our BigGAN model at 512×512 resolution.

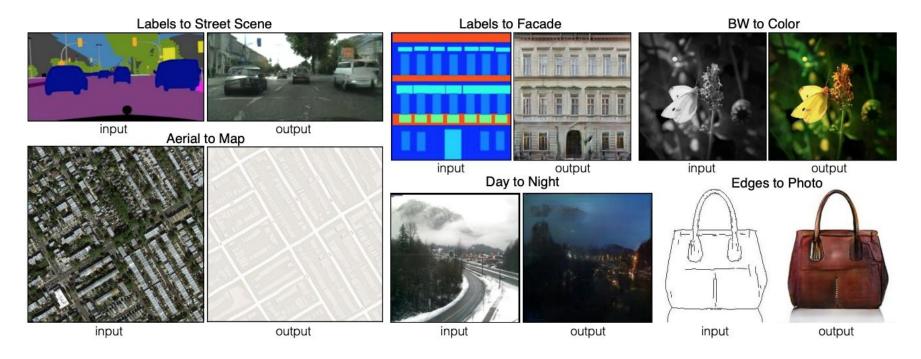


# **Image Super-Resolution**



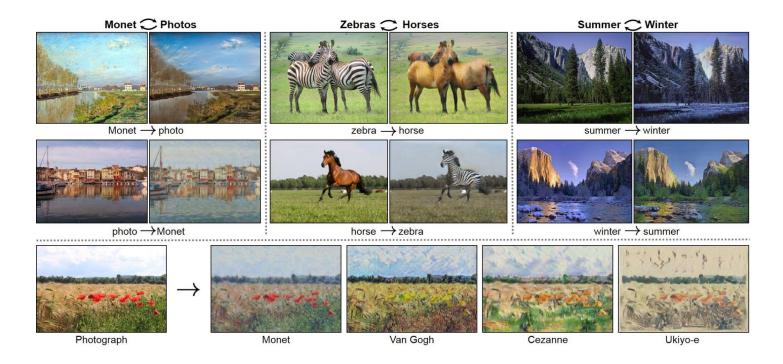
Christian Ledig, Lucas Theis, Ferenc Huszar, Jose Caballero, Andrew Cunningham, Alejandro Acosta, Andrew Aitken, Alykhan Tejani, Johannes Totz, Zehan Wang, Wenzhe Shi. Photo-Realistic Single Image Super-Resolution Using a Generative Adversarial Network. CVPR 2017

# Image-to-Image Translation: Pix2Pix



Phillip Isola, Jun-Yan Zhu, Tinghui Zhou, Alexei A. Efros. Image-to-Image Translation with Conditional Adversarial Networks. CVPR 2017

# Unpaired Image-to-Image Translation: CycleGAN



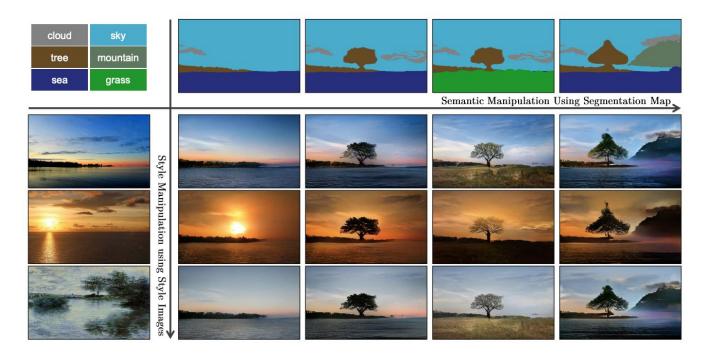
Jun-Yan Zhu, Taesung Park, Phillip Isola, Alexei A. Efros. Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks. ICCV 2017

# Unpaired Image-to-Image Translation: CycleGAN



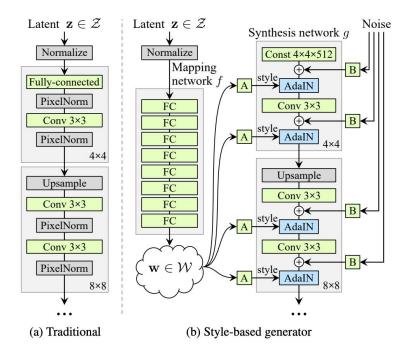
Jun-Yan Zhu, Taesung Park, Phillip Isola, Alexei A. Efros. Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks. ICCV 2017

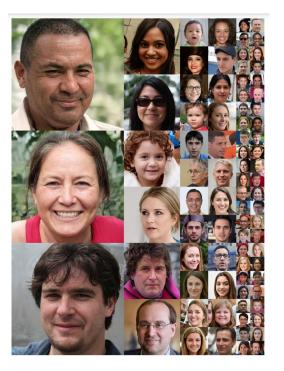
# Label Map to Image



Taesung Park, Ming-Yu Liu, Ting-Chun Wang, Jun-Yan Zhu. Semantic Image Synthesis with Spatially-Adaptive Normalization. CVPR 2019

# StyleGAN





Tero Karras, Samuli Laine, Timo Aila. A Style-Based Generator Architecture for Generative Adversarial Networks. CVPR 2019

# **Video Generation**



Aliaksandr Siarohin, Stéphane Lathuilière, Sergey Tulyakov, Elisa Ricci, Nicu Sebe. First Order Motion Model for Image Animation. NeurIPS 2019

# Video Generation



Caroline Chan, Shiry Ginosar, Tinghui Zhou, Alexei A. Efros. Everybody Dance Now. ICCV 2019

# **GAN Summary**

Jointly train two networks:

Discriminator classifies data as real or fake

Generator generates data that fools the discriminator

